



Improved Winding Design of  
a Doubly Fed Induction Generator (DFIG)  
Wind Turbine using  
Surrogate Optimisation Algorithm

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To my father, Yueting Tan  
and my mother, Hong Zheng



## Abstract

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The use of renewable sources of energy is becoming increasingly important role in electricity generation. Wind energy is the fastest growing renewable energy source and is making a significant contribution to meeting the energy demands while still reducing CO<sub>2</sub> emissions. In designing generators for installation in wind turbines, characteristics of high efficiency and low cost are among the first to consider. As the number of installed wind turbines increases across the world, questions of turbine component failure and repair are also receiving much attention.

This PhD starts with the investigation of modern wind turbine generator design with a focus on electrical generator and its operation. The finite element analysis of an off-the-shelf 55 kW doubly fed induction generator is used as a case study in order to investigate its design and improve the machine performance.

The main work of this PhD is on a novel approach by surrogate-based analysis and the optimisation of winding design and rewinding design based upon the doubly fed induction generator for energy efficiency improvement. Surrogate models of the machine are constructed using Latin Hypercube sampling and the Kriging modelling. Having validated the surrogate models, the particle swarm optimisation algorithm is developed and applied to find the optimal solution.

Assuming a winding failure occurs mid-life of the wind turbine, three optimisation plans have been studied for the repair and re-design of the stator and rotor winding separately and in combination.

To validate the optimisation results, an improved testing standard is developed to test doubly fed induction generator. The original machine is then rewound following the optimised plan and tested to determine the difference in performance. By comparing the two machines, improved performance is achieved both in optimisation simulation and experiments.

Finally an annual wind speed profile at a specific location (Albemarle site) is analysed to estimate wind power. The Weibull distribution of the wind speed data is combined with the turbine topologies for estimating the annual wind energy production. The annual power generation from the two machines is compared to validate the proposed technology.



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# Acronyms and Symbols

## List of Symbols

$A$	cross-sectional area
$A_s$	swept area of rotor
$B$	magnetic field density
$C_M$	torque coefficient
$C_{p,max}$	power coefficient and maximum power coefficient
$C_{1,2}$	acceleration factor
$c$	scale factor
$D_{bearing,r}$	inner diameter of the bearing and the rotor diameter
$F$	bearing load
$f$	frequency
$H$	magnetic field intensity
$H_s$	significant wave height
$H_{1,2}$	turbine height
$I$	current
$J$	current density
$K_e$	energy pattern factor
$k$	shape factor
$k_{p,d}$	pitch and distribution factor
$k_r$	roughness coefficient
$k_l$	constant coefficient
$k_{h,e}$	hysteresis and eddy current coefficient
$L$	inductance
$L_p$	peak wave length for the wave spectrum
$L_{w,r}$	winding and rotor length
$m$	number of harmonic
$N$	number of winding turns
$N_{PR}$	number of basis function
$N_{ob}$	number of observations
$n$	number of coils per phase
$n_{s,r}$	synchronous speed and rotational speed
$P$	power
$p_j^k$	personal best of particle $j$ at the $k$ th iteration



$p_g^k$	global best of entire swarm at the $k$ th iteration
$p$	number of magnetic pole pairs
$q$	unit vector
$R$	resistance
$R^{-1}$	the inverse of the correlation matrix
$r$	correlation vector
$r_c$	basis function centre
$s$	slip
$T$	torque
$t$	winding temperature
$V$	voltage
$V_w$	wind velocity
$V_j^k$	velocity of the $j$ th at iteration $k$
$\bar{V}_w$	mean wind speed
$w$	inertia weight
$X_j^k$	location of the $j$ th at iteration $k$
$y$	observed data vector
$\hat{y}(t)$	approximation model
$Z$	number of slots
$Z_0$	aerodynamic roughness length
$z_j$	basis function
$z(t)$	fundamental function
$\vartheta$	pitch angle
$\delta$	distribution angle
$\tau_{w,p}$	coil pitch and pole pitch
$\mu_f$	friction coefficient
$\psi$	flux
$\mu_{0,r}$	permeability of the air and material
$\alpha$	frequency exponent
$\beta$	flux density exponent
$\rho_{e,a,c}$	electrical resistivity and density of air and coolant
$\varepsilon$	unobserved random error
$\xi^2$	variance
$\omega_j$	coefficient of linear combinations

$\Phi_i(r)$	radial basis function
$\eta$	efficiency
$\varphi$	uniformly distributed random number
$\omega$	electrical angular speed
$\lambda$	power law exponent
$\sigma^2$	standard deviation
$\eta_{1,2}$	efficiency of drivetrain and generator

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**List of Acronyms**

AC	Alternating current
CFRP	Carbon fibre reinforced plastics
C.S.A	Cross-sectional area
CFD	Computational fluid dynamics
DFIG	Doubly fed induction generator
DC	Direct current
DoE	Design of experiment
FE	Finite element
FEM	Finite element method
GA	Genetic algorithm
GFRP	Glass fibre reinforced plastics
GSC	Grid side converter
HAWT	Horizontal axis wind turbine
LHS	Latin Hypercube sampling
OAD	Orthogonal array design
PMG	Permanent magnet generator
PR	Polynomial regression model
PSO	Particle swarm optimisation
PMSG	Permanent magnet synchronous generator
RSC	Rotor side converter
RBF	Radial basis function
SLL	Stray load loss
SRG	Switched reluctance generator
SCIG	Squirrel cage induction generator
SFIG	Single fed induction generator

SBAO	Surrogate-based analysis and optimisation
VAWT	Vertical axis wind turbine
WRIG	Wound rotor induction generator
2D	2-dimensional
3D	3-dimensional

## Chapter 1 Introduction

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This doctoral thesis focuses on researching a novel approach to the winding design and optimisation of a doubly fed induction generator to improve the machine's efficiency. This chapter gives an overview of the research background and objectives, and then discusses the methodologies used to achieve each objective. The thesis structure is also described in detail.

### 1.1 Background

With increases in the population and economic development activities across the world, energy demand is likely to soar in the coming years, especially in developing countries [1]. In the past decade, the energy consumption of developed countries has grown by 1.5% per year, compared to 3.2% per year in developing countries [2]. Assuming that this trend continues, global energy demand will increase significantly in the future. Currently, there are many different types of energy used to satisfy the world's energy demand. Fossil fuel, which includes coal, petroleum, and natural gas accounts for 80% of total demand; nuclear energy and bioenergy represent approximately 7% and 13.7% respectively; and renewable energy, such as wind and solar energy accounts for 2.2% of total energy demand [3]. It can easily be seen that the excessive dependence on fossil fuel is quite serious today since it is non-renewable, and will therefore be exhausted at some point. Therefore, renewable energy, including wind energy, has already attracted increasing attention, and wind energy alone represents a huge potential source of power.

Wind energy use is increasing significantly, since its development has been encouraged by the policies of many governments throughout the world. Figure 1.1 shows the trend of increasing global cumulative installed wind capacity from 1997 to 2014.

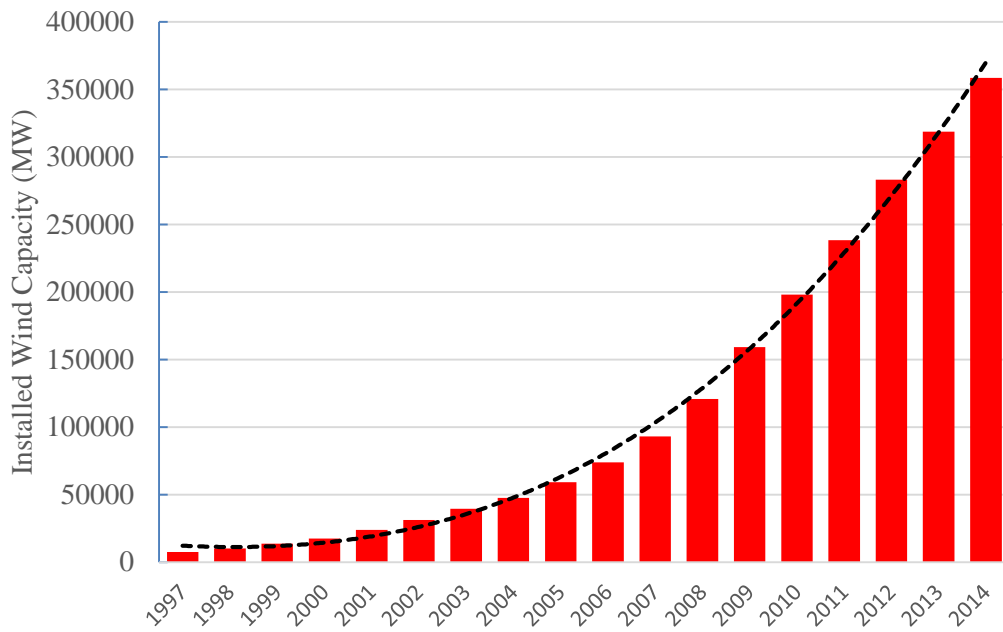


Figure 1.1 Global cumulative installed wind capacity [4].

Figure 1.2 then gives a prediction made by the GWE council of increasing trend of global cumulative wind power capacity [4]. Their moderate scenario estimates the developing trend of cumulative power capacity by considering the existing or planned policies supporting renewable energy worldwide. The advanced scenario assumes that all of these policies to support wind energy development can be achieved. From the chart, it can be seen that the potential for future development is still vast.

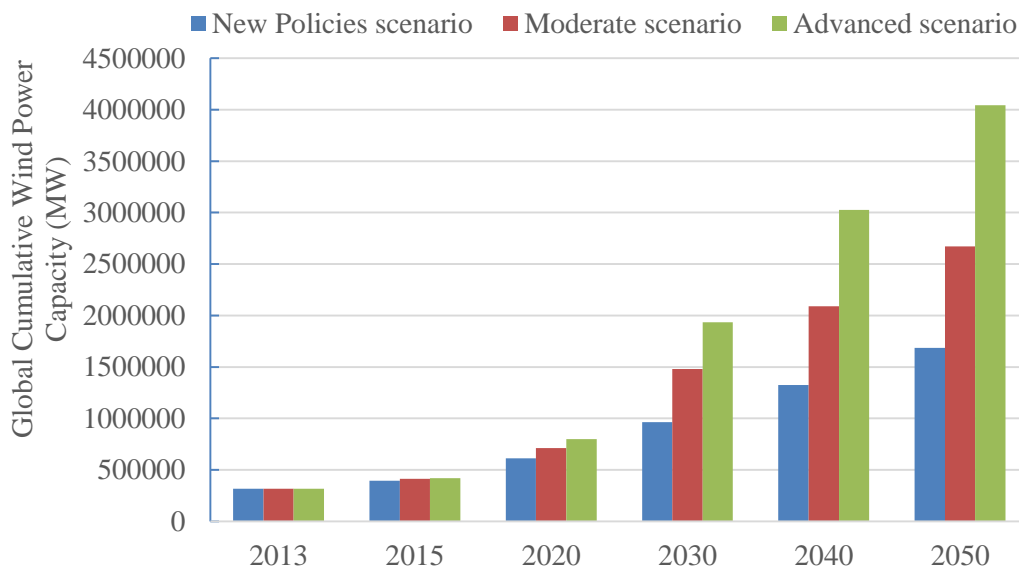


Figure 1.2 The prediction of global cumulative wind power capacity [4].

In the meantime, various different generator technologies have been developed for wind turbines over the last three decades, including the Doubly Fed Induction Generator (DFIG), Permanent Magnet Synchronous Generator (PMSG), and switched reluctance machines. In particular, the PMSG was developed rapidly due to its high power density and high efficiency; hence it attracted many people's attention to develop the relevant technologies. However, an inevitable problem with PMSG, is the materials used, because rare-earth metals are very expensive and scarce, and also the environmental pollution from excavation sites is critical. In addition, with their increased turbine power rates, the cost of the power electronics required rises dramatically. Thus, for these reasons, the DFIG is coming into fashion again. Its advantages, such as high reliability, low cost, lower cost of power electronic components, and variable speed control at constant power, can definitely offset its drawback of giving lower power density than the PMSG. Therefore, nowadays up to 70% of wind turbines installed incorporate DFIGs [5], and they have already been widely used in onshore and offshore wind farms. So the focus of this research is the wind turbine with a doubly fed induction generator.

## **1.2 Motivations and Objectives**

This project focuses on the winding design and optimisation of the DFIG to obtain the maximum power output from the wind turbine, and the objectives of the research are shown as follows:

1. To achieve the rewinding optimisation of the DFIG machine in order to give higher efficiency than the original;
2. To provide a detailed loss characterisation of all the different losses from the DFIG's components;
3. To develop a new method for the precise testing of the DFIG using input-output method with loss segregation under two different operational mode;
4. To validate the results obtained using a laboratory test bench;
5. To estimate the likely improvement in annual wind energy production from a wind turbine at a specific location.

To achieve these objectives, the efficiency of the DFIG for wind turbine applications should be improved. For this purpose, the most suitable optimisation approach and algorithm is determined and applied. The optimisation results are then applied to a wind turbine at a specific site to estimate annual wind energy production.

### 1.3 Methodology

The work described in this thesis concerns the machine winding optimisation of a DFIG wind turbine to acquire the maximum possible power output. In order to achieve the optimisation and to validate the results, the following steps are introduced:

- A design review and analysis of an initial DFIG machine. The software tool used is *Infolytica Magnet* for Finite Element (FE) electromagnetic evaluation.
- The performance of the initial DFIG machine is improved by applying a surrogate optimisation algorithm with the evaluation of different winding parameters, with the help of *Matlab* software based on Finite Element Method.
- The original and optimised DFIG machines are constructed and tested of both to validate the results, which involves exploring a method to test the performance of the DFIG
- The wind speed profile at a specific location is estimated, and the annual wind energy production of the original and optimised DFIG machines is compared.

### 1.4 Thesis Overview

This thesis presents the work conducted on the winding design and optimisation of a DFIG for maximum power output. A total eight chapters are included in the thesis, and a brief description of each is provided as follows:

Chapter 2 is a review chapter covering the history and development of wind turbines, wind turbine topologies, modern wind turbine design, the selection of turbine generators, the principles of the DFIG, and types of failure in turbine generators.

Chapter 3 describes a mechanical design review of a DFIG machine and the losses in different components of DFIG are discussed. A finite element analysis of the original DFIG machine is presented.

Chapter 4 proposes a novel method of constructing a surrogate model of the DFIG based on finite element method, and also an optimisation algorithm is chosen to achieve optimisation.

Chapter 5 compares several of the main international test standards for induction machines. Based on the IEEE standard 112-B, an improved method for testing the DFIG is carried out.

Chapter 6 validates the results of the simulation and practical work for the original designed machine and the optimised rewind machine based on the proposed optimisation algorithm.



Chapter 7 investigates the statistical analysis of the wind speed profile for a specific site. The annual wind energy production at this site is then estimated using the Weibull probability density function.

Chapter 8 gives main conclusions of the study and recommendations for further work.

## 1.5 Contribution to Knowledge

This thesis contributes to knowledge in the following areas:

- Development of surrogate modelling for use in the design of electromagnetic applications.
- Methodology for the winding optimisation of the DFIG.
- Exploration of the selection of different winding parameters for both stator and rotor in machine designing, instead of empirical formula.
- Development of a testing method for the DFIG.
- Segregation of all losses in different machine components, especially the addition loss – stray load loss.

## 1.6 Published Work

The following peer-reviewed conference and journal papers have stemmed from this research:

- a) Z. Tan, X. Song, W. Cao, Z. Liu, and Y. Tong, “DFIG Machine Design for Maximizing Power Output Based on Surrogate Optimization Algorithm,” *IEEE Transaction on Energy Conversion*, vol. 30, Issue 3, pp. 1154-1162, September 2015.
- b) Z. Tan, X. Song, B. Ji, Z. Liu, J. Ma, and W. Cao, “3-D thermal analysis of a permanent magnet motor with cooling fans,” *Journal of Zhejiang University-Science A*, ISSN 1673-565X, August 2015.
- c) Z. Tan, N. J. Baker, W. Cao, “Novel optimisation algorithm for electrical machines,” *the 8<sup>th</sup> IET International Conference on Power Electronics, Machines and Drives (PEMD)*, UK, 2016.
- d) Z. Tan, W. Cao, Z. Liu, X. Song, and B. Zahawi, “Optimization of doubly fed induction generators (DFIGs) for Maximizing the Wind Power Yield,” *the Ninth International Symposium on Linear Drives for Industry Applications Conference (LDIA'13)*, 2013.
- e) W. Cao, Z. Tan, Y. Xie, B. Zahawi, A. Smith, and M. Jovanovic. “Analysis of wind power data for optimising DFIGs,” *the 2<sup>nd</sup> International Symposium on Environment Friendly Energies and Applications Conference (EFEA)*, pp. 452-457, June 2012.

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- f) W. Cao, Y. Xie, and Z. Tan, “Wind Turbine Generator Technologies,” Book Chapter in *Advances in Wind Power*, INTECH, pp. 177-204, November 2012.
  - g) Z. Liu, W. Cao, Z. Tan, B. Ji, X. Song, and G. Tian, “Conditional monitoring of doubly-fed induction generators in wind farms,” *the Ninth International Symposium on Linear Drives for Industry Applications (LDIA '13)*, 2013.
  - h) Z. Liu, W. Cao, Z. Tan, X. Song, B. Ji, and G. Tian, “Electromagnetic and temperature field analyses of winding short-circuits in DFIGs,” *the IEEE International Symposium on Diagnostics for Electrical Machines, Power Electronics & Drives (SDEMPED)*, Spain, August, 2013.
  - i) N. Yang, W. Cao, Z. Tan, X. Song, and T. Littler, “Novel asymmetrical rotor design based on surrogate optimization algorithm,” *the 8<sup>th</sup> IET International Conference on Power Electronics, Machines and Drives (PEMD)*, UK, 2016.
  - j) N. Yang, W. Cao, Z. Liu, Z. Tan, Y. Zhang, S. Yu, and J. Morrow, “Novel asymmetrical rotor design for easy assembly and repair of rotor windings in synchronous generators,” *the 2015 IEEE International Magnetism Conference (INTERMAG)*, Beijing, China, May 2015.

## **Chapter 2 Literature Review**

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In this chapter, the wind turbine history of development is introduced at the beginning. In addition, an up-to-date survey of the current state of wind turbine technology is presented, the benefits and the challenges associated with wind energy is discussed. As one of the most important parts of turbine design, the generator design and its characteristics are considered. The aim of this thesis is to present work done on the winding repair and re-design of doubly fed induction generator to obtain the maximum power output for a specific wind turbine. So the survey will focus more on introducing the turbine generator design and the modern wind turbine topologies.

## 2.1 Wind Energy

In recent years, major research in the electricity generation area has focused on the advancement of wind energy as the main source of renewable energy. Wind energy has a lot of advantages over conventional fossil fuel. First of all, wind energy does not emit harmful gases or hazardous materials to pollute the air or water sources and while nuclear power plants; it does not produce hazardous by products either, which are quite hard to deal with safety. Secondly, wind energy as a clean fuel does not lead to CO<sub>2</sub> or other atmospheric emissions, which cause acid rain or greenhouse gases. Thirdly, wind power is one of the cheapest energy technologies available today, depending on the wind resources available. Wind resources are inexhaustible, and so wind energy as a clean and sustainable source of renewable energy could reduce dependence on fossil fuels.

However, here are challenges too. Normally, sufficient wind resources exist in remote places, far from the urban areas, so if the local power absorptive capacity is not strong enough, the electricity will have to be delivered from wind farms to cities, but both the long building cycle and coordination ability of power grid are very difficult to be solved. As a result, the wind turbine has to be abandoned as the only one choice by power grid operator. Beside this, wind energy does have an effect on the environment; it is well known that noise radiation from a wind turbine is recognized as one of the key features controlling its public acceptability [6], and for this reason, researchers have tried to reduce the mechanical and aerodynamic noise of wind turbines [7, 8]. Furthermore, the aesthetic pollution and wildlife protection have been referred to as well. Generally, before wind farms are built, the analysis of aesthetic sensitivity should be combined with concern for the local environment, and there are a lot of ways to build aesthetic sensitivity have been listed [9].

In addition, the death rates of birds are quite high when they fly into the rotors. Today, many wind energy research groups are trying their best to solve this problem, even though birds colliding with wind turbines do not always happen. For example, the Energy Technology Support Unit (ETSU) started a series of activities to reduce the death rates of birds during a wind energy project in the United Kingdom [10]. With all these factors in mind, it is imperative for researchers to come up with improved methods to increase wind energy utilization and reduce its effects on the environment.

## 2.2 Wind Turbines Past and Present

The windmill was invented several centuries ago. As a source of power for grain milling and water pumping, wind was first used for electricity generation over a hundred years ago, when a windmill was built in Scotland in 1887 by James Blyth [11]. In 1891, the Danish scientist, Poul la Cour constructed a wind turbine to generate electricity to light the Askov High School [12]; after four years in 1895, he converted this into a prototype electrical power plant that was used to light the village of Askov [12]. At the beginning of the 1930s, the wind turbine technology with low power capacity was widely promoted and applied.

In 1941, Palmer Cosslett Putnam designed the world's first megawatt-sized wind turbine, which was connected to the local electrical distribution system on a mountain in the USA [13]. In order to find cheaper energy sources, many countries in the world placed their hopes on wind energy in the 1960s. In the meantime, some large-scale wind turbines were built by investing a lot of manpower and material and financial resources. Research at this time proved that small-scale wind turbines are relatively economical, but large-scale wind turbines are quite expensive compared to the power generated from fossil fuels. In this period, the prevailing challenge faced by the wind turbine development was cost, which caused research into wind energy to stagnate.

In 1973, the fuel crisis erupted across the whole world, and many countries encountered the dilemma of energy shortages. Therefore, research into wind energy resumed again in developed countries including the United States, United Kingdom, and Denmark. Medium-sized and large wind turbines of low cost and high reliability were developed. In 1978, the Tvind wind turbine was put into operation; at that time this was representative of the state of the art in wind energy. In 1980, the Nortank 55kW wind power generator was unveiled in Denmark, and the price of wind power had been reduced by about 50%. Wind energy technology was becoming more and more mature.

The 21st century has seen a huge development in wind turbine manufacture, as improvements in machine design and advancements in power electronics came to play a key role in the development of wind energy. Wind turbine manufacturers have come up with many different directions to improve current technologies. Some of these new wind turbines are already in production and are distributed for consumer use, whilst other are still in concept form for the future. A few prominent wind turbine companies currently present in the wind energy market are mentioned below.

- Vestas, is a Danish wind turbine company which has the largest market share in the world. Its production facilities have already been distributed in more than 12 countries, such as China, Spain, and the United States. In the 1990s, Vestas produced a highly reliable, advanced 55kW/11kW wind turbine, which has been called the beginning of modern wind turbines.
- GoldWind, is a Chinese wind turbine manufacturer which is engaged in developing and producing large permanent magnet wind turbine generators. The major products of GoldWind are 1.5MW and 2.5MW permanent magnet direct drive wind turbines.
- Siemens, is a famous Germany company in the wind energy field. Both onshore and offshore wind projects can be handled by Siemens, and its major aim is to reduce the costs of wind turbines.
- GE, wind turbines produce of with the highest annual energy yield in the world at 2MW and 3MW.

Nowadays, wind energy is the fastest growing renewable energy in the world; there were over two hundred thousand wind turbines in operation, with a total nameplate capacity of 282482 MW, at the end of 2012 [14]. The marketing scale is expanding continuously, and so the cost of wind energy is falling. In some places, the price of wind energy can compete with power plants using fossil fuels. Although there is still a lot of work to be done on wind energy, the sector is facing a promising future.

### **2.3 Overview and Topologies of Wind Turbines**

There are a wide range of topologies established today for wind turbines, with different designs of components and control methods explored to make the wind turbines more efficient, reliable and safer. Most of these designs concentrate on the rotors of the wind turbines. The main choices of wind turbine topology are introduced below.

#### **2.3.1 Rotor Axis Orientation**

The rotor axis orientation is the fundamental selection when designing a wind turbine. There are two types of rotor axis orientation: the Horizontal Axis Wind Turbine (HAWT) and Vertical Axis Wind Turbine (VAWT). The VAWT does not need a yaw system, and thus the wind power can be captured from any direction. Moreover, its blades have a chord and no twist [15], which could reduce complexity and costs. Although there are several promising advantages of the VAWT, this kind of design has not been accepted widely, due to the likelihood of fatigue damage to the blades, and especially since the connection points to the rotor are even weaker.

On the other hand, another problem with the VAWT is control, such as variable pitch control. In this case, stall control is the primary method in high winds, which causes a higher-rated wind speed accordingly. Therefore, the space requirement of drive train components is large.

The HAWT is preferable in modern wind turbines, because rotor solidity is relatively low when the design tip speed ratio is provided, so its cost is also lower. Another reason is that the average height of the rotor swept area is higher above the ground [15], so the ability to capture wind power could be better. At present there are no commercially available VAWT, at the multi-megawatt scale, and so the focus of the work presented in this thesis is the horizontal axis wind turbine.

### **2.3.2 Rotor Power Control**

For maximum efficiency the wind turbine must operate within the designed speed and torque, and so the rotation speed of the wind turbine has to be controlled properly for power generation. Wind power increases as with wind speed cubed, and so in order to regulate power as wind speed increases, the wind turbine design must take into consideration the maximum wind speed. Actually, wind turbines produce power output under a range of wind speeds. If the wind speed exceeds the survival speed of the wind turbine, it would suffer damage. Therefore, power has to be limited when the wind speed exceeds the rated value of the design. To achieve this kind of power control, stall control and pitch control are mainly selected.

In a stall-regulated wind turbine, power generation decreases when the wind speed is higher than a certain value, which is due to the rotation speed or the aerodynamic torque decreases. Therefore, the rotor of the wind turbine has to be controlled by reducing the rotation speed during the period when wind speed exceeds the rated value. Generally, stall control is achieved with an induction generator which is connected directly to the electrical grid. The blades in stall-controlled wind turbines are designed aerodynamically to perform less efficiently when wind speed is very high. The power decrease is due to the aerodynamic blade design of the wind turbine in response to increasing wind speed. The advantage of this kind of wind turbine is that, because of the simple structure by which the blade is connected to the rest of the hub, the cost and maintenance of the stall-controlled wind turbine is lower. Beside this, a stall-controlled wind turbine also has a braking system to make sure that the wind turbine can survive in extreme wind speeds.

A pitch-controlled wind turbine can change the pitch angle of the wind turbine blades to reduce the torque generated in a fixed speed wind turbine and to decrease the speed in a variable speed

wind turbine when the wind speed is above the rated value. Generally, pitch control is selected for high wind speed only. When the wind speed is very high, the blades will vary the pitch angle to get less lift and more drag due to the increasing flow separation along the blade length [16]. In this way, either the rotation speed of the wind turbine and the torque produced can be reduced appropriately to keep the power output more or less constant. There are four main regions in the power curve of a pitch-regulated wind turbine. When the wind speed is very low, there is not enough torque to support the rotation of the turbine blade, which is the first region. When the wind speed then increases until the cut-in speed, the wind turbine will start to rotate and deliver useful power; during this period, the power output increases rapidly. In the third region, the wind speed reaches or even exceeds the rated output speed, and the output power will remain constant as rated power output due to the limitation. In the final region the turbine braking system causes the rotor to come to a standstill if the wind speed exceeds the survival speed of the wind turbine, so that damage can be avoided. As in the stall-controlled wind turbine, brakes are installed in the pitch control wind turbine to prevent damage under extreme wind conditions. The difference between pitch control and stall control can be easily seen. The stall-regulated wind turbine relies on the aerodynamic design of the turbine blades [16] to control the torque produced and the rotation speed when the wind speed is very high, so the power output cannot be kept constant. However, the pitch-regulated wind turbine has an active control system to vary the pitch angle of turbine blades, so that constant power output will be generated above the rated wind speed.

### **2.3.3 Rotor Position**

In the design of a horizontal axis wind turbine, the rotor could be either upwind or downwind of the nacelle, as shown in figure 2.1. Modern wind turbines adopt an upwind rotor design to avoid the wake produced by the tower contributing to fatigue damage to the blades and ripples in the electricity produced. Furthermore, noise is another drawback of downwind design when the rotor blades pass through the wake. Although downwind rotors of wind turbines generally have a free yaw system, which is simpler to implement than active yaw [15], free yaw is not in fact really necessary due to the risk of sudden changes in wind direction with too fast a yaw movement.



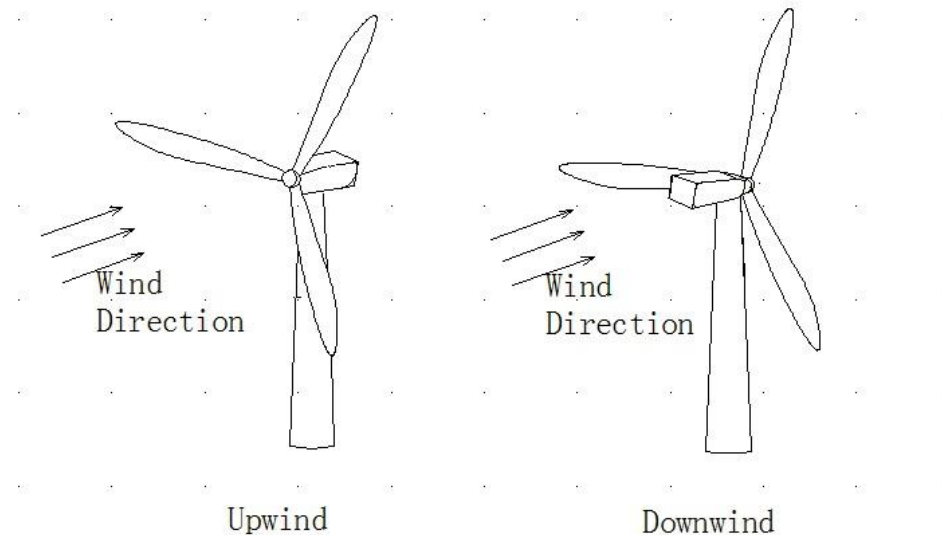


Figure 2.1 Wind Turbine Rotor Position.

### 2.3.4 Yaw Control

As the wind direction changes constantly, horizontal axis wind turbines have to be able to adjust their orientation. Usually a wind vane is installed on the back of the nacelle to detect wind direction. As mentioned above, the downwind rotor allows the turbine to have free yaw. Upwind wind turbines usually adopt active yaw control to maximise power output. In order to keep the turbine stationary in yaw, the system must be robust, including a yaw motor, gears, and a brake. Meanwhile, there is another method to control the power, where the rotor of the wind turbine could be turned away from the wind when wind speed is relative high in order to reduce the power.

### 2.3.5 Rotor Speed

In the 1990s, most turbine rotors were running at a constant speed, as determined by the electrical generator and the gearbox, if they were not coupled with power converter and so synchronous speed was fixed by grid frequency. More recently, due to advances in power converters, generator speed can be decoupled from grid frequency, allowing rotors to run at variable speeds. This allows rotor speed to match the maximum efficiency operation a point which could capture the maximum power with an optimum tip speed ratio at low wind speeds and to reduce the load in the drive train with a lower tip speed ratio under high wind speed conditions. On the other hand, the conventional constant speed rotors of wind turbines could be connected directly to the grid; however, complex and expensive power electronic equipment is required for systems with variable speed rotors.

### **2.3.6 Number of Blades**

The selection of blade number is mainly determined by the stress in the blade root, where there is a higher requirement for solidity made with an increasing number of blades. In modern wind turbines, the three-blade structure is often chosen, but in some turbines two or even one blade is adopted. Historically, a single-blade wind turbine was built, due to the low cost with only one blade involved; also, the wind turbines can operate with a high tip speed ratio. Beside this, wind turbines with more than three blades are rarely seen, because of the high cost of additional blades. But now the three-bladed wind turbine is relatively popular due to its advantage that the polar moment of inertia is constant with the yawing system, and it is independent of the azimuthal position of the rotor [15].

### **2.3.7 Generator Speed**

As discussed in section 2.5 below, different generator topologies operate at different operating speeds, which are mainly classified as one synchronous speed, multiple synchronous speeds, and variable speeds. For example, the squirrel cage induction generator and synchronous generator have their own synchronous speed. Moreover, if a generator has two sets of winding layouts with a different pole number, the generator can have two synchronous speeds, depending on which winding configuration is used [15]. The wound rotor induction generator, permanent magnet generator, and generator with fully rated output power conversion can achieve variable speed operation.

In fact, the selection of generator speed is one of the most important design factors for wind turbines, because it has significant effect on both the selection of power electronics and the drive train design. When the rotor speed is the same as the generator speed, a gearbox is not needed and the system is said to be direct drive. However, if a rotor speed and generator speed differ, a torque converter needs to be installed in the drive train system.

## **2.4 Modern Wind Turbine Design**

As mentioned in section 2.3.1, the performance and design requirements of horizontal axis wind turbine depend on the topologies chosen. The electrical generator as the core component has an immediate effect on the power delivered to the grid. The work presented in this thesis focuses on the wind turbine application of the electrical generator as a Doubly Fed Induction Generator.

### **2.4.1 Rotor**

The blades and hub have a significant effect on turbine performance and total cost. The blade converts the force of the wind into a shaft torque. The hub is used to connect the blades to the main shafts and the rest of the drive train, so it has to handle all the load that is delivered from the blades. Generally the hub is made of steel, either welded or cast [15].

The rotor of the modern wind turbine uses a three-blade structure with an upwind direction. Historically, the material used for turbine blades was wood/epoxy laminates. Today glass and carbon fibre reinforced plastics (GFRP and CFRP) can maximise power efficiency and exhibit high fracture toughness, fatigue resistance and thermal stability [17].

### **2.4.2 Drive Train**

The drive train system typically includes the rotor, a low-speed shaft, a high-speed shaft, a gearbox, and generator. All of these components are introduced below. Other components in the drive train system, such as the coupling, bearings, and brakes, are omitted as they are unaffected by changes to the electrical machine topology.

#### **2.4.2.1 Shafts**

The main shaft transmits torque and must carry the weight of the rotor. So the shaft to be strong is required and generally it is made of steel. The rotor, gearbox and generator are connected together through the main high-speed shaft and low-speed shaft. In the design, the shaft may be integrated into the gearbox or separated from it completely and connected by the couplings.

#### **2.4.2.2 Gearbox**

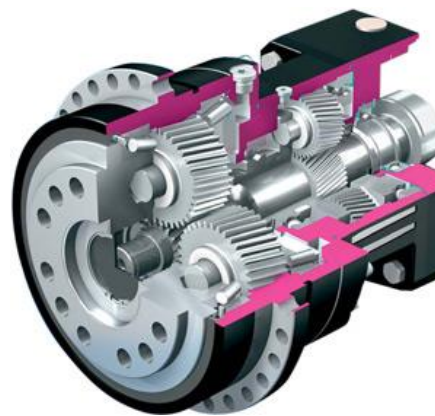
The gearbox appears in most wind turbine drive train systems. The function of the gearbox is to increase the rotational speed and reduce the torque of the rotor from the low-speed shaft at the rotor side to the high-speed shaft at the generator side. In fact, the gearbox is one of the heaviest components in a wind turbine, especially in large turbines [15]. The weight of the gearbox increases significantly with increasing power ratings of the turbine [15]. On the other hand, gearbox is generally manufactured by a different company, and the gearbox is designed based on a specific turbine model. So this means that the gearbox designer must understand both gearboxes and wind turbine design. However, the cost of gearboxes is quite expensive, and their maintenance is another problem because they are easily damaged and hard to replace. Therefore, the concept of direct-drive wind turbine is mentioned, but in the same wind condition the volume of direct-drive turbine generator is very large, so the weight of this kind of wind

turbine is quite heavy; another problem is the cost of direct-drive system is more expensive than the geared system.

There are two main types of gearbox which are selected in wind turbine applications, as shown in figure 2.2. These are the parallel-shaft gearbox and planetary gearbox. In the single-stage parallel-shaft gearbox, a low-speed shaft is connected to the rotor and a high-speed shaft is connected to the generator. Beside this, gears of the two different sizes are assembled on each shaft. Rotor rotation can thus speed up due to the ratio of rotational speed. On the other hand, the planetary gearbox is notably different from the parallel-shaft gearbox. Firstly, its shafts are coaxial, with a structure just like the planets. Moreover, the loads on each gear are lower due to the multiple pairs of gear teeth meshing at any time [15]. In this case, the advantages of the planetary gearbox are lighter weight and space savings.



(a)



(b)

Figure 2.2 Classifications of gearbox: (a) parallel-shaft gearbox [18], (b) planetary gearbox [19].

### 2.4.3 Nacelle

The nacelle provides protection for the wind turbine components which may be damaged by weather conditions, such as rain, snow or sunlight. Due to weight limitations, the nacelle material normally selected is fibreglass. As mentioned above, the gearbox is the most susceptible to damage component, so regular inspection and maintenance of the wind turbine is necessary. In small and medium-sized wind turbines, the nacelle is connected to the main frame, which can be opened directly. The larger wind turbines there are enough space to allow maintenance staff to enter the nacelle, in order to achieve the purposes of inspection and maintenance.

### 2.4.4 Yaw System

The principle of the yaw system is to adjust the direction of the nacelle in order to keep the wind turbine facing toward the wind so as to capture the maximum wind energy. Due to this characteristic, the yaw system is sometimes selected as one of the methods to regulate power output. The yaw systems generally installed on horizontal axis wind turbines may operate using active yaw control or free yaw control.

The structure of the yaw system usually includes yaw bearings, a yaw drive, and a yaw brake, as shown in figure 2.3. Among these, the yaw bearings are one of the most important components in the yaw system. These are the rotational parts between the tower and the nacelle of the wind turbine. So they have to have the ability to handle very high loads from the nacelle and rotor. Furthermore, the yaw drive has an electrical motor, a speed reduction gear, and a pinion gear [15]. Finally, the yaw brake is necessary to against yaw bearing rotation, and it stabilizes the turbine nacelle.

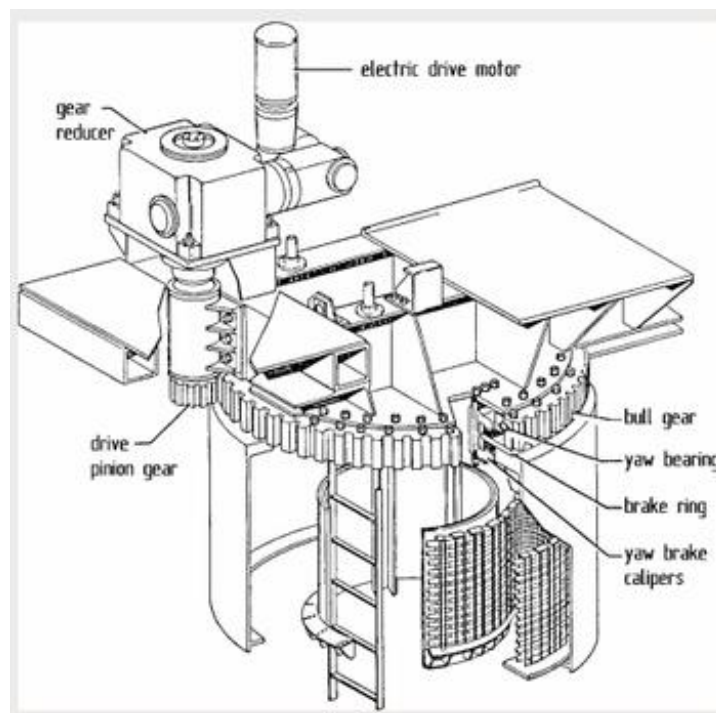


Figure 2.3 A cutaway of typical yaw drive with brake [20].

### 2.4.5 Tower

Towers are used to support the main structure of the wind turbine at a very high position to capture wind energy. Generally, tower height is higher than 24 metres, because lower wind speed and more turbulence exist closer to the ground [15]. It is well known that three different types of tower have been used for horizontal axis wind turbines: a tubular tower, truss tower,

or guyed tower, as shown in figure 2.4. However, the guyed tower is not widely accepted, and so is rarely seen in the market. In the past, the truss tower was commonly used in wind turbines. However, the tubular tower is used more frequently today.

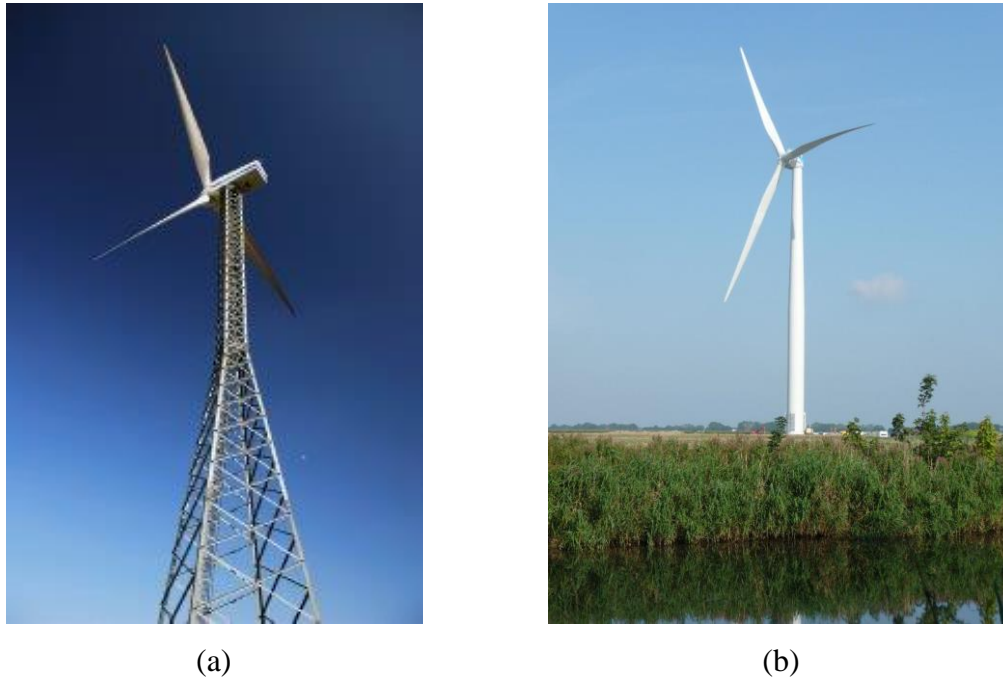


Figure 2.4 Towers for wind turbine: (a) truss tower [21], (b) tubular tower [22].

## 2.5 Survey of Generator Types for Wind Energy

The choice of generator type in wind turbines is based on cost, efficiency, and the ability to power generate under conditions of varying wind speed. Each type of wind turbine has its own power performance and their relative innovative researches on wind energy are not stopped today; meanwhile, power output varies with wind speed. In order to produce a power curve for a wind turbine it is necessary to predict the level of power generation.

Nowadays, induction and synchronous machines account for the biggest share of the market in generator for wind energy applications, due to their inherent advantages and disadvantages of characteristics and market background. Direct current generators were adopted when wind energy technology started to be developed, but in recent years these are rarely seen due to their own limitations. Beside this, switched reluctance machine is attempting to be applied in the wind energy application.

### 2.5.1 Direct Current Generator

Direct current (DC) generators were a historically important type of electrical machine for wind energy applications. In the past, they were commonly used in small-sized, battery charging

wind turbines [15]. The conventional DC generator has the same basic elements as the alternating current (AC) generator, so that when current pass through the field winding, an electric field is generated. Beside this, a commutator is installed on the rotor to rectify the power to DC. Meanwhile, brushes are needed to transmit the generated current. A characteristic of DC generator is that the magnetic field, armature voltage, and electrical torque increase with speed.

However, DC generators are rarely used today, due to their high costs and maintenance requirements. And they are to work in large power systems; the fire hazards of wiring must be solved. Detailed information concerning DC generators is given by Johnson [23].

## **2.5.2 Permanent Magnet Generator**

The Permanent Magnet Generator (PMG) is applied more frequently in both large and small wind turbine applications today. This is because PMGs have higher efficiency compared with other machine types when operating in the constant torque region, along with high torque density due to their simple and lightweight rotor structure without windings. Therefore, its good performance makes the PMG likely to be a great choice in the future with the development of rare-earth magnets. Meanwhile, a special design needs to be used in wind energy, which is the direct drive PMG. This is because the direct-drive wind energy system is not able to adopt the conventional high-speed electrical machines. This kind of generator has a sufficient number of poles to enable the generator rotor to turn at the same speed as the wind turbine rotor [15], and so the gearbox is no longer needed. Normally, direct drive generators on wind turbines are used with power electronic converters. Due to the large number of poles, the size of the generators is relatively large, so it is quite important for machine designers to minimise their size and weight with high torque density. Besides, Neodymium as the most important material in permanent magnet machines, and therefore cost effectiveness is another important issue which must be considered carefully.

### **2.5.2.1 Radial Flux Machine**

The radial flux machine is the conventional type of PMSG. It has many different topologies due to the flexibility of magnet location design in the rotor, where the magnets can either be on the surface of the rotor, or inserted or buried in the rotor [24]. So the structure of radial flux machines can be divided into three main topologies which are shown in figure 2.5, these are the surface permanent magnet, inset permanent magnet, and interior permanent magnet. Furthermore, the manufacturing technology of these machines is well established, which make their production costs lower than for the axial flux machine [25].

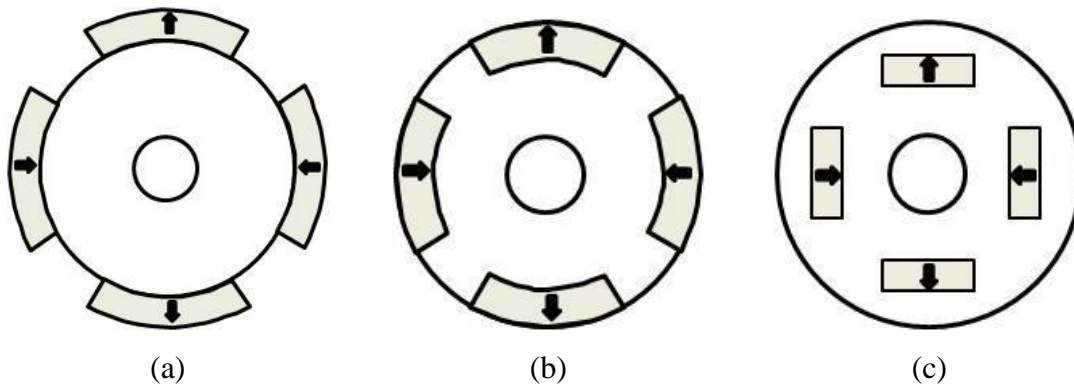


Figure 2.5 Radial flux machine topologies: (a) surface permanent magnet, (b) and (c) interior permanent magnet [26].

### 2.5.2.2 Axial Flux Machine

In axial flux machines, the air-gap flux flows in the axial direction. In recent years, various axial flux topologies have been developed. Generally, the length of an axial flux machine is shorter than the radial flux machine, and another advantage is its high torque density. So it is quite suitable for some applications where space is limited, especially in the axial direction. However, the disadvantage is that any change in machine length will cause a change in air-gap diameter. Hence, to increase the power rating a new design and a new geometry are needed [27].

### 2.5.2.3 Transverse Flux Machine

In the transverse flux machine, the flux path is a 3-dimensional structure as is shown in figure 2.6 [28]. Figure 1 shows that the flux path of a transversal flux machine. The flux travelled from the circumferentially magnetized magnets (1) to the “north” pole-piece (2) firstly, crossing the air gap into the tooth (3) by changing the flow direction, then passing through the core back (4) and returning via the opposing tooth (5), to arrive the “south” pole-piece (6) by crossing the air gap once again to achieve the magnet circuit, finally enclosing the coil (7) [28]. The use of these machines can be proposed in applications with low speed and high torque density requirements, like wind systems, free piston generators for hybrid vehicles and for propulsion [29]. The drawback of the transversal flux machine is its poor power factor due to the high leakage flux. On the other hand, the complex structure of the machine causes weak mechanical construction for rotation along with difficult manufacturing processes.



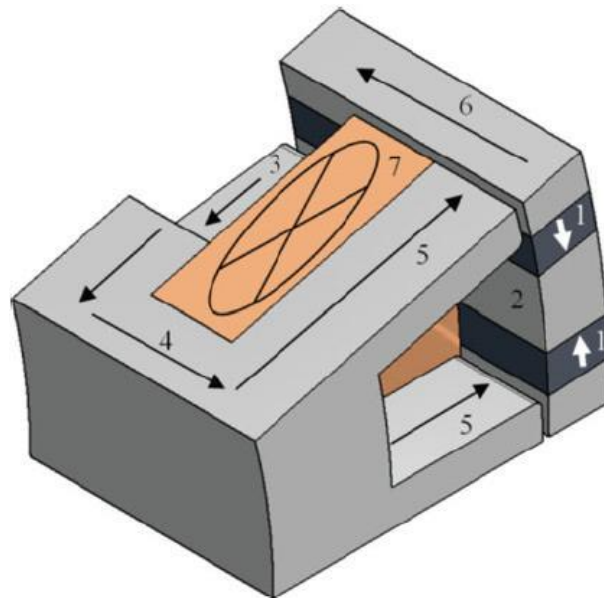


Figure 2.6 A cut-out section of a transversal flux machine [28].

### 2.5.3 Switched Reluctance Generator

The switched reluctance generator (SRG) is proposed as an effective option for machines in the future in wind energy applications [15]. No SRGs are currently installed in wind turbines, but research in this direction is underway. Hansen has conducted a series of extensive research on this type of generator for wind energy [30]. The SRG is suitable for any high-speed application due to its simple robust iron rotor without any windings or magnets. Meanwhile, the cost of an SRG is quite cheap, because there is only iron and copper in the structure; however, due to the need to have a small air-gap the manufacturing tolerances can be tight [26, 31]. Because of its simple construction, the SRG does not need much maintenance. At present, the development of the SRG is matched with using of power electronic converters. However, the advantages of the SRG are also drawbacks in certain respects. For example, the iron loss of its rotor can be significantly higher than with other machine technologies at high speed [32], and moreover these machine generate very loud acoustic noise and the torque ripple is very high due to its operational mode. At present no turbine manufactures build SRGs, although advances in power electronics and variations in permanent magnet costs may mean it attracts more interest in the future.

### 2.5.4 Induction Generator

Among all of the main types of generator used for wind energy applications, the induction generators are the most commonly used. They are asynchronous generators, and so they have the ability to operate at variable speeds, which is good for wind power generation due to the wide range of wind speeds involved. Furthermore, their simple rugged construction, relatively

low cost, and ease of manufacture are also primary reasons for them to be adopted in industrial applications in recent years. Generally, the induction machine is very efficient in the constant power region, where a low magnetization current is required, and also the constant power region can easily be extended to 4-5 times the base speed [26, 33]. However, the drawback of induction machines is a lower torque density, and their efficiency is lower when operating at lower speeds. Induction machines also require an external source of reactive power, along with an external constant frequency source to control the speed of rotation [15]:

$$n = \frac{60f}{p} \quad (2.1)$$

where  $f$  is the supply frequency in hertz and  $p$  is the number of magnetic pole pairs.

Slip is the percentage of the difference between the synchronous speed  $n_s$  and the rotor speed  $n_r$  at the same frequency:

$$s = \frac{n_s - n_r}{n_s} \quad (2.2)$$

For motor operation, the slip is positive; and for generator operation, the slip is negative. Typical values of slip at rated conditions are in the order of 2% [15].

Currently, there are two main types of induction generator which are used in wind turbines. These are the squirrel cage induction generator and the wound rotor induction generator respectively.

#### ***2.5.4.1 Squirrel Cage Induction Generator***

The squirrel cage induction generator (SCIG) has solid conducting bars embedded in the grooves and both side ends are shorted through end rings, so that the bar structure makes the rotor look like a squirrel cage, as shown in figure 2.7. The conducting bars are composed of stacks of electrical steel laminations, which are made by either copper or aluminium. The stator structure of this kind of generator is similar to that of a synchronous generator. The solid conducting bars usually adopt a slightly skewed design which can eliminate torque ripple and reduce noise.

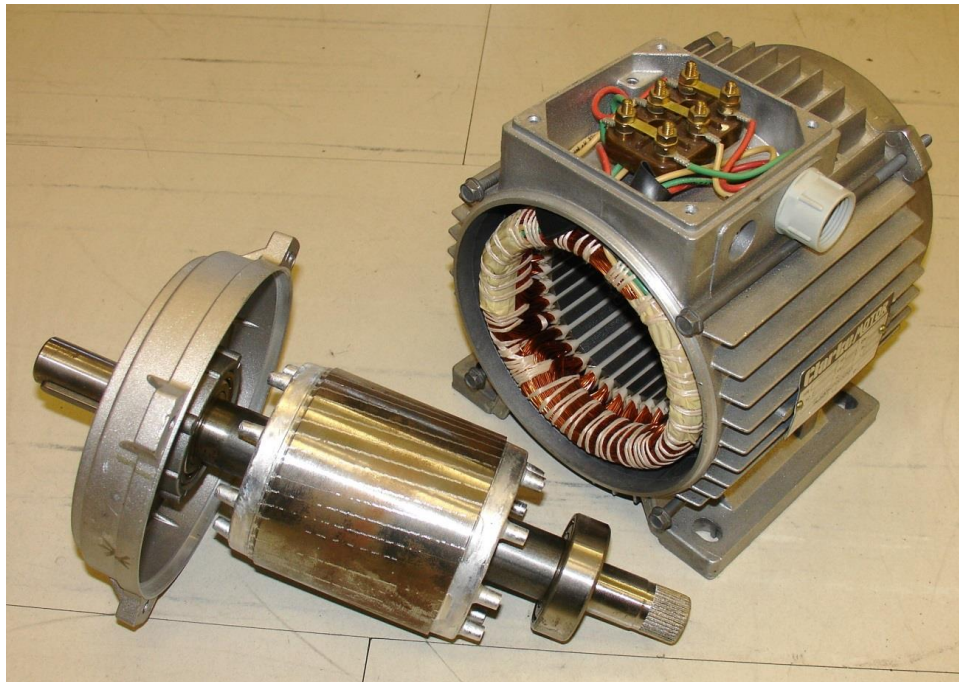


Figure 2.7 Squirrel cage induction machine [34].

In wind energy applications, the SCIG is coupled with the grid directly through a drive train system, which enables stall-regulated machines to operate at constant speed. Generally, these are defined as the singly fed induction generator (SFIG). The simple, rugged and cost effective construction of the SFIG has the interest of attracted wind turbine manufacturer. But the reactive power must be consumed in the SFIG because of its magnetizing reactance, and this is undesirable especially in large wind turbines and weak grids. Therefore, a compensating capacitor is generally adopted to compensate for the reactive power consumption, as shown in figure 2.8. So the SFIG is usually used in low power installations (<1MW per turbine) [30].

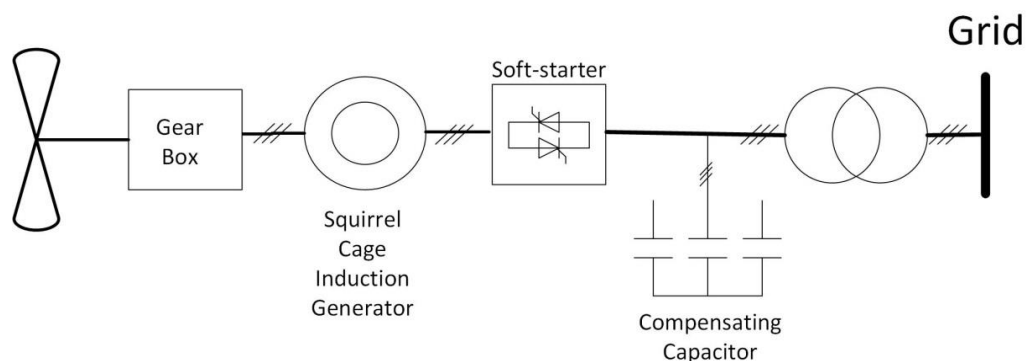


Figure 2.8 A single fed induction generator scheme.

The drawback of the SFIG is that the speed of the machine is uncontrollable and variable only in a very narrow range. Furthermore, generator operation is only available when the running

speed is higher than the synchronous speed. It is well known that wind speed is variable and irregular, so this type of wind turbine is not able to adjust to change speed, which causes low efficiency. The difficulties of gearbox maintenance and acoustical noise are additional problems with the SFIG.

An advanced version of the SCIG uses a back-to-back power converter to instead of the capacitor bank. So a gearbox is still used and the generator is connected to the grid through a back-to-back power converter, which is termed a fully rated converter SFIG as shown in figure 2.9. With this design, the ability to capture energy is better than with the conventional design, but the cost of a full-scale back-to-back power converter should be considered carefully due to its full power rating.

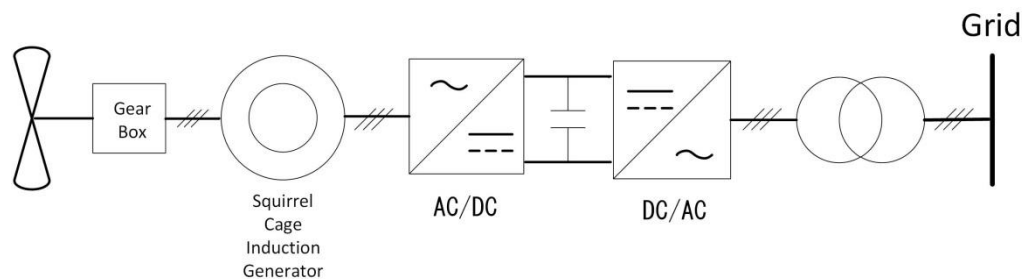


Figure 2.9 An advanced single fed induction generator scheme.

#### 2.5.4.2 Wound Rotor Induction Generator

The Wound Rotor Induction Generator (WRIG) has the same stator structure as the squirrel cage generator; but the rotor structure is quite different in that the insulated windings are placed in the rotor slots, and the rotor is brought out via slip rings and brushes. The rotor component is punched by stacked laminations and fitted directly onto the shaft. In wind turbine applications, the WRIG adopts variable resistance and a compensating capacitor in the system. Its stator is connected to the grid directly, while the rotor is connected to a variable resistance, as shown in figure 2.10. In that case, variable speed operation can be achieved by controlling the energy extracted from the WRIG rotor, but this power must be dissipated in the external resistor [35].

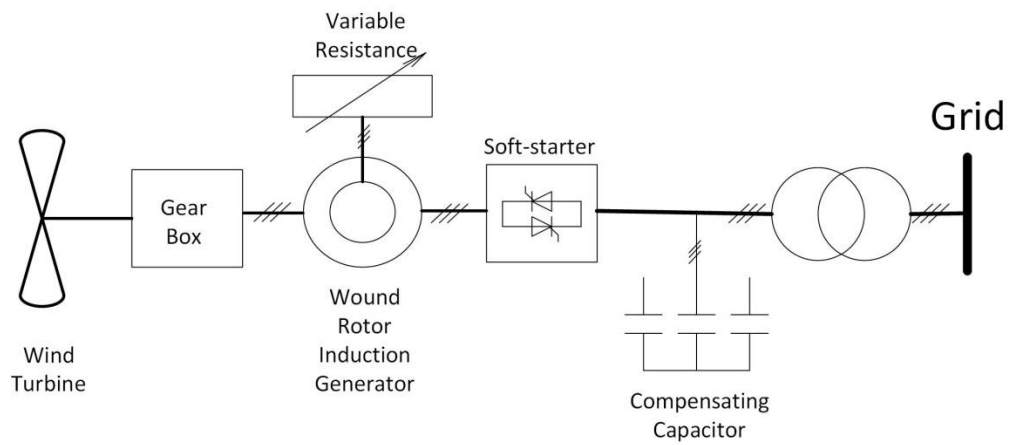


Figure 2.10 Schematic of a wound rotor induction generator

### 2.5.4.3 Doubly Fed Induction Generator

The Doubly Fed Induction Generator (DFIG) is constructed from a WRIG with multiphase windings which feed AC currents into both stator and rotor windings, where the former is connected to the grid directly. In the rotor, the winding is connected to a multiphase slip ring assembly with brushes which are used to transfer the power, in order to achieve the energy conversion with the grid typically via a bi-directional back-to-back voltage source converter. This part of the power in the rotor is the slip power, which could be either fed from the grid or delivered to the grid. The back-to-back converter consists of three components: a rotor side converter (RSC), DC link capacitor, and grid side converter (GSC). Inside the back-to-back converter, the rotor side converter is used to control the speed or torque of the DFIG and the machine power factor; the role of grid side converter is to minimise the DC link capacitor's voltage ripple [36]. Figure 2.11 presents the schematic of a DFIG wind turbine system. The DFIG has become popular in recent years, and now is one of the most popular wind turbines for industry applications, especially large-scale turbines.

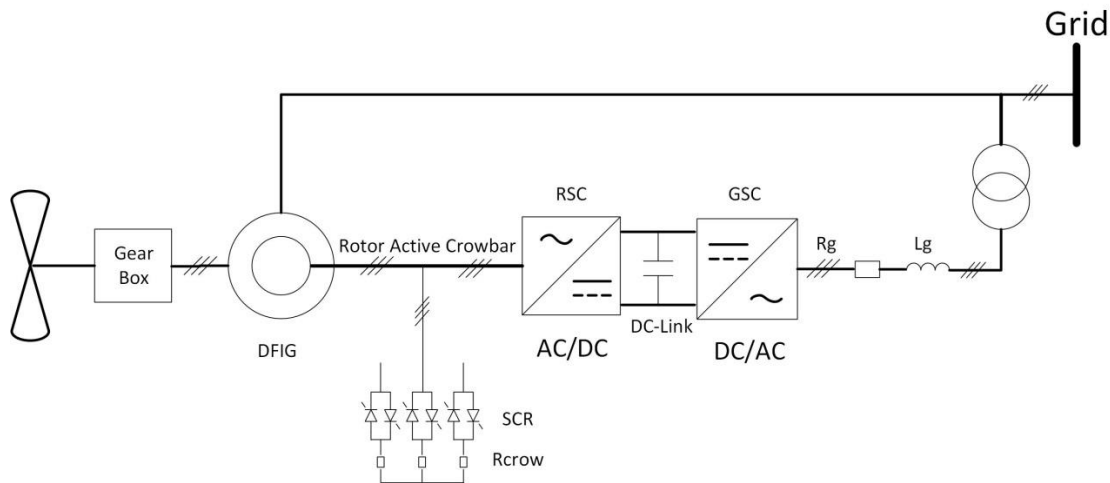


Figure 2.11 Schematic of a doubly fed induction generator wind turbine system

In variable speed wind turbines, as the name suggests, the rotation speed of the generators could vary with wind speed. However, the three phase asynchronous generator cannot be used in variable speed wind turbines, due to the fact that it is connected to the grid directly with a nearly fixed rotation speed, which is similar to the synchronous generators. With wind speed fluctuating naturally, both the torque and the power output of the wind turbines will change together accordingly, and if a sudden wind gust occurs, the torque of the generator increases significantly, as does the power output of the wind turbine. It is well known that significant fluctuations in power output from wind turbines can cause the destabilization of the grid.

DFIGs are used since they can produce constant voltage and frequency outputs by adjusting the amplitude and frequency of the AC current fed into the generator rotor winding [36] whatever the variation of either generator rotation speed or wind speed. Hence, the primary feature of the DFIG is that it is able to connect to the grid directly as an asynchronous generator, and to remain synchronized with the AC power grid in the meantime. When the grid fault or an abrupt voltage drop occurs, the ability of low voltage ride through could keep wind energy conversion system remain connected to the grid and provide ancillary services [37]. Moreover, according to the same method, regulation of the amount of reactive power exchanged between the generator and the power grid could control the power factor of the system. So the DFIG is able to operate close to a power factor of unity [36].

The DFIG's rotor is connected to the grid via a power electronic converter, which means that the rotor part actively participates in energy conversion with the power grid. So the converter in the DFIG only needs to carry part of the power output, which is typically 30% of the rated power output in industrial applications today. Accordingly, the size of the power electronic converter used in DFIG is approximately only 30% of those used in synchronous generators for

variable speed wind turbines. Consequently, the cost and losses of power electronic converters in DFIG are reduced to achieve the same variable speed control compared with synchronous generators.

To summarize, the doubly fed induction generator has the following advantages:

- Operates under conditions in which both rotor and wind speeds are variable while the amplitude and frequency of output voltage remain constant.
- Ability to control the power factor.
- The cost of the converter is lower than fully rated power converter, due to it carrying a power rating of about 30% of the system power output.
- Performs well with good efficiency.

However, the drawbacks of the DFIG with a gearbox are as follows [38]:

- Maintenance of slip rings and gearbox required.
- Limited capacity to supply reactive power.
- High torque occurs during fault conditions, which require the ability of low voltage ride through.
- Start-up current shall be limited via the voltage source converters [39].

To eliminate the maintenance requirements of the slip rings, a brushless DFIG has been developed. Here, a multiphase slip ring assembly is no longer needed, but there are still a lot of problems with the efficiency, cost, and size of the brushless DFIG. Despite this, the DFIG is still by far the main choice to be used in wind turbines to produce electricity.

### **2.5.5 Manufactured Wind turbines**

Today, wind energy is extensively accepted, and wind turbine manufacturers are also investing heavily in the development of wind energy technologies. Table 2.1 shows the generator technologies in some manufactured wind turbines:

Table 2.1 Generator technology used in manufactured wind turbines.

Model	Power Rating (MW)	Generator Type	Wind Turbine Model
Vestas V110 (Denmark)	2MW	DFIG	
Goldwind S48/750 (China)	750 kW	PMSG	
Enercon E53-800 (Germany)	800 kW	Annular generator	
Siemens SWT-2.3-101 (Germany)	2.3 MW	Asynchronous generator	
Nordex N100 (Germany)	2.5 MW	Doubly fed asynchronous generator	



## 2.6 Machine Failure Types

As wind energy is occupying an increasingly important position in renewable energy, the faults and failures of wind turbines attract considerable attention. In the literature, failures in all types of wind turbine generator cause significant downtime and impact on the whole electrical system [40, 41]. Undetected generator faults may have a catastrophic effect on the turbine drivetrain resulting in costly and lengthy repairs [42]. These can be generally classified as:

- Rotor winding faults
- Stator winding faults
- Bearing faults
- Cooling system faults

Among these types of failure, there has been a considerable increase in rotor and stator winding failures in wind turbine generators, especially when the installed capacity of the generator is less than 1 MW [43]. As a result, winding faults in the rotors and stators of wind turbines are major failures, and are extremely common in wind turbine systems [44]. They can be separated into open circuits and short circuits faults. An open circuit happened in the windings, if it cannot be detected in time, the machine will be damaged by overheating with continual unhealthy shaking. Besides this, if a short circuit in the windings is not detected in time, this can cause the catastrophic failure of the generator or even a breakdown of the entire wind turbine system, as shown in figure 2.12 for a rotor-winding fault.



Figure 2.12 Catastrophic failure of a wind turbine generator due to rotor winding fault [43].

Furthermore, winding faults in turbine generators may consist of turn-to-turn, coil-to-coil, phase-to-phase, phase-to-ground, and winding-to-iron faults [45, 46], as shown in figure 2.13.

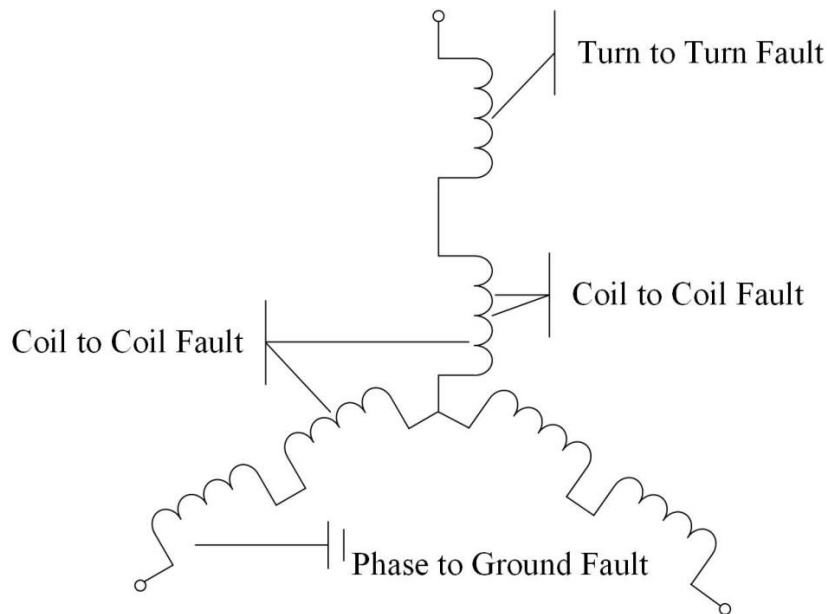


Figure 2.13 Winding failures in the rotor and stator of the turbine generators.

In fact, the turn-to-turn fault is often the initial problem [47-49], which leads to excessive heat in the winding. With heat accumulation during generator operation, the temperature increases considerably to create a hotspot inside the generator [50]. Finally, the overheating causes the insulation to deteriorate and break down. Similarly, phase-to-phase or phase-to-ground faults happen in the generator, which damage the entire wind turbine system and drop off the line [51]. More seriously, one damaged or shut down generator can cause a chain reaction, and lead to the entire wind farm dropping out of the power grid [52]. Hence, the winding faults of wind turbine generators are a serious problem which cannot be ignored.

In general, the conditional monitoring is used to detect the winding faults occurred in a wind turbine [53], a choice is then faced to either repair the faulted machine or replace it with a new one. In 1993, the number of new machines purchased and installed by the industry every year is nearly the same as the number of motors repaired and reemployed [54]. This is because machine repairs are thought to cause loss of efficiency loss and performance deterioration each time [55]. In the literature, some rewinding studies have concluded that the losses involved are less than 1% [56], or about 1% [57], 2% [58], or up to 6% [59] of efficiency. However, it has to be pointed out that the common practice today in the machine repair industry is to return to the original design as closely as possible. On the other hand, a lot of studies conclude not only small or negligible losses occur [60-62] in efficiency or even an improvement may occur [63],

so that the rewinding and repeated rewinding of an induction machine is another opportunity to optimise machine efficiency or improve machine performance [64]. As a result, a novel method is investigated in this thesis to design and re-design the windings of DFIGs for both stators and rotors.

## **2.7 Summary**

In this chapter, the topology of wind turbines and a survey of electrical generators have been extensively reviewed. Although wind energy has been exploited for a long time, there is still growing investment in research and development to improve system performance and tackle the challenges facing the industry today. The designs of different components of modern wind turbines are then introduced. Clearly, each machine technology has distinct advantages and depending on considerations of cost, eco-friendliness, and utilization, the selected machine technology can be optimised to best meet specifications. Electrical generators used in wind turbines by different manufacturers are discussed and the power ratings of wind turbines described. Different types of failure and relevant machine repair strategies are also reviewed.

This work focuses on the winding repair and re-design of an electrical generator in wind turbines when winding failures occur, because winding selection and design can directly affect machine performance. The generator selected for this work is the DFIG machine.

### **Chapter 3 Doubly Fed Induction Generator Analysis**

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This chapter explains the mechanical aspects and winding configuration of an off-the-shelf doubly fed induction generator for use as a wind turbine generator. The losses in different generator components are separated into conventional and additional losses, and these are investigated and discussed in detail. A numerical model of the equivalent circuit of the doubly fed induction generator is then presented, and an analysis is carried out of the electromagnetic losses according to the model and to validate its accuracy using a finite element package.

### 3.1 Background

The use of electrical generators in wind turbines requires the development of a variable speed generator while also achieving low cost and high efficiency. Among the several types of electrical generator used in wind turbines, the induction machine plays an important role in renewable energy systems. However, with the advances in wind turbine technology, stator and rotor winding failures are becoming a major issue. When winding failures occur, this is also an opportunity for machine winding re-design to take place. Hence, the purpose of this thesis is to accomplish the repair and re-design of the winding of an off-the-shelf DFIG machine when winding failure occurs.

During the process of rewinding, the damaged winding is first burned away, and then the new winding is placed into the slots of either the stator or rotor lamination. Therefore, the mechanical aspects of induction machines are presented firstly, and winding design is explained in order to analyse the rewinding work needed. In any machine design, some part of the energy during energy conversion will be dissipated as heat, reducing overall efficiency. It is important to understand the different types and effects of losses in a DFIG in order to improve the machine's performance and efficiency.

Later in this chapter, the finite element method for the magnetic modelling of electric machines is adopted in building a model of the DFIG based on the initial mechanical structural design, and is used to estimate the various losses in different components, which will help in achieving improvements in efficiency through winding design. The verification of the model's accuracy therefore must be rigorous; and a detail Finite Element Method (FEM) of this model is then performed to validate its accuracy in terms of the original design of the DFIG. Meanwhile, assessment of conductor and core loss is carried out using a FEM.

### 3.2 Mechanical Aspects of Induction Machine

As a key part of the power generating system, the DFIG is analysed and optimised in this thesis. Figure 3.1 shows a cutaway of a doubly fed induction generator. In this thesis, a three-phase four-pole 55 kW DFIG is used as the case study for the winding optimisation techniques developed later in Chapter 4, and the machine structure and slot dimensions are described in detail in this section before applying the optimisation routine.

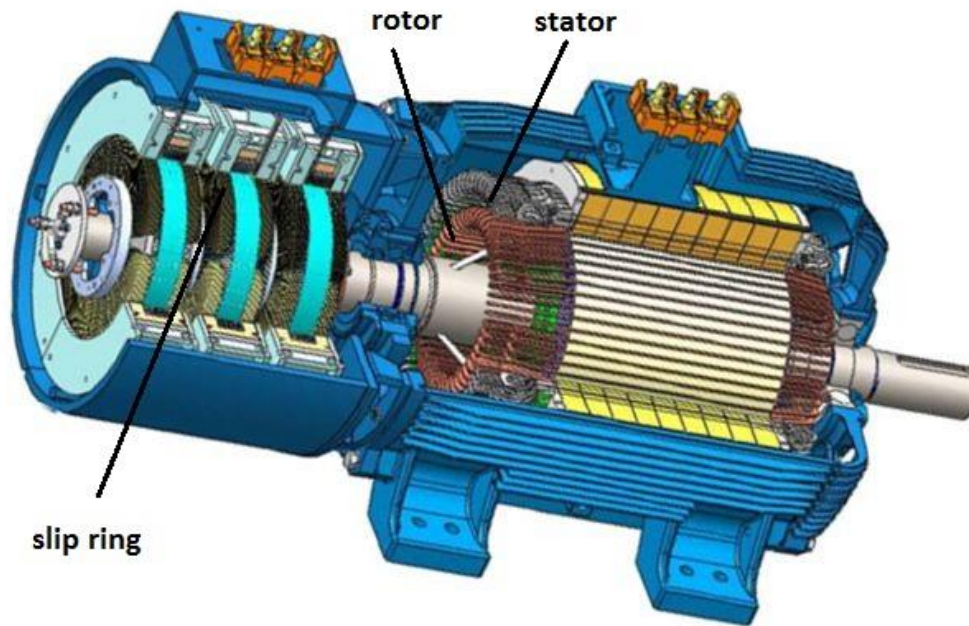


Figure 3.1 Cutaway of a wound rotor induction generator [65].

### 3.2.1 Stator Lamination

The stator is the stationary part of an induction machine which is used to carry the alternating flux. Figure 3.2 presents the size of the stator structure and slot, where the stator core is made of laminated steel to reduce eddy current. M600-50A silicon steel is selected for the construction, and the properties of this laminated material will not change after winding optimisation. These structures are made by stamping laminations 0.5 mm in thickness so as to build a stator core, which is then housed in a stator frame. There are a total of 60 slots on the periphery of the stator lamination where the three-phase stator windings will be placed.

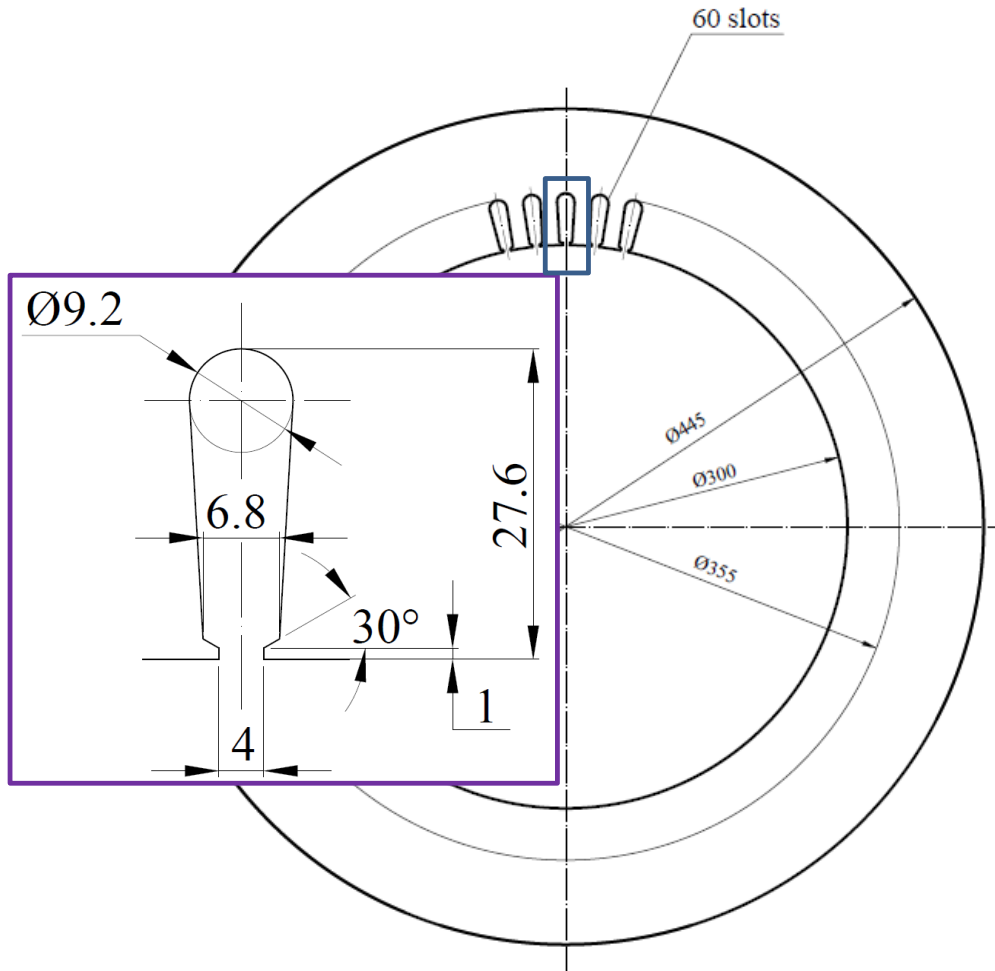


Figure 3.2 Structure of stator and stator slot.

The slot area and filling factor are very important to machine performance. The slot filling factor is equal to the ratio of the conductor area over the total slot area, and thus if a slot filling factor is 50% this signifies that half of the slot area is occupied by conductor material such as pure copper or aluminium whereas the other 50% is accounted for by conductor isolation, slot insulation, and the inevitable gaps between the conductors and the slot sides. Hence, selection of the insulation around conductors has an effect on the slot filling factor. According to the shape of the stator slot, its slot area is calculated at approximately 193 mm<sup>2</sup>. The detailed winding design and slot filling factor are introduced later in section 3.2.3.

### 3.2.2 Rotor Lamination

The rotor is wound for the same number of poles as the stator, but it has fewer slots and less turns per phase, with a larger Cross-Sectional Area (C.S.A) conductor, as shown in figure 3.3. The lamination material is the same as for the stator lamination, which is M600-50A silicon steel. The rotor consists of 48 slots and the three-phase rotor winding is placed inside these slots,

whilst the three end terminals are connected together to form a star connection. Furthermore, the rotor slot area is about  $223 \text{ mm}^2$ .

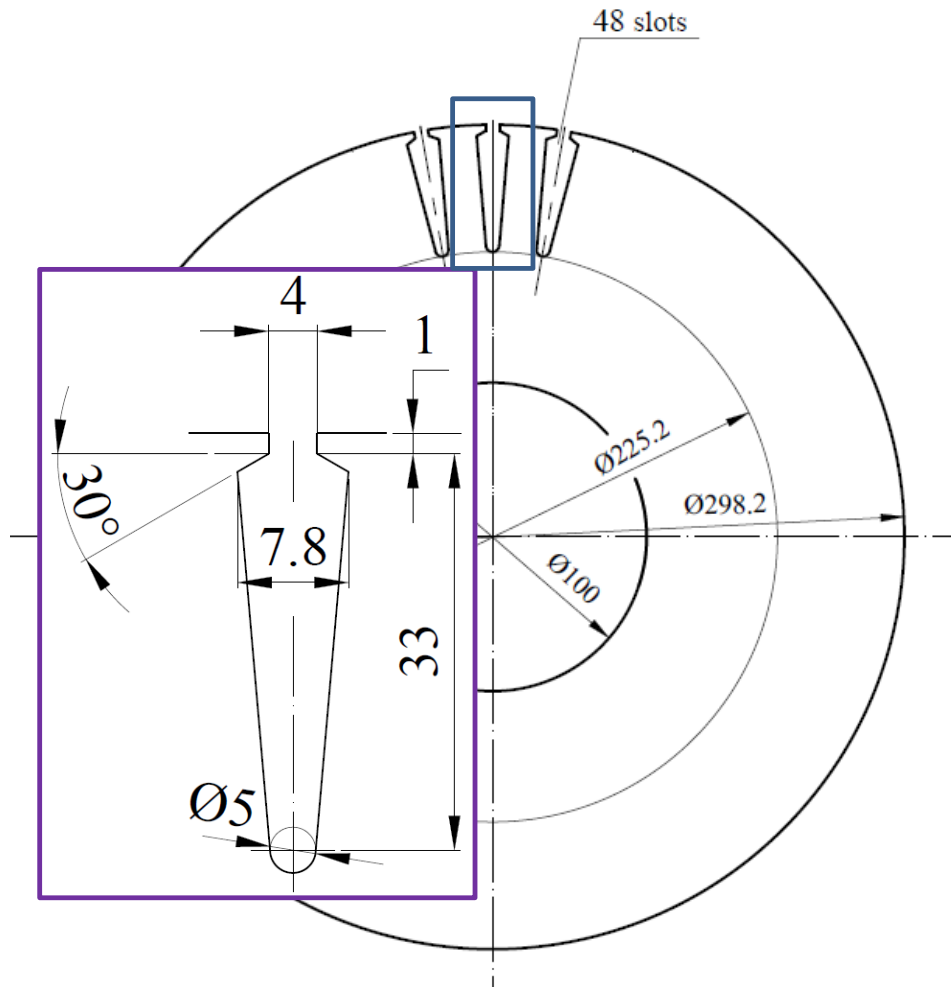


Figure 3.3 Structure of rotor and rotor slot.

### 3.2.3 Winding Design

The winding configuration influences the machine's weight, loss depletion, air-gap harmonic distortion and current density. There are two basic types of winding for any electrical machine: distributed and concentrated winding. Machines designed with distributed winding tend to exhibit less harmonics or noise in the waveform and less armature reaction compare to a concentrated winding. However the copper loss and weight of the machine are increased when distributed winding is used [66, 67]. Due to the structure of the DFIG, its winding is composed of stator and rotor winding. Three-phase winding can be further classified as single layer, double layer, and mixed winding. In the single layer winding, each end of a single coil occupies a full slot and there are four types of this kind of winding:



- concentrated winding
- lap winding
- chain winding
- cross winding

When the ends of two coils occupy a slot equally, this is called a double layer construction, which can be further separated into:

- double layer lap winding
- double layer wave winding

The double layer winding has a few advantages over a single layer winding. It has a neater arrangement because all of the coils are of the same size, and it is more flexible since coil span can be easily varied [68]. Although this design carries some inherent risk of isolation between the coils inside a slot, this is offset by other advantages such as better performance and saving in material. So the double layer winding is the most widely adopted class of windings, including in this thesis. Meanwhile, lap winding can provide more parallel paths, and so it is more suitable for low voltage and high current generators. For this reason, the double layer lap winding is selected in electrical generator applications.

The span of the coil of a phase is defined as the coil pitch, and when the span angle is 180 electrical degrees, this is a fully pitched coil which is equal to pole pitch. If the electrical angle between the starting and ending point of the coil is less than 180 degrees, the coil is short pitched. Therefore, the configuration of double layer lap windings can either be fully pitched or short pitched. Furthermore, the factor that describes the angle between two coils in one phase is termed distribution factor [24]. So the winding factor can be calculated based on these two factors as in equations 3.1-3.3; where  $k_p$  is the pitch factor,  $k_d$  is the distribution factor and  $k_w$  is the winding factor,  $m$  the harmonic number,  $\vartheta$  the pitch angle,  $\delta$  the distribution angle and  $n$  the number of coils per phase [24]:

$$k_{pm} = \cos\left(\frac{m\vartheta}{2}\right) \quad (3.1)$$

$$k_{dm} = \frac{\sin\left(\frac{mn\delta}{2}\right)}{n \sin\left(\frac{m\delta}{2}\right)} \quad (3.2)$$

$$k_{wm} = k_{pm} \times k_{dm} \quad (3.3)$$

In this design, short-pitching coil is selected rather than full-pitching coil, due to a series of advantages. For example, short pitched winding reduces the account of coil material requires and the harmonic content of flux density in the air-gap, especially the high order harmonics. It also produces a more sinusoidal current linkage distribution than a full-pitching coil. However, whatever winding configuration is selected, some basic rules have to be obeyed for a three-phase winding construction to generate a rotating magnetic field:

- the slot number of winding per phase must be the same
- the three-phase winding should be spaced at a 120° electrical angle to each other
- the three-phase winding adopts a 60° phase spread, which is divided into 6 balanced phase spreads in the magnetic field

In order to obtain better electrical performance, the coil pitch should be designed so to be as close as possible to the pole pitch, as shown in equation 3.4.

$$\tau_w \approx \tau_p = \frac{Z}{2p} \quad (3.4)$$

where  $\tau_w$  is coil pitch,  $\tau_p$  is pole pitch,  $Z$  is the number of slots, and  $p$  is the number of pole pairs.

Due to these reasons, the coil pitch of the stator and rotor were selected as 1-14 and 1-12 by the machine manufacturer in the original DFIG design. The stator has 60 slots and the rotor has 48 slots with a four-pole design, so that the pole pitches are 15 and 12 respectively. Each coil has 16 turns with a C.S.A of the stranded conductor of 4.29 mm<sup>2</sup> set for the stator winding, and 14 turns with a C.S.A of 6.95 mm<sup>2</sup> for the rotor winding. Therefore, the filling factor of the stator and rotor are about 35.52% and 37.35% respectively. The coil material is copper 100% IACS, with a resistivity of 1.7843×10<sup>-8</sup> Ωm at 20°C.

Because of the power rating of this DFIG, both the stator and rotor winding per phase are connected with two parallel paths to draw high current flows into the winding, as shown in figures 3.4 and 3.5. Figures 3.6 and 3.7 show details of the connection method with three-phase winding for the stator and rotor. A delta connection for the stator winding and a star connection for the rotor winding were selected. Table 3.1 and Table 3.2 present the winding configurations.

Table 3.1 Stator winding configuration

<b>Parameter</b>	<b>Value</b>
<b>Winding</b>	2 parallel sets of five adjacent coils per phase with 1-14 coil pitch, delta connection
<b>Physical Type of Winding</b>	Double layer
<b>Winding Material</b>	Copper 100% IACS
<b>Number of Turns</b>	16 per slot
<b>Cross-sectional Area</b>	4.29 mm <sup>2</sup>
<b>Phase Resistance</b>	0.1624 ohms
<b>Fill Factor</b>	35.52%

Table 3.2 Rotor winding configuration

<b>Parameter</b>	<b>Value</b>
<b>Winding</b>	2 parallel sets of four adjacent coils per phase with 1-12 coil pitch, star connection
<b>Physical Type of Winding</b>	Double layer
<b>Winding Material</b>	Copper 100% IACS
<b>Number of Turns</b>	12 per slot
<b>Cross-sectional Area</b>	6.95 mm <sup>2</sup>
<b>Phase Resistance</b>	0.056 ohms
<b>Fill Factor</b>	37.35%

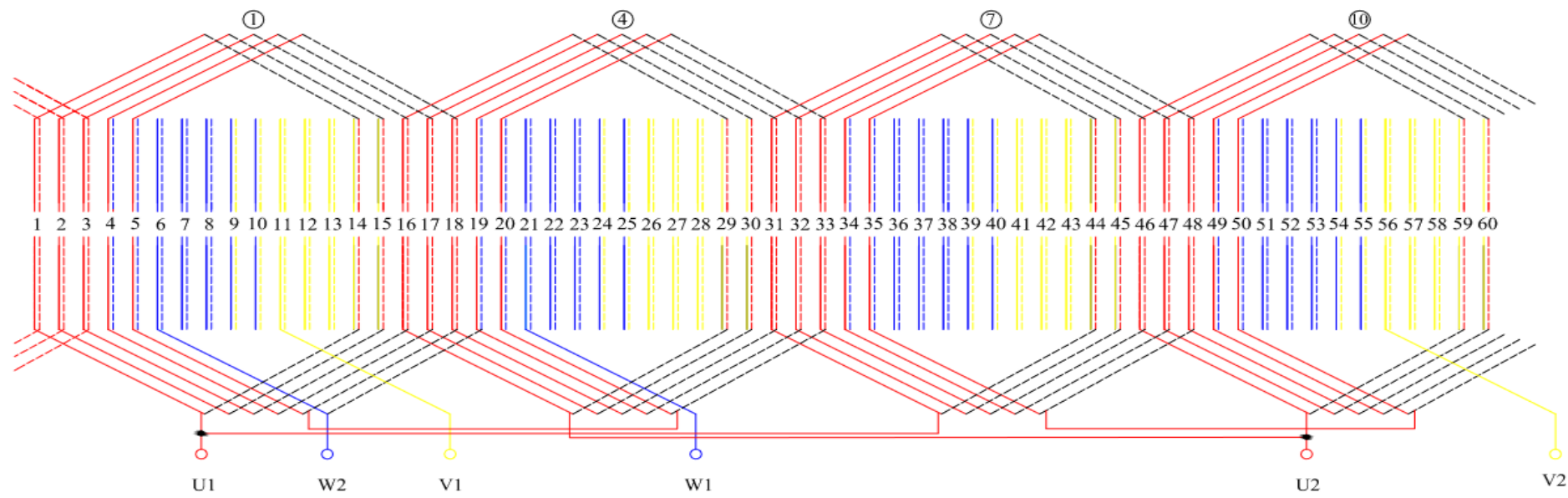


Figure 3.4 Three-phase 4-pole 60 slots double layer winding configuration with two parallel sets (coil pitch 1-14).

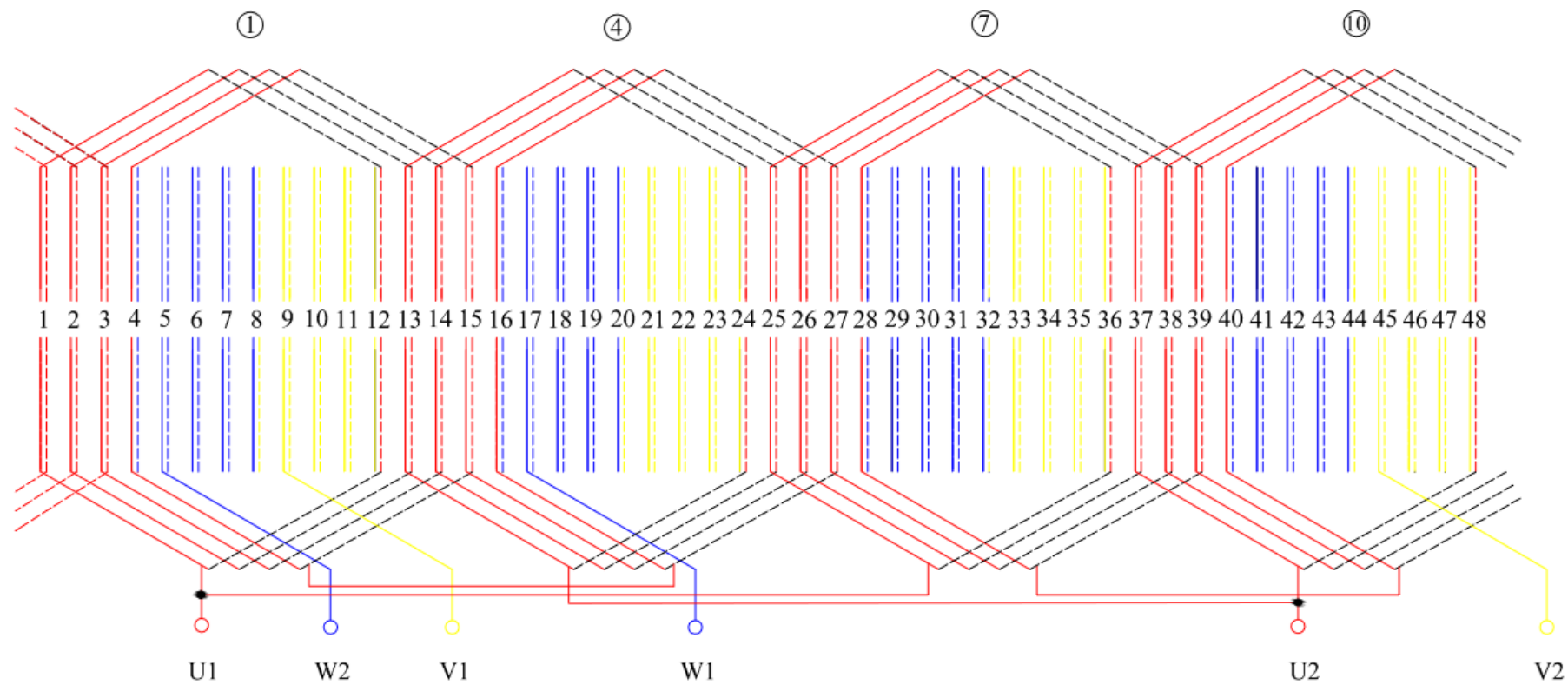


Figure 3.5 Three-phase 4-pole 48 slots double layer winding configuration with two parallel sets (coil pitch 1-12).

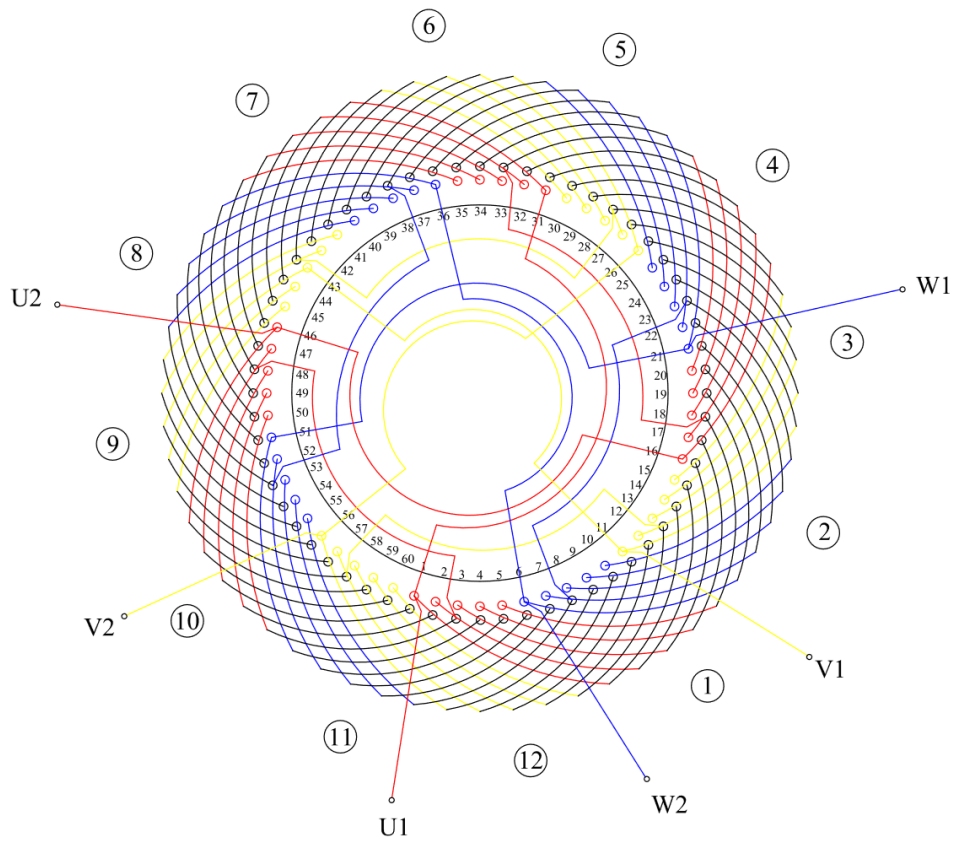


Figure 3.6 Three-phase winding connection in stator.

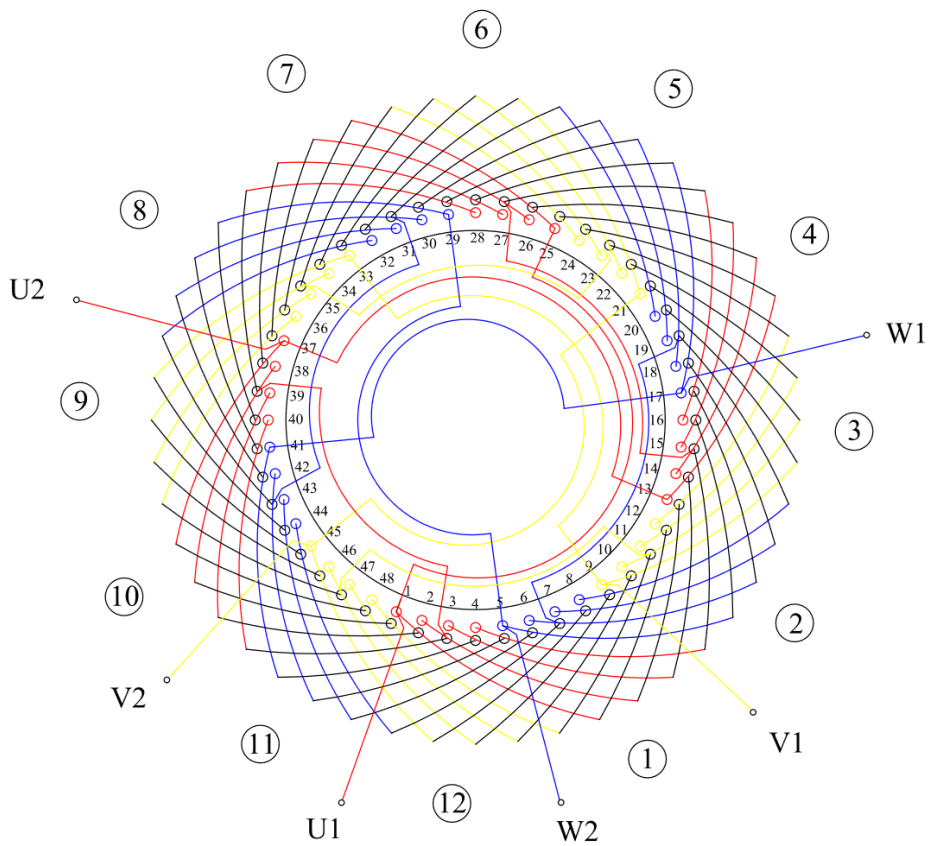


Figure 3.7 Three-phase winding connection in rotor.

### 3.3 Loss Components

Losses in induction machines occur in the windings and magnetic cores and include mechanical friction and windage losses. These losses can be broken down into five components:

- stator conductor loss
- rotor conductor loss
- core loss
- windage and friction losses
- stray load loss

Among these, only winding and core losses are electromagnetic losses. These are introduced next.

#### 3.3.1 Stator Conductor Loss

Stator conductor loss occurs in the conductors in the stator due to the current flowing through it and the inherent resistance. This loss can be defined as stator copper loss, which is determined by the conductor material, winding layout, operating temperature and current values.

For a three-phase induction machine, the stator conductor loss can be expressed as in equation 3.5:

$$P_s = 3I^2R_p \quad (3.5)$$

where  $I$  is the measured current per phase in amperes (A), and  $R_p$  is the per-phase DC resistance in Ohms.

#### 3.3.2 Rotor Conductor Loss

The principle of rotor conductor loss is nearly the same as that in the stator in a wound rotor induction machine in which the current flows through the rotor conductors. As such, it too is affected by conductor material, winding layout, operating temperature, and current. In addition, it is a non-linear function when frequency is applied to the rotor part of the induction machine. So the harmonics of the power supply will affect the rotor conductor loss [69]. In a Squirrel-Cage Induction Generator (SCIG), however, the rotor conductor loss is quite different due to the different rotor structure where there are rotor bars, instead of rotor windings. These are made either of copper or aluminium, but aluminium is generally selected to save the costs. The present research focuses on a wound rotor induction machine, and so the SCIG is not considered further.

For a three-phase wound rotor induction machine, the rotor conductor loss  $P_r$  can be determined by equations 3.6 and 3.7 as shown below:

$$\text{Motor:} \quad P_r = (P_{in} - P_s - P_c) \times s \quad (3.6)$$

$$\text{Generator:} \quad P_r = (P_{out} + P_s + P_c) \times s \quad (3.7)$$

where  $s$  is the slip per unit,  $P_c$  is the core loss,  $P_{in}$  is the measured input power,  $P_s$  is the stator conductor loss, and  $P_{out}$  is measured power output.

### 3.3.3 Core Loss

Core loss occurs in magnetic steel components of both the stator and rotor, and so they can be called iron loss or magnetic loss.

For conducting ferromagnetic materials, core loss is further divided into hysteresis loss and eddy current loss. Stators are usually composed of stacked laminations, to give a lower relative area, and so the total resistance increases. Eddy current loss can be minimised by laminating the core back, because the current will flow in a loop in the plane of the laminations only, not perpendicular to the plains. Hysteresis loss occurs due to reversals of the magnetic field. When the magnetic material is magnetized initially with an increasing magnetic field  $H$  and then demagnetized with an opposite magnetic field  $-H$ , the demagnetized path is different from the magnetized path in the magnetization curve [70], as shown in figure 3.8.

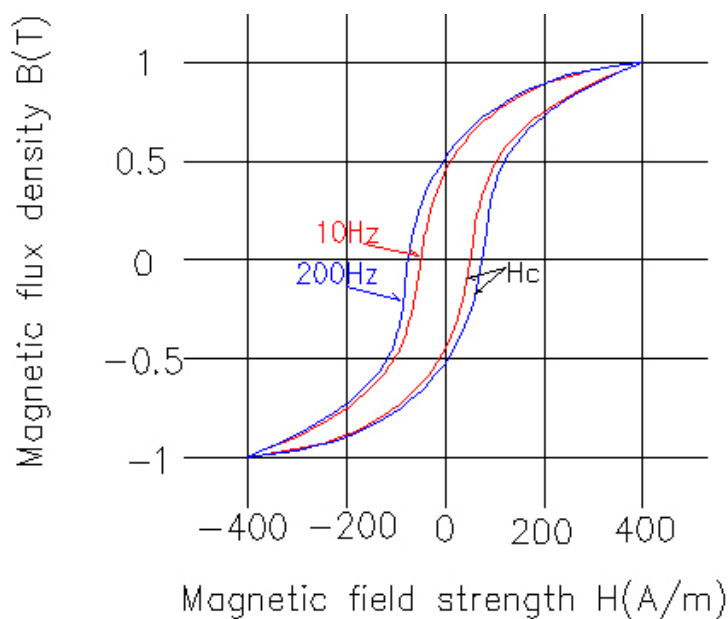


Figure 3.8 BH hysteresis curve of a ferromagnetic material at 10 Hz (red) and 200 Hz (blue) [70].



Hysteresis loss is related to the area bound by these curves and is determined by the hysteresis properties of the material. If high grade silicon steel is used, the hysteresis loss is low. Consequently, any change in current or load conditions will cause the core loss to change.

The stator core loss is usually larger than the rotor core loss. This is because the stator frequency is equal to the power supply frequency, but the frequency of the rotor equals the supply frequency multiplied by the slip, and so is always less than stator frequency. The rotor core loss is often neglected in running conditions.

It is not easy to predict or measure core loss accurately and directly. To estimate the iron loss, “loss correction factors” or “build factors” are generally applied to FEM predictions. However, these correction factors are empirical parameters, which are usually 1.6-2 or even higher, which means that errors between simulations and corresponding measurements are often quite large [71]. Alternatively, an indirect method using power measurement and loss separation can be selected. But detailed information from the analytical model is required, such as concerning geometry, saturation, and even the harmonics. Nowadays, the FEM is widely accepted to provide the relevant calculations for the in-depth analysis of iron losses from electro-magnetic simulations. For example, the software *Infolytica Magnet* is based on Epstein Frame loss measurements, but uses the Steinmetz equation augmented by an eddy current term to separate the total iron losses into two components: hysteresis with anomalous losses and eddy current losses [72]. Unfortunately, error between the results of FE analysis and actual loss measurements still exist, and these sometimes reach 20% [73].

### 3.3.4 Windage and Friction Losses

Windage and friction losses comprise losses due to bearing friction, windage, the cooling fan load, and any other source of friction or air movement in the machine. Bearing friction loss depends on the shaft speed, bear type, the properties of the lubricant and the load on the bearing [74], as expressed by SKF [75] in equation 3.8:

$$P_{\rho,bearing} = 0.5\omega\mu_f FD_{bearing} \quad (3.8)$$

where  $\omega$  is the angular velocity of the shaft supported by a bearing,  $\mu_f$  is the friction coefficient (typically 0.001-0.005),  $F$  is the bearing load and  $D_{bearing}$  is the inner diameter of the bearing.

Windage loss occurs in the air-gap due to the friction between the surfaces of the machine’s rotating components and air. Extensive experimental investigations into windage loss in

electrical machines were carried out by Vrancik in 1968 [76]. The windage loss is also affected by the surface shape and material, as well as the air temperature as shown in figure 3.9.

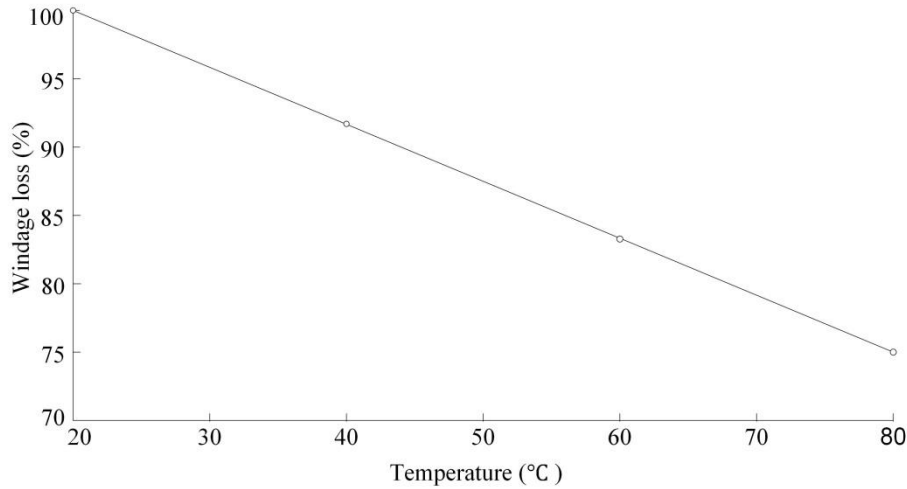


Figure 3.9 Effect of temperature on windage loss [77].

Beside this, Saari [78] proposed a method to estimate the windage loss in 1995 using equation 3.9:

$$P_{\rho w1} = \frac{1}{32} k_r C_M \pi \rho_c \omega^3 D_r^4 L_r \quad (3.9)$$

where  $k_r$  is a roughness coefficient,  $C_M$  is the torque coefficient,  $\rho_c$  is the density of the coolant,  $\omega$  is the angular velocity,  $D_r$  is the rotor diameter and  $L_r$  is the rotor length.

Also, the friction loss at the end surfaces of the rotor is expressed [78] as equation 3.10:

$$P_{\rho w2} = \frac{1}{64} C_M \rho_c \omega^3 (D_r^5 - D_{ri}^5) \quad (3.10)$$

where  $D_r$  is the outer diameter of the rotor, and  $D_{ri}$  is the shaft diameter. Therefore, the windage losses are the sum of equations 3.9 and 3.10.

$$P_{\rho w} = P_{\rho w1} + P_{\rho w2} \quad (3.11)$$

The windage and friction losses are often appreciable in large and high speed motors with a cooling fan. These losses vary with rotating speed whereas if the speed remains constant in a three-phase induction motor, so the windage and friction losses remain almost constant. These kinds of losses are generally determined either by using empirical formula or by Computational Fluid Dynamics (CFD) simulations.

### 3.3.5 Stray Load Loss

Conductor losses, core loss, windage and friction loss can be identified by experimental test of induction machine, and are collectively called “conventional losses”. Meanwhile the Stray Load Loss (SLL) is an additional loss caused by the non-ideal nature of a machine in practice [79], and it is not a negligible component of the power and energetic balance in the induction machine [80]. According to the relevant research for USA and European standards, this part of the losses is a key part of the correct evaluation of an induction machine’s efficiency [81, 82]. The SLL accounts for only a small fraction of the total power [79], but any error in the measurement or calculation of other conventional losses will make the SLL quite difficult to calculate analytically. Recognising the source of the SLL is important. It due to the pulsations of flux in the teeth of the stator and rotor, and in air-gaps [83]. Beside this, a series of harmonics in the conductors and magnetic materials are other causes of the SLL due to leakage flux, especially in high frequency components in the rotor bars and teeth resulting from stator and rotor slotting [84]. The currents in the stator windings produce a sinusoidal main field for the rotor windings during operation, which is superimposed on a series of harmonics. These are generally separated precisely as follows [85]:

- MMF harmonics have a direct relationship with the style, connection, and geometry of the stator winding. The frequency and order of the harmonics are determined by the number of stator slots and the pitch of the winding.
- Permeance harmonics are generated entirely due to the number of stator and rotor slots.
- Saturation harmonics occur when the core laminations operate at levels of flux density that are increasingly in the non-linear saturation zone.

So the harmonic losses can be analysed theoretically using the equivalent circuit method, and superposition can be used to find the total harmonic load losses if saturation in the magnetic circuit is neglected [69]. The individual harmonic losses can be separated from the total harmonic losses, and the corresponding equivalent circuit is shown in figure 3.10, where  $R$  is the resistance and  $X$  is the impedance.

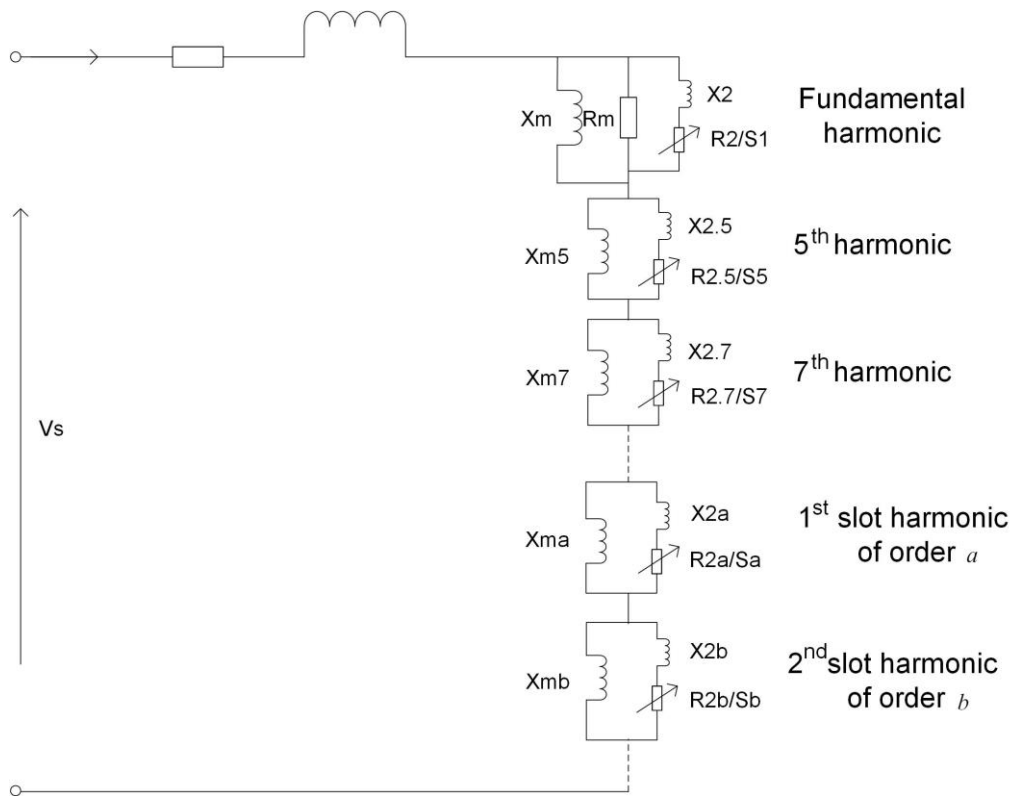


Figure 3.10 Complete equivalent circuit of induction motor [86].

The space harmonic is a result of non-sinusoidal distribution of the coils in the machine and slotting, which has effects on torque, speed, and current; in the meanwhile, the rotor slot sweep through the stator slot when the machine is running, the slot harmonic is generated by the flux changing inside the slots. As a result, it can be clearly seen that winding layout, numbers of slots in the stator and rotor, shape of the stator and rotor, and irregularities and mechanical imperfections in the air-gap are the main factors which affect the SLL. Most of the SLL occurs in the stator and rotor teeth at the air-gap surface [87].

Different testing standards have contrasting criteria for the accounting percentage of SLL in induction machines. The IEC 34-2 [88] assumes that the SLL is 0.5% of the rated input power to the motor. The NEMA MG1 [89] claims that SLL accounts for about 1.2% of the total losses in induction machines when the rated power is less than 1.8 MW; if higher than this value the rate will decrease to 0.9%. Furthermore, the IEC 61972 [82] gives a figure which illustrates the percentage of SLL versus rated output power, as shown in figure 3.11. Finally, the IEEE 112 standard [81] gives details of the varying proportions of SLL with different motor ratings, as shown in Table 3.3.

Table 3.3 Assigned ratio of stray load loss to rated output power in IEEE 112-B

Motor ratings (kW)	Stray load loss (%)
1-95	1.8
96-370	1.5
371-1799	1.2
$\geq 1800$	0.9

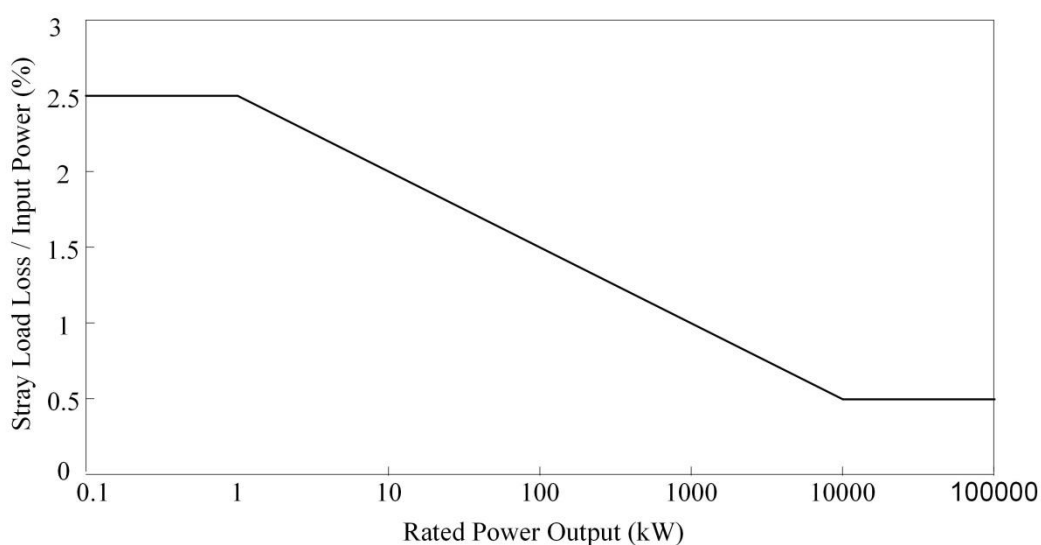


Figure 3.11 Assigned allowance for stray load loss [82].

Researchers have attempted to measure SLL accurately for many decades. For example, the SLL was considered to calculate using equivalent circuit method [80]. The evaluation of SLL can also be carried out using magnetic field analysis with the FEM [87, 90-92]. Beside this, an alternative calorimetric technique has been developed to measure the SLL precisely [64, 93, 94]. Furthermore, direct SLL measurement is often adopted, which includes two independent tests when the rotor is removed and in reverse rotation [95, 96]. Finally, the input-output method with loss segregation by IEEE 112-B standard is used globally to remove the conventional losses from total losses, and the measurement of SLL can thus be achieved by loss segregation. In this case, the highly accurate measurement of conventional losses is conducted first.

Any mechanical imperfection, turbulence or interference from the power supply or load, or other non-ideal situations, will cause errors in SLL measurement. Sometimes, similar induction

machines may exhibit huge differences in the values of SLL. Even in the same induction machine, the SLL could differ in varying experimental environments.

### 3.4 Finite Element Analysis

Now that the dimensions and previous descriptions of the DFIG have been introduced, a detailed, high-fidelity model therefore requires a finite element analysis to provide an estimation of machine losses and efficiency.

#### 3.4.1 Details of the Model

The flux analysis of the DFIG is assumed to be two-dimensional, and modelling can hence be undertaken using a two-dimensional FEM program. The commercial finite element software used here is *Infolytica Magnet*. As described in section 3.2, a three-phase, four-pole DFIG was simulated using this software, and due to the complex winding configuration of the machine a full model is built. The 2D basic model with mesh is shown in Figure 3.12.

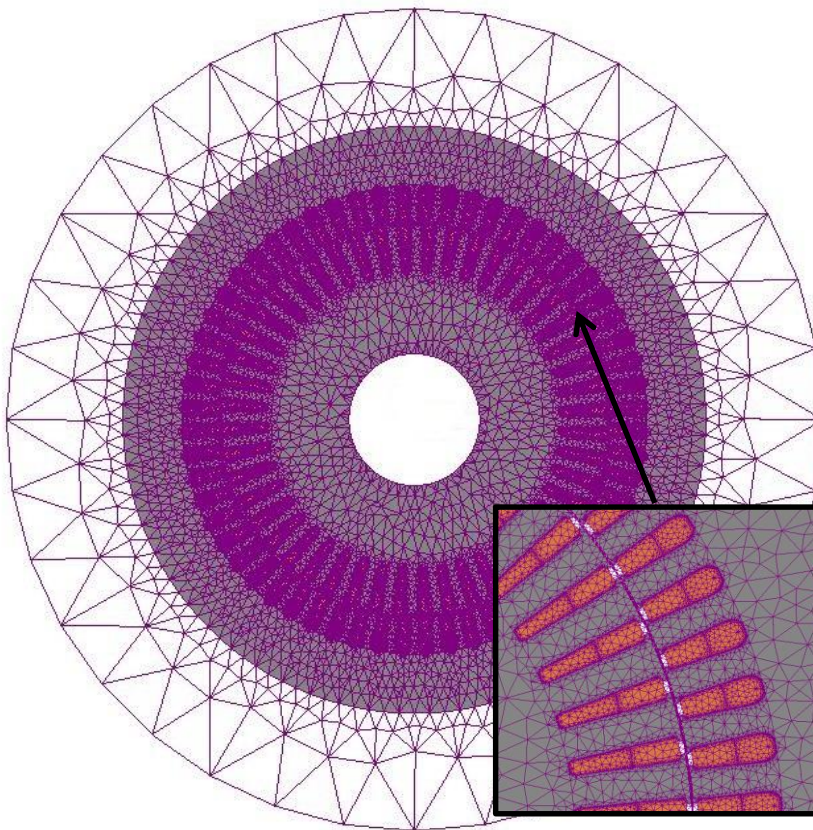


Figure 3.12 FEM mesh of DFIG.

The size of the mesh elements of the model varies, and mesh size is one of the most important aspects of a finite element solution. Due to the unit of measurement of the air-gap and conductors, the densest mesh sizes have to be used. In order to ensure the accuracy of simulation,

the model boundary air was split into four parts: the air enclosures surrounding the stator and rotor, and the static and rotating air-gaps that complete the two sections of the model's air-gap. The mesh of the static and rotating air-gap has a maximum element size of 3.5 mm to accurately allow the description of the rate of change of the magnetic field in the air-gap. Besides this, the smaller mesh size of 1.6 mm was chosen around the stator and rotor conductors. Meanwhile, the model is surrounded by a background region of air in order to reduce the influence of artificial boundary conditions. This is necessary in running the finite element analysis [97]. The electromagnetic traveling field is generated by the stator currents which exist in the air-gap and crosses the rotor teeth to embrace the rotor windings. Hence, the pattern of the electromagnetic field is equivalent and symmetrical as shown in figure 3.13.

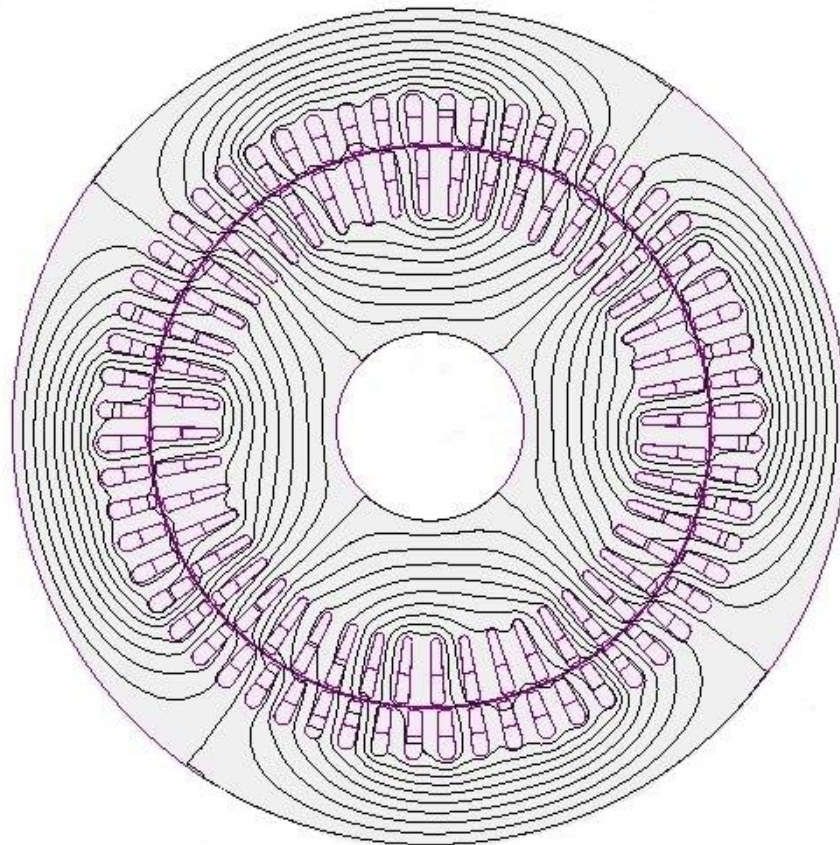


Figure 3.13 Contour flux plot of DFIG.

To achieve the purpose of the winding analysis, the prediction of machine behaviour using finite element analysis requires the model to be run with various sizes of coil. All of the FE model solutions applied to obtain the desired results were transient 2D with motion.

### 3.4.2 Equivalent Circuit of the DFIG

To analyse the DFIG's performance, the numerical model of the per-phase equivalent circuit is used with the inclusion of the magnetizing losses, as shown in Fig. 3.14. The biggest difference between the DFIG and conventional induction machines is in the rotor side circuit, where a voltage source is added to inject voltage. Applying Kirchoff's voltage law to the circuit [98] gives:

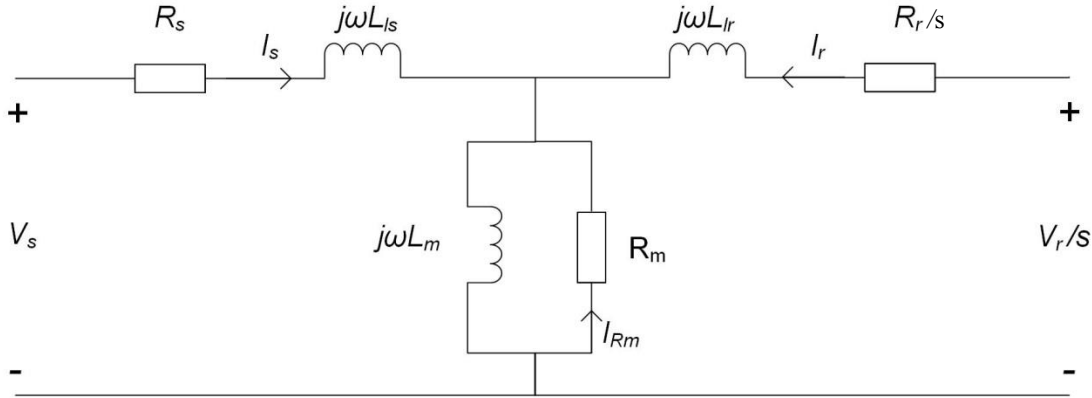


Figure 3.14 Equivalent circuit of the DFIG.

$$V_s = R_s I_s + j\omega L_{ls} I_s + j\omega L_m (I_s + I_r + I_m) \quad (3.12)$$

$$\frac{V_r}{s} = \frac{R_r}{s} I_r + j\omega L_{lr} I_r + j\omega L_m (I_s + I_r + I_m) \quad (3.13)$$

$$0 = R_m I_m + j\omega L_m (I_s + I_r + I_m) \quad (3.14)$$

where  $V_s$  is the stator voltage,  $R_s$  is stator resistance,  $V_r$  is rotor voltage,  $R_r$  is rotor resistance,  $I_s$  is stator current,  $I_r$  is rotor current,  $R_m$  is magnetizing resistance,  $L_{ls}$  is stator leakage inductance,  $L_{lr}$  is rotor leakage inductance,  $I_m$  is magnetizing resistance current, and  $L_m$  is the magnetizing inductance.

The air-gap flux, stator flux and rotor flux are defined as in equations 3.15-3.17:

$$\psi_m = L_m (I_s + I_r + I_m) \quad (3.15)$$

$$\psi_s = L_{ls} I_s + L_m (I_s + I_r + I_m) = L_{ls} I_s + \psi_m \quad (3.16)$$

$$\psi_r = L_{lr} I_r + L_m (I_s + I_r + I_m) = L_{lr} I_r + \psi_m \quad (3.17)$$



Therefore, the equations describing the equivalent circuit can be reformulated as follows:

$$V_s = R_s I_s + j\omega\psi_s \quad (3.18)$$

$$\frac{V_r}{s} = \frac{R_r}{s} I_r + j\omega\psi_r \quad (3.19)$$

$$0 = R_m I_m + j\omega\psi_m \quad (3.20)$$

The resistive losses of the induction generator are

$$P_{loss} = 3\left(R_s |I_s|^2 + R_r |I_r|^2 + R_m |I_m|^2\right) \quad (3.21)$$

And it is then possible to express the electro-mechanical torque,  $T_e$  as in equation 3.22 [98]:

$$T_e = 3pI_m \left[ \psi_m I_r^* \right] = 3pI_m \left[ \psi_r I_r^* \right] \quad (3.22)$$

### 3.4.3 Magnetic Field

The software solves the FEM model based on electromagnetic field analysis; it therefore does not take account of mechanical windage and friction loss or SLL. Electromechanical energy process energy from mechanical to electrical energy and vice versa, within a magnetic field. Magnetic fields created by current, equation 3.23 solved relate the magnetic field strength to the current density in the conductor [97]:

$$\vec{\mathbf{J}} = \nabla \vec{\mathbf{H}} \quad (3.23)$$

where  $\vec{\mathbf{J}}$  is the current density and  $\vec{\mathbf{H}}$  is the magnetic field strength.

A magnetic field in a two dimensional problem is composed of tangential and normal components, which can be expressed as in equation 3.24:

$$\vec{\mathbf{H}} = H_n \vec{\mathbf{a}}_n + H_t \vec{\mathbf{a}}_t \quad (3.24)$$

In unsaturated material such as air, the relationship between flux density and field intensity can be described as in equations 3.25 and 3.26. In order to facilitate highly precise modelling, the non-linearity of the steel material M600-50A is provided, as shown in figure 3.15.

$$\vec{\mathbf{B}} = \mu \vec{\mathbf{H}} \quad (3.25)$$

$$\mu = \mu_0 \mu_r \quad (3.26)$$

where  $\mu_r$  is the relative permeability of the material and  $\mu_0$  is the permeability of the air which is equal to  $4\pi \times 10^{-7}$  [1/H]. Similar to field intensity, flux density contains normal and tangential components, and hence it can be expressed as in equation 3.27.

$$\vec{\mathbf{B}} = B_n \vec{a}_n + B_t \vec{a}_t \quad (3.27)$$

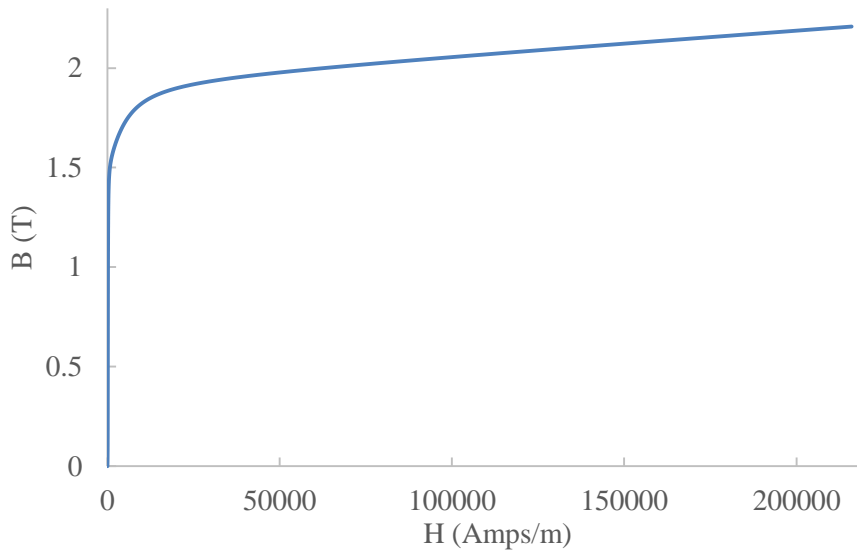


Figure 3.15 B-H data for FEM.

Figure 3.16 reveals that the FEM predicted that the peak value of  $B_{\text{normal}}$  in the air-gap would be at about 0.76T and the value of  $B_{\text{tangential}}$  about 0.23T.

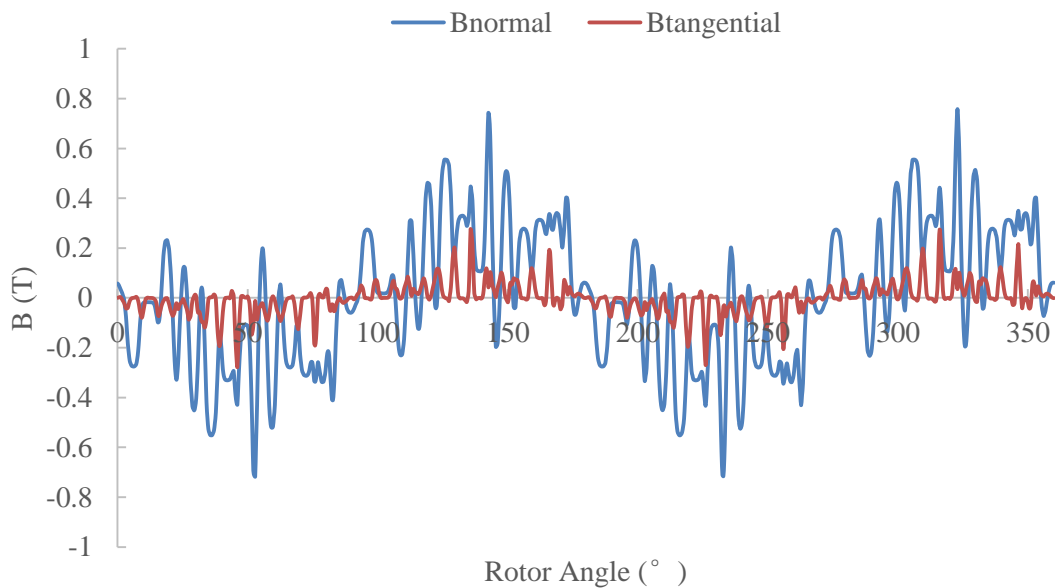


Figure 3.16 Air-gap flux density of normal and tangential components.

### 3.4.4 Core Loss

As introduced in section 3.3, the hysteresis loss  $P_h$  is related to the hysteresis loop area and the frequency of the magnetic field in sinusoidal systems [99], which can be described as in equation 3.28.

$$P_h = k_h f B_m^2 \quad (3.28)$$

where  $k_h$  is the hysteresis coefficient,  $f$  is the frequency, and  $B_m$  is the flux density.

The eddy current loss  $P_e$  occurs in magnetic material due to the induced electric current, which can be shown as in equation 3.29.

$$P_e = k_e f^2 B_m^2 \quad (3.29)$$

where  $k_e$  is the eddy current coefficient.

Hence, analytical approximation is chosen to determine the core loss in the finite element program, as shown in equation 3.30, and the relationship between the maximum magnetic field intensity and the value of core loss for the magnetic material M600-50A at 50 Hz is presented in figure 3.17.

$$P = k_h f^\alpha B^\beta + k_e (fB)^2 \quad (3.30)$$

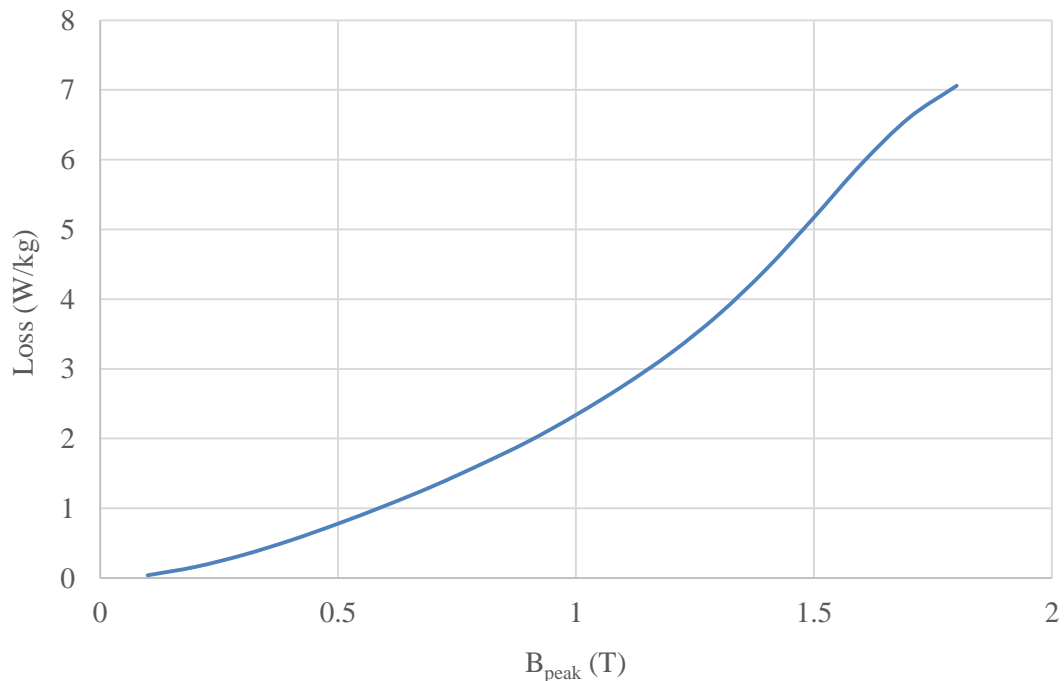


Figure 3.17 Magnetic loss estimation for FEM.

For this DFIG model, finite element program calculates the solution of the core loss, which is 915.1W.

### 3.4.5 Electrical Conductor Loss

The material of the electrical conductor is selected as copper 100% IACS in the FEM, and the electrical resistivity of the conductor is  $1.7241 \times 10^{-8} \Omega\text{m}$  at  $20^\circ\text{C}$  and the value varies with temperature as referred to in section 5.2.4. Section 3.2.3 introduced the complex winding layouts and design of this machine, where the stator coil pitch is 1-14 with two parallel delta connections and the rotor coil pitch is 1-12 with two parallel star connections. Both stator and rotor adopt a double layer connection. Beside this, a winding temperature of  $20^\circ\text{C}$  is assumed. The winding resistance of the original machine is then calculated as in the following equations.

The one-wire resistance of the stator winding is calculated as follows:

$$R_1 = \rho_{20} \frac{L_{s1}}{A_{s1}} = 0.017241 \times \frac{0.48676}{4.29} = 0.00196 \Omega \quad (3.31)$$

Because of the two routes in the parallel connection layout of the stator winding, the single route winding resistance of the stator winding is expressed as:

$$\begin{aligned} R_1' &= R_1 \times \frac{\text{number of stator slots}}{\text{phase number}} \times \frac{\text{stator winding turns in one slot}}{\text{route number of parallel connection}} \\ &= 0.00196 \times \frac{60}{3} \times \frac{16}{2} = 0.3136 \Omega \end{aligned} \quad (3.32)$$

Hence, the phase resistance of the stator winding is calculated as:

$$R_{ps} = \frac{R_1' R_1'}{R_1' + R_1'} = \frac{R_1'}{2} = 0.1568 \Omega \quad (3.33)$$

The one-wire resistance of the rotor winding is determined as follows:

$$R_2 = \rho_{20} \frac{L_{r1}}{A_{r1}} = 0.017241 \times \frac{0.45233}{6.95} = 0.00112 \Omega \quad (3.34)$$

The rotor winding design uses a double layered structure too, so the single route winding resistance of the rotor's winding is as follows:

$$\begin{aligned}
 R_2' &= R_2 \times \frac{\text{number of rotor slots}}{\text{phase number}} \times \frac{\text{rotor winding turns in one slot}}{\text{route number of parallel connection}} \\
 &= 0.00112 \times \frac{48}{3} \times \frac{12}{2} = 0.10752 \Omega
 \end{aligned} \tag{3.35}$$

The phase resistance of the rotor winding is then calculated as in equation 3.36:

$$R_{pr} = \frac{R_2' R_2'}{R_2' + R_2'} = \frac{R_2'}{2} = 0.0538 \Omega \tag{3.36}$$

It is now possible to investigate the accuracy of the model used to determine the three-phase conductor losses of the stator and rotor and to predict machine efficiency. According to Joule's law, the three-phase stator conductor loss is 2163.8W and the rotor conductor loss is 1085.4W. Therefore, the total losses are 3249.2W.

### 3.5 Summary

An off-the-shelf three-phase four-pole DFIG has been chosen and analysed for a wind turbine application. The mechanical construction and materials of the DFIG having different numbers of slots but similar types of slot shapes in the stator and rotor laminations have been described. The winding design has been extensively investigated, and the three-phase winding configurations for both stator and rotor presented with the initial settings of the parameter of the winding.

The characteristics and estimations of all the losses in DFIG have been described, which could be split into two main parts: conventional losses and additional loss. Among the conventional losses, conductor losses and core loss can be calculated using finite element electromagnetic analysis. However, the windage and friction loss and additional loss (SLL) cannot be obtained from the FEM.

A two-dimensional DFIG has then been extensively simulated to predict the conductor losses and core loss using FEM, and also the FE model is validated using magnetic field analysis.

## **Chapter 4 Surrogate-based Analysis and Optimisation of Rewinding Design**

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The main aim of this PhD work is to apply a novel approach to the optimisation of winding repair and re-design for a doubly fed induction generator, in order to improve the performance of the machine. The number and locations of sampling points used for simulation is determined according to the Latin Hypercube sampling. Then the method for the construction of the surrogate model is investigated, and the Kriging model is chosen. The relationship between machine performance and different winding parameters is investigated in great detail for the stator and rotor separately, and combined. Three sets of optimisation results for the winding are provided using the particle swarm optimisation algorithm, since winding faults may occur in either the stator, the rotor, or both stator and rotor.

## 4.1 Introduction

A major challenge in the successful full-scale development of electrical machines is to balance competing objectives, such as improved performance, reduced costs, and a wide application field. In this regard, accurate, high-fidelity models are typically obtained by using numerical FEM [100], which takes into account the complex topology of the electrical machine as well as its multi-physical characteristics, such as eddy currents and magneto thermal coupling [101].

However, FEM optimisation has the obvious disadvantages of being time consuming and computationally expensive, due to the objective function needing to be evaluated for each set of structural parameters. There is a way to solve this problem; however, using a simplified objective function instead of the FEM estimation which requires less computing time since it reduces the number of FEM simulation needed. A series of approximation methods have been developed, such as polynomial regression [2], radial basis function [102], multi-quadratic basis functions [103, 104], or diffuse element approximations [105]. Furthermore, the optimisation of electrical machines involves a large amount of model parameters problems, which means that the number of objective function estimations significantly increases. Therefore, the optimal design process is difficult to identify when a multi-dimensional approximation of the objective function is created. In order to solve this problem, statistical methods have been developed to evaluate the relationships between the parameters of electrical machines and the relevant numerical simulation results in order to reduce the number of significant parameters required for efficiency optimal design [101]. A wide variety of statistical methods and analyses called “design of experiment” has been developed [106, 107], initially in agricultural and industrial applications [101].

The surrogate-based approach is an effective tool for the analysis and optimisation of computationally expensive models, and is suitable for electrical machine optimisation. The surrogate model is constructed by using the data obtained from high-fidelity models, and it provides rapid approximations of objectives and constraints at new design points so that optimisation studies are feasible [108]. Surrogate-Based Analysis and Optimisation (SBAO) has been successfully applied in industrial applications, for example in rotor blade design and optimisation [109], high-speed civil transport [110], aerofoil shape optimisation [111-113], diffuser shape optimisation [114], supersonic turbines [115-117], and injectors [116-120]. However, no previous study has considered winding in electrical machines, and so this research is the first to adopt SBAO for the winding design and optimisation of an induction machine.

## 4.2 Overview of Surrogate Modelling

Before SBAO is carried out, surrogate modelling is the key part of the process. This can be understood as a nonlinear inverse problem [121] to determine a continuous function ( $f$ ) of a set of design variables from a limited amount of available data ( $f$ ) [108]. These available data ( $f$ ) are used to evaluate the real function ( $f$ ), even though in general the available data could not carry sufficient information to identify a real function ( $f$ ). This means that a variety of estimated functions may be built based on the available data ( $f$ ), as shown in figure 4.1, with an assumed error of zero.

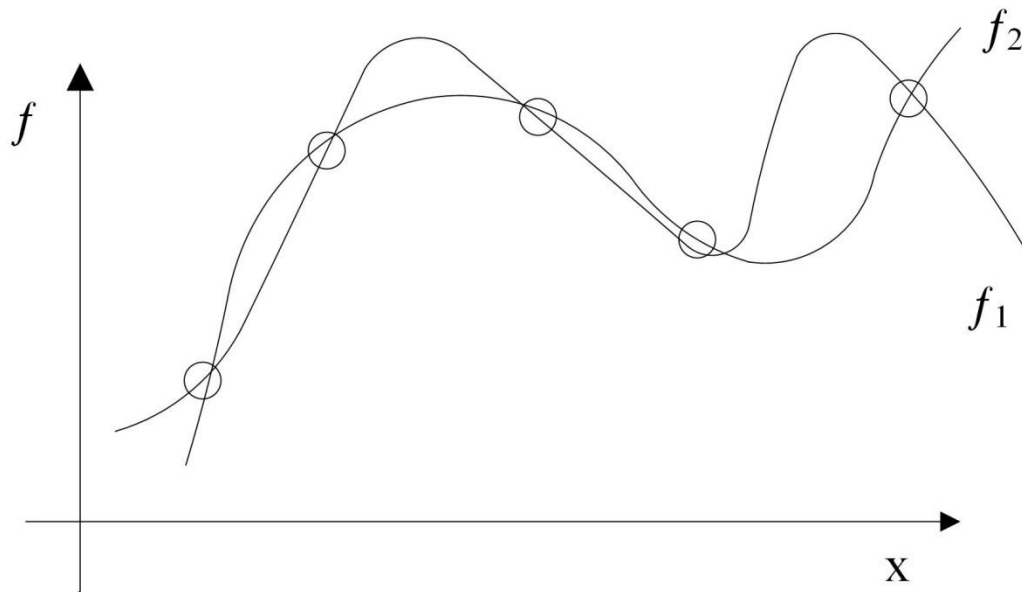


Figure 4.1 Different surrogate models may be constructed with the same data.

Therefore, in building a surrogate model two problems have to be faced: estimating the surrogate model based on the available data, and evaluating the model by assessing its errors  $\varepsilon$  [122, 123]. Hence, the predicted surrogate function based on simulation models can be expressed as  $f_p(x) = \hat{f}(x) + \varepsilon(x)$ . In general, the variance of the predicted value is affected by a probability density function  $\theta$ , which means that the estimated uncertain area is a small part of the area as shown in figure 4.2. So the challenge of surrogate modelling is to build a surrogate model as accurately as possible, whilst using as few as possible simulation estimations.



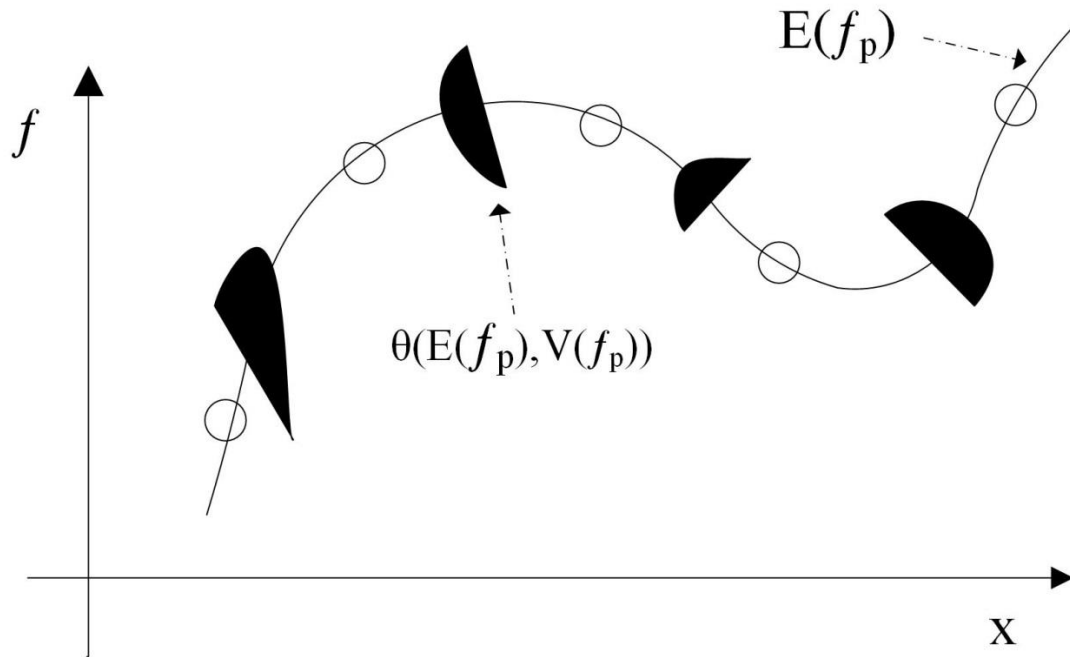


Figure 4.2 Predicted uncertain area using probability density function  $\theta$  in the predicted function  $E(f_p)$  [108].

The main advantage of a surrogate model is that it can be constructed without previous knowledge of the physical system of interest, and it can be used for a wide variety of problems. Importantly, evaluation of the model is often very cheap, but the selection of the amount of data used should be considered carefully to ensure a reasonable general level of accuracy [124, 125]. Figure 4.3 shows the procedures used for surrogate model construction where the design of experiment is for allocation of sampling points in the design space, and then the surrogate model is constructed using predicted approximation approaches which have been proven to be effective [126-129], such as polynomial regression, Gaussian radial basis function, neural network [130], and the Kriging model [131]. Model estimation and model appraisal in these methods are discussed later. The next step is to check for convergence, and if the results have not converged, the construction has to go back to the design of experiment to repeat the procedures. Once results are converged and the model is validated, the surrogate model has been built successfully.

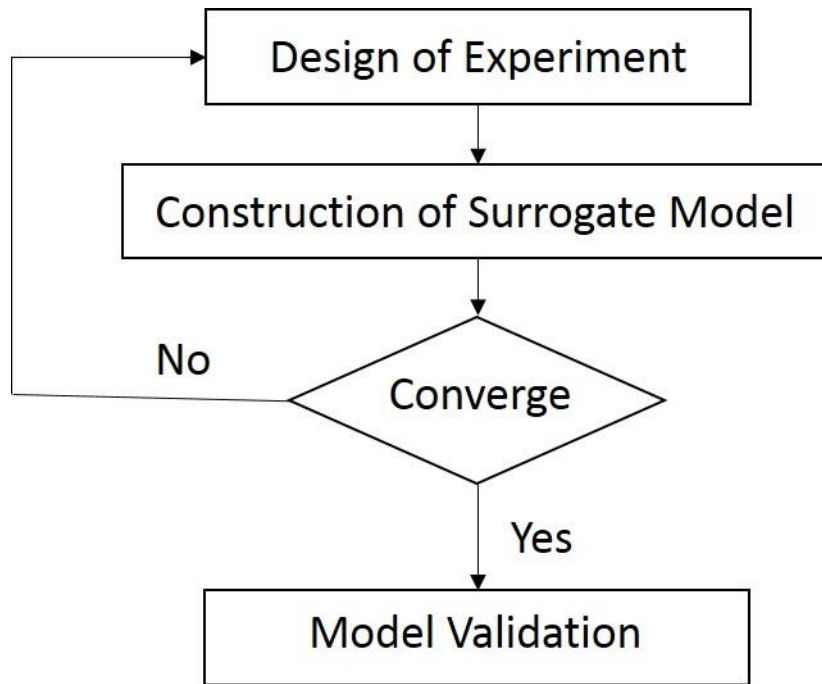


Figure 4.3 The flowchart of surrogate model construction.

### 4.3 Design of Experiment

The design of experiment (DoE) is the sampling plan to allocate sampling points in variable design space [108, 132-134], which aims to maximise the amount of information acquired and minimise the bias error. Sampling plans provide unique values of input variables at each point in the input space. Meanwhile, a high-fidelity model will be simulated at these sampling locations to acquire the training data set which will be used to construct the functional surrogate model. However, due to the computational expense involved the number of sample points is severely limited, and a balance between bias error and variance errors should be found during the construction of the surrogate model. If a surrogate model has a lower bias error, so a larger variance is needed, and vice versa. Both bias error and the variance could be decreased by adding to the number of sampling points at the expense of computing costs. Therefore, there is a clear trade-off between the number of points selected and the amount of information that can be extracted from these points.

At present, several different DoE techniques have been adopted based on the different characteristics and conditions of the design. Conventional DoE techniques are factorial designs applied to discrete design variables to explore a large region of the search space [132]. Here, if the design variables are continuous, they will be easily analysed once discretized. Factorial designs can be categorized as full factorial, fractional factorial, central composite, star, and Box-Behnken designs [135] as shown in figure 4.4.

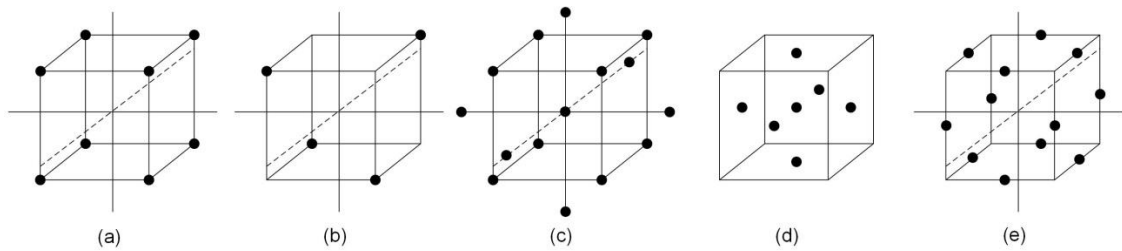


Figure 4.4 Factorial designs for three design variables ( $n=3$ ): (a) full factorial design, (b) fractional factorial design, (c) central composite design, (d) star design, and (e) Box-Behnken design [135].

For general use, bias error can be reduced through a DoE that distributes the sample points uniformly in the design space [136-138]. When all the possible sampling points are combined together, as shown in figure 4.4 (a), the structure is defined as a full factorial design. Moreover, if model evaluation is expensive and the number of design variables is large, a fractional factorial design will be more efficient, as shown in figure 4.4 (b). This is because in the full factorial design, the increasing number of design variables leads to an exponential increase in the number of sampling points, and this also sometimes happens when the computational expense prohibits the full factorial designs. The star design shown in figure 4.4 (d) is generally adopted in combination with space mapping [139].

If there is no prior knowledge about the objective function, some modern DoE techniques have been developed for deterministic experiments without the random error which arises in laboratory experiments, such as orthogonal array design and Latin Hypercube sampling. The former is a uniform design but it generates particular forms of point replications; the latter has variable sampling locations in the design space, but the points are not replicated.

### 4.3.1 Orthogonal Array Design

The Orthogonal Array Design (OAD) [108] of strength  $t$  is a matrix of a number of samples  $N_s$  and a number of variables  $N_{dv}$  with elements taken from a set of  $q$  symbols. The  $q$  symbols are the levels defined for the variables of interest. Moreover, the strength  $t$  is an indication of how many effects can be accounted. So the OAD can be expressed as: OAD ( $N_s, N_{dv}, q, t$ ) [108].

However, there are two limitations which must be considered carefully when the OAD is adopted in DoE techniques:

- Lack of flexibility. Although the input parameters are sometimes provided, an orthogonal array may not exist [108].

- Point replication. OAD works on the subspace spanned by the effective factors, which could generate replicated points. This may cause bias error, which has a deleterious effect on the model estimation.

### 4.3.2 Latin Hypercube Sampling (LHS)

One of the most popular DoE techniques is Latin Hypercube sampling (LHS) [140], which is a type of stratified sampling approach with the restriction that each of the input variables has all portions of its distribution represented by input values [140]. In practice, the range of every parameter for  $n$  design variables is separated as  $p$  bins, so that the total number of  $p^n$  bins will be generated in the design space. The samples are randomly selected in the design space, and each will be located randomly in one of the whole bins, and a simple chart of LHS is shown in figure 4.5. Moreover, there is exactly one sample in each bin for all one-dimensional projections of the  $p$  samples and bins [135]. So the standard LHS is commonly not a uniform distribution.

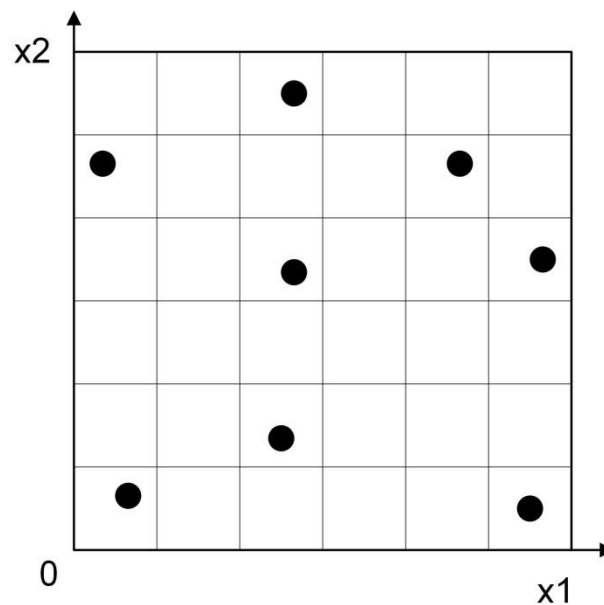


Figure 4.5 Latin Hypercube Sampling with  $p=8$ ,  $n=2$  for uniform distribution.

While LHS represents an improvement over unrestricted stratified sampling [141], it can provide sampling plans with very different performance in terms of uniformity, as shown in figure 4.6. As a result, the LHS approach is adopted as the DoE technique in this work.

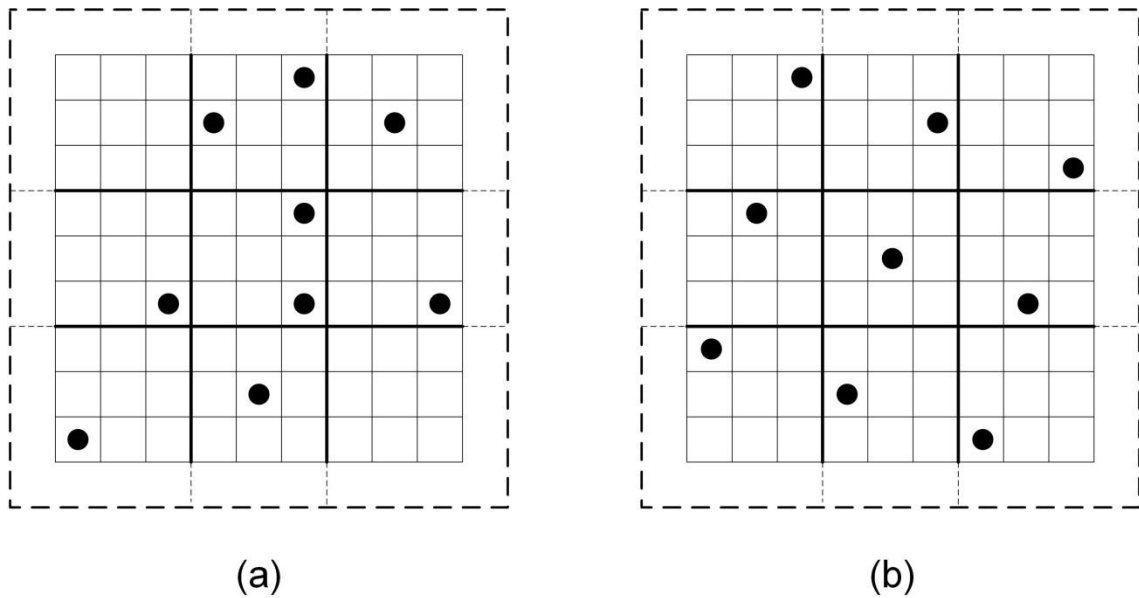


Figure 4.6 Different performance of LHS in terms of uniformity.

#### 4.4 Construction of Surrogate Model

Once the DoE technique has been selected and the data obtained from the high-fidelity model simulation, a suitable approximation approach is chosen in the next step. Parametric approaches such as polynomial regression model (PR) assume that the global functional form of the relationship between the response variable and the design variables is known [108]. A non-parametric approach such as the radial basis function (RBF) builds the overall model by using different types of simple local models in different regions of the data. Furthermore, a semi-parametric approach called the Kriging model has been developed which has the advantages of both parametric and non-parametric methods. For example, it allows much more flexibility than parametric models, since no specific model structure is used, and the non-parametric part is considered as the realization of a random process [142]. In this section, brief introductions to these approximation methods for the surrogate model are presented.

##### 4.4.1 Polynomial Regression Model

PR analysis is a method to estimate the relationship between the prediction function  $f$  and basis function  $z_j$  with the number of basis functions  $N_{PR}$  [143], so the linear regression model is expressed as in the equation below:

$$f(z) = \sum_{j=1}^{N_{PR}} \beta_j z_j + \varepsilon \quad (4.1)$$

$$V(\varepsilon) = \xi^2 \quad (4.2)$$

where  $\varepsilon$  is the unobserved random error with an expected value equal to zero and a variance of  $\zeta^2$ . For example, second order polynomial regression models with one variable and two variables are shown in the following equation:

$$f(z) = \beta_0 + \beta_1 z + \beta_2 z + \varepsilon \quad (4.3)$$

$$f(z) = \beta_0 + \beta_1 z_1 + \beta_2 z_2 + \beta_{11} z_1^2 + \beta_{22} z_2^2 + \beta_{12} z_1 z_2 + \varepsilon \quad (4.4)$$

So a  $N_s \times N_{PR}$  matrix  $X$  of the set of equations above can be expressed with the number of sampling points and the design variables, which is a general model for fitting any relationship that is linear to the unknown parameter  $\beta$  as:

$$f = X\beta + \varepsilon \quad (4.5)$$

Hence, a solution for the estimated parameter  $\hat{\beta}$  using least square method can be calculated as [144]:

$$\hat{\beta} = (X^T X)^{-1} X^T f \quad (4.6)$$

However, there is an important limitation of polynomial regression models, which is the order of the model. The order should be as low as possible and high order polynomials of more than two should be avoided.

#### 4.4.2 Radial Basis Function

The RBF belongs to the class of generalized linear models, which has been developed for the interpolation of scattered multivariate data [108, 145]. The approximation method using linear combinations of symmetrical functions  $\phi_j$  with the number of radial basis functions  $N_{RBF}$  is shown in the next equation:

$$f(r) = \sum_{j=1}^{N_{RBF}} \omega_j \phi_j \left( \|r - r_c^{(j)}\| \right) + \varepsilon \quad (4.7)$$

where  $\omega_j$  is the coefficients of linear combinations and  $r_c^{(j)}$  is the different basis function centres.

Similar to the polynomial regression model, the radial basis function can be expressed as:

$$f = \omega_j \Phi + \varepsilon \quad (4.8)$$

The coefficient of linear combinations  $\omega$  can then be computed from:

$$\omega_j = (\Phi^T \Phi)^{-1} \Phi^T f \quad (4.9)$$

And the radial basis function  $\Phi$  is a matrix with the number of sampling points and the number of basis function  $N_s \times N_{RBF}$  given by:

$$\Phi = \begin{bmatrix} \varnothing(\|r^{(1)} - r_c^{(1)}\|) & \varnothing(\|r^{(1)} - r_c^{(2)}\|) & \dots & \varnothing(\|r^{(1)} - r_c^{(N_{RBF})}\|) \\ \varnothing(\|r^{(2)} - r_c^{(1)}\|) & \varnothing(\|r^{(2)} - r_c^{(2)}\|) & \dots & \varnothing(\|r^{(2)} - r_c^{(N_{RBF})}\|) \\ \vdots & \vdots & \ddots & \vdots \\ \varnothing(\|r^{(N_s)} - r_c^{(1)}\|) & \varnothing(\|r^{(N_s)} - r_c^{(2)}\|) & \dots & \varnothing(\|r^{(N_s)} - r_c^{(N_{RBF})}\|) \end{bmatrix} \quad (4.10)$$

### 4.4.3 Kriging Model

The Kriging model is currently gaining in popularity as a technique to interpolate deterministic noise-free data [146-149]. The basic formulation of the Kriging model is to estimate the value of a function or response at some unknown location or area, which comprises of two components: the polynomial model and a systematic departure representing either small scale components with high frequency variation or large scale components with low frequency variation [150].

The systematic departure component represents the fluctuations around the real function, with the basic assumption being that these are correlated and the correlation depends only on the distance between the locations under consideration [108]. More precisely, a zero mean, second-order, stationary process is represented as described by a correlation model. Therefore, an approximation expression of the Kriging model is given by:

$$y(t) = \beta + z(t) \quad (4.11)$$

where  $\beta$  is a constant, and the fundamental function  $z(t)$  is calculated by Gaussian distribution with error, where the residual error is an independent, identically distributed error or normal random variables whose mean and variance are 0 and  $\zeta^2$  respectively. If  $\hat{y}(t)$  is defined as the approximation model, and the mean-squared error of  $y(t)$  and  $\hat{y}(t)$  are minimum, satisfying the unbiased condition,  $\hat{y}(t)$  is estimated as

$$\hat{y}(t) = \hat{\beta} + r^T R^{-1} (y - \hat{\beta}q) \quad (4.12)$$

where  $R^{-1}$  is the inverse of the correlation matrix  $R$ ,  $r$  is the correlation vector,  $y$  is the ns observed data vector, and  $q$  is the unit vector. The correlation matrix and correlation vector are

$$R(\mathbf{t}^j, \mathbf{t}^k) = \text{Exp} \left[ -\sum_{i=1}^n \theta_i |t_i^j - t_i^k|^2 \right] \quad (4.13)$$

$$(j = 1, 2, \dots, ns, k = 1, 2, \dots, ns) \quad (4.14)$$

$$\mathbf{r}(\mathbf{t}) = \left[ R(\mathbf{t}, \mathbf{t}^{(1)}), R(\mathbf{t}, \mathbf{t}^{(2)}), \dots, R(\mathbf{t}, \mathbf{t}^{(ns)}) \right]^T \quad (4.15)$$

The parameters  $\theta_1, \theta_2, \dots, \theta_n$  are unknown, but they can be calculated using the following equation.

$$\text{maximise} - \frac{[n_s \ln(\widehat{\sigma}^2 + \ln|\mathbf{R}|)]}{2} \quad (4.16)$$

where  $\theta_i (i=1, 2, \dots, n) > 0$ .  $\theta_i$  can be solved using the optimisation algorithm.

With given the various approximation methods which have been developed, it is important to select a relatively high precise method to construct a surrogate model. Various studies have compared the precision of the estimated models using the RBF and Kriging methods, as the Kriging model has been found to be more accurate [142, 151]. As a result, the Kriging model is employed in this work as the approximation method used to construct the surrogate model.

#### 4.5 Surrogate-based Optimisation

Surrogate model-based optimisation accomplishes optimisation rapidly by using a surrogate model for the objective and constraint functions. The surrogate model is able to address optimisation problems with non-smooth or noisy responses, and can even provide insights into the nature of the design space [119, 120, 152, 153]. SBAO has also been found to be effective in both multi-disciplinary and multi-objective optimisation [108]. The optimisation algorithms of SBAO are discussed next.

The proposed surrogate-based analysis and optimisation algorithm is shown as a flowchart in figure 4.7. The part of procedures have been introduced in the section 4.3 and 4.4, indicating how to build the surrogate successfully. Before constructing the surrogate model, the problem definition should make clear which parameters need to be varied or constrained, and what the objective of the optimisation is. Furthermore, an optimisation algorithm is required to achieve the SBAO.



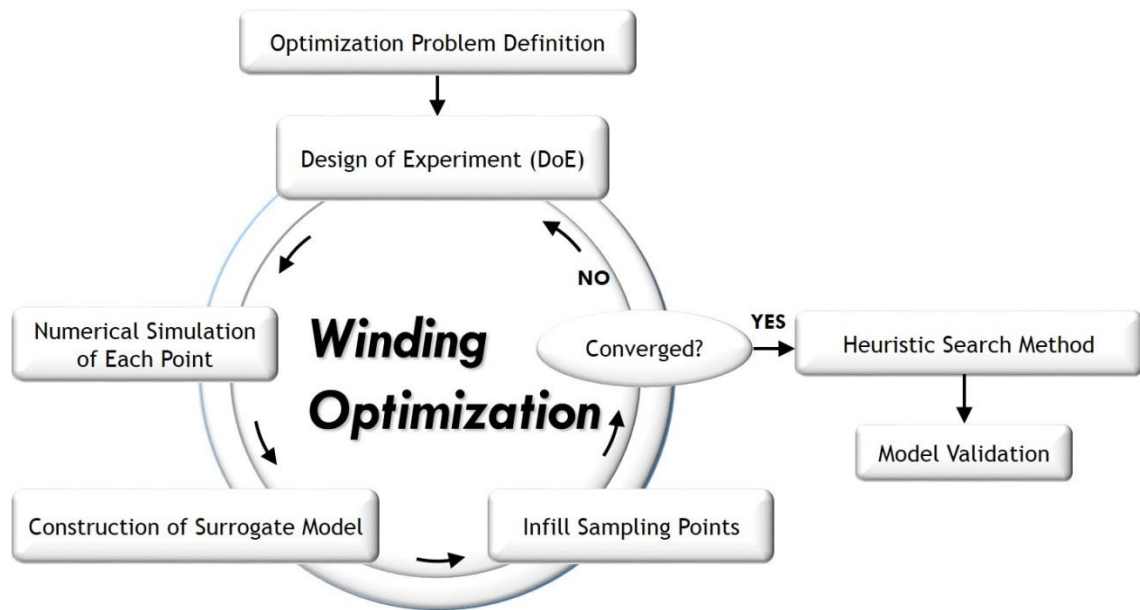


Figure 4.7 Surrogate-based analysis and optimisation.

- *Optimisation Problem Definition.* Before any optimisation design is carried out, the objectives and number of variables and constraints must be defined carefully.
- *Design of Experiment.* The design of experiment method is adopted to determine the locations of sampling points in the specific design space. In this step, the number of sampling points is severely limited, because of the computing expense for each sample point.
- *Numerical Simulation of Each Point.* A computationally expensive model with all the variables is simulated, and the variables are determined using the DOE method.
- *Construction of Surrogate Models.* The selection of methods used for building the surrogate model and model identification must be carefully considered.
- *Infill Sampling Points.* This step makes the estimated function more accurate by adding more sampling points at specific locations. If the results converge, then the model estimation is stopped.
- *Converge.* The convergence of the surrogate model can be judged according to the linking of infill sampling points. If there is no convergence, the ‘best’ point has to be added into the DoE again to obtain the next best point. Upon convergence, the surrogate model has been built successfully.
- *Heuristic Search Method.* When the surrogate model has been built, the exact optimal point is found using the optimisation method.
- *Model Validation.* The purpose of this step is to evaluate the precision of the predicted surrogate model to the actual objective function.

The optimisation of electrical machines is a multi-variable and multi-modal problem [154-160]. In such cases, a wide range of optimisation algorithms have been developed. In the past, these optimisation algorithms were mostly used in combination with analytical models [161, 162]; however, there has been a trend in recent years to combine them with FEM [163, 164]. Hence, the time and computing costs are important in judging which algorithm is more suitable. At present, two main types of evolutionary optimisation algorithms are commonly adopted: genetic algorithm and particle swarm optimisations.

#### 4.5.1 Genetic Algorithm

The genetic algorithm (GA) was developed using the principles of evolution, natural selection and genetics from natural biological systems [165, 166]. During GA computing, a population of artificial individuals is modified repeatedly based on biological evolution rules that converge towards a better solution of the problem to be solved. At each step, individuals are selected randomly from the current population to be parents. These individuals are used to produce children for the next generation. Based on biological principles, the fittest individuals survive and the least fit die.

Generally, a GA consists of three main procedures: selection, crossover, and mutation. It starts with an initial population containing a number of chromosomes each of which represents a solution to the problem. However, some chromosomes are not fit, and these will be ignored while only the fittest chromosomes will be designated for reproduction. In order to keep the size of the initial population stable, some fit chromosomes will be used more than once, so this subset is called the 'mating pool'. The purpose of this selection operation is to obtain a mating pool with the fittest individuals according to a probabilistic rule that allows the fittest individuals to be mated into the new population. After the selection stage, a genetic crossover operation is then applied between parent pairs from the mating pool. Each pair will produce two children to maintain the size of the population. The crossover operation forces the new chromosomes to have the properties and characteristics of both parents. Mutation is the final operation which takes place after crossover and introduces a change into the offspring bit string to produce new chromosomes. Besides this, it may represent a solution to the problem whilst avoiding the population falling to a local optimal point. The mutation operation is performed with a probability of mutation which is usually low. This preserves good chromosomes and mimics real life where mutations rarely happen. The new individuals created by these three basic operations may be fitter than their parents. This algorithm is repeated for many

generations and finally stops when individuals are produced who provide an optimal solution to the problem. GA optimisation is shown in figure 4.8 in detail.

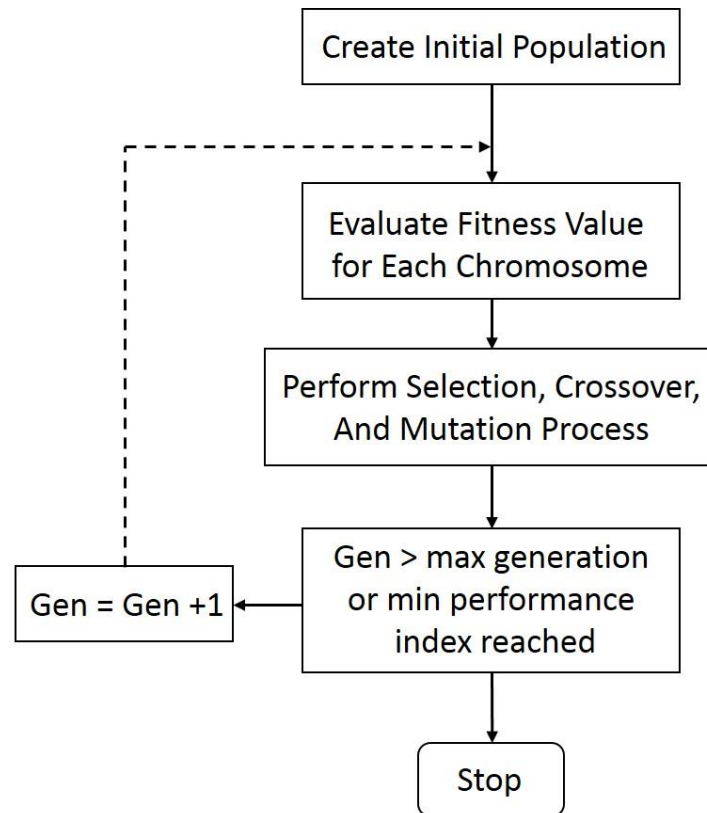


Figure 4.8 Genetic algorithm optimisation.

The GA has been used for the optimisation of an induction machine [167, 168], and has also been proposed to address complex problems [169, 170]. However, a GA requires many function calls to find a local peak, which significantly increases the time taken for optimisation. The FEM needs to be run at every function call, and one solution of the FEM takes a long time [171-173]. This is particularly inconvenient in the design of electrical machines with large numbers of function calls needed.

#### 4.5.2 Particle Swarm Optimisation

Particle swarm optimisation (PSO) has been identified as quite effective in optimising difficult multi-dimensional problems in a variety of fields [174, 175], and it has been successfully applied to many optimisation problems [175-181]. In an optimisation case, PSO can be described as an animal or particle moving from a certain position at random velocity in a search field. Within a population (called a swarm), each particle is treated as a point in a d-dimensional design space. Each particle keeps track of its position in the solution space that is associated with a fitness value, termed the personal best (*pbest*). Meanwhile, there exists a global best fitness value called the global best (*gbest*). This is achieved by the whole swarm. The operation

of PSO gradually changes the velocity of each particle toward its *pbest* and *gbest* positions each time. The new velocity and position follow

$$V_j^{k+1} = wV_j^k + C_1\varphi_1(p_j^k - X_j^k) + C_2\varphi_2(p_g^k - X_j^k) \quad (4.17)$$

$$X_j^{k+1} = X_j^k + V_j^{k+1} \quad (4.18)$$

where  $V_j^k$  and  $X_j^k$  are the velocity and location of the  $j$ th particle at iteration  $k$ ;  $p_j^k$  is the *pbest* of particle  $j$  at the  $k$ th iteration;  $p_g^k$  is the *gbest* of the entire swarm at the  $k$ th iteration;  $C1$  and  $C2$  are acceleration factors;  $\varphi_1$  and  $\varphi_2$  are the uniformly distributed random numbers between 0 and 1; and  $w$  is the inertia weight that controls the influence of the previous velocity on the new velocity. Each particle will try to change its position according to four variables: the current position, the current velocity, the distance between the current position and *pbest*, and the distance between the current position and the *gbest*. The PSO algorithm is illustrated in figure 4.9.

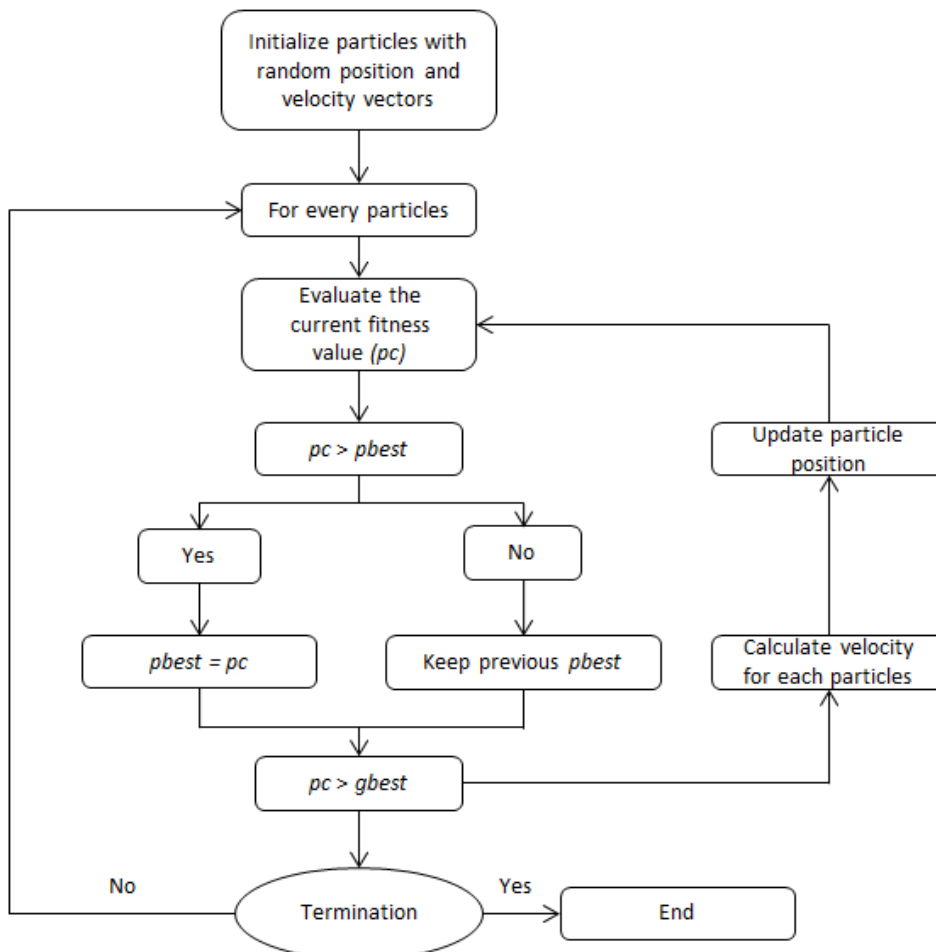


Figure 4.9 Particle swarm optimisation algorithm.

There is a large body of work comparing the GA and PSO to show which is more effective and accurate [161, 182, 183]. From the results, the PSO performs better in terms of optima found and time required to find these optima [184]. It is also suggested that PSO performs better in terms of simple implementation and high computational efficiency with few control parameters [174, 185]. For these reasons, the PSO is chosen as the optimisation algorithm in this work.

## 4.6 Stator Rewinding Design

As mentioned in the literature review, if winding failure happens only in the stator winding and the rotor winding is without damage, only the stator winding could be replaced and the rotor winding left intact. This presents a good opportunity to re-design and re-wind the induction machine to make it more efficient. Unlike the original rewinding that follows the original design as closely as possible, this thesis investigates a novel method to optimise machine efficiency during the machine re-winding procedure. In the meantime, the relationship of efficiency to the winding turns and the C.S.A is plotted using the surrogate modelling method, which provides theoretical data for the machine winding design rather than conventional empirical information. Also the relationship between the torque and winding turns and C.S.A are provided. The detailed re-design and re-winding procedures are introduced in the following sections.

### 4.6.1 Optimisation Problem Definition

The objective of this work is to change the winding parameters to maximise machine efficiency by taking into account a combination of variables and constraints. The dominant two-dimensional parameters for optimisation are the number of stator winding turns  $N_{stator}$  and stator winding C.S.A  $A_{stator}$ , which can directly affect machine efficiency. Furthermore, some constraints are imposed by the limitations of manufacturing processes, which limit the maximum fill factor of stator slot with a thermocouple  $ff_{stator}$  on 40% or 44% without the thermocouple, torque  $T$  to maintain the machine power rating, and optimising range of winding turns and C.S.A. In order to build the model, the FEM-based commercial software *Infolytica Magnet* is used to analyse the performance of the induction machine with different winding parameter designs.

It should be noted that, in order to gain precise testing results, a thermocouple is inserted into the stator slot to test the winding temperature. This accounts for about 4% of the stator slot area, and here two optimisation plans are presented: one space for the thermocouple, the other without it. Therefore, the following general expression focuses on the optimisation problem definition for stator winding with a thermocouple.

$$\begin{aligned}
 \text{Objective} & \quad \text{Maximise efficiency } \eta \\
 \text{Subject to} & \quad 20\% \leq ff_{stator} \leq 40\% \\
 & \quad 360 \leq T \leq 363 \text{ Nm} \\
 & \quad 1.61 \leq A_{stator} \leq 8.5 \text{ mm}^2 \\
 & \quad 10 \leq N_{stator} \leq 24
 \end{aligned}$$

Similarly the optimisation problem definition for a stator slot without a thermocouple is:

$$\begin{aligned}
 \text{Objective} & \quad \text{Maximise efficiency } \eta \\
 \text{Subject to} & \quad 20\% \leq ff_{stator} \leq 44\% \\
 & \quad 360 \leq T \leq 363 \text{ Nm} \\
 & \quad 1.61 \leq A_{stator} \leq 8.5 \text{ mm}^2 \\
 & \quad 10 \leq N_{stator} \leq 24
 \end{aligned}$$

After determining the problem definition for the stator winding optimisation, the next step is to generate the sampling plan using the LHS method.

#### 4.6.2 LHS for Stator Winding Optimisation

The initial sampling plan is generated using the LHS realization of 50 samples, which is achieved via *Matlab* software and plotted as in figure 4.10. Now, the relative constraints for stator windings optimisation are plotted in the LHS plan. First of all, the two design variables ( $n_{dvs} = 2$ ) of stator winding turns and C.S.A are defined as x-axial and y-axial separately as shown in figure 4.11. The next constraint of the stator slot fill factor between 20% and 44% is displayed in figure 4.12, which is due to the maximum fill factor of the stator slot being 44%. The final sampling plan could then be obtained. However, there are some points which do not satisfy the design constraints, to add the constraints of fill factor to reduce the non-meaningful points. Figure 4.13 presents the available locations of sampling points, and information from these sampling points is fed into the finite element model to acquire simulated results for the construction of the surrogate model.

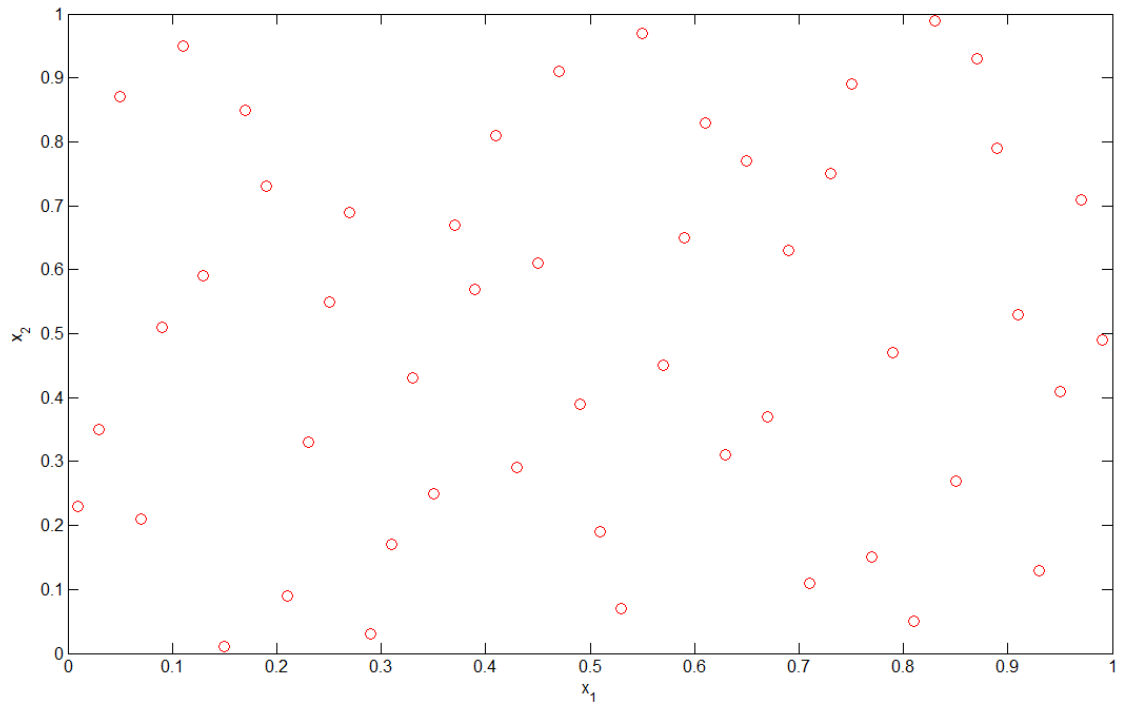


Figure 4.10 Initial Latin hypercube sampling plan for stator winding optimisation.

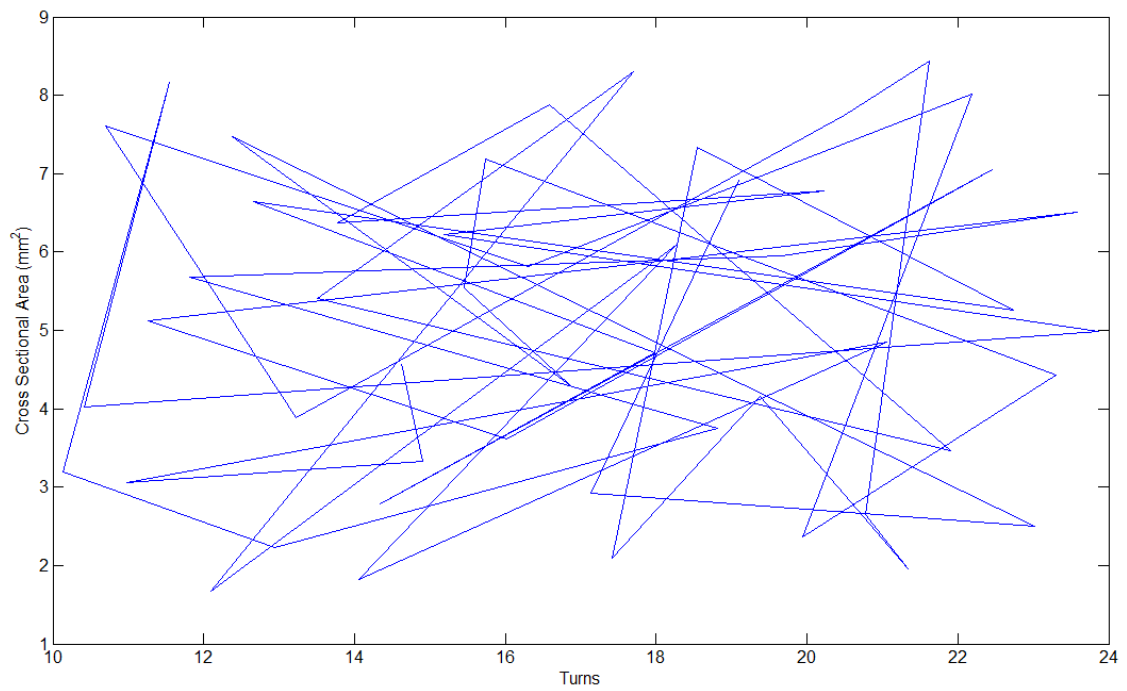


Figure 4.11 Definition of the constraints of stator winding turns and cross-sectional area.

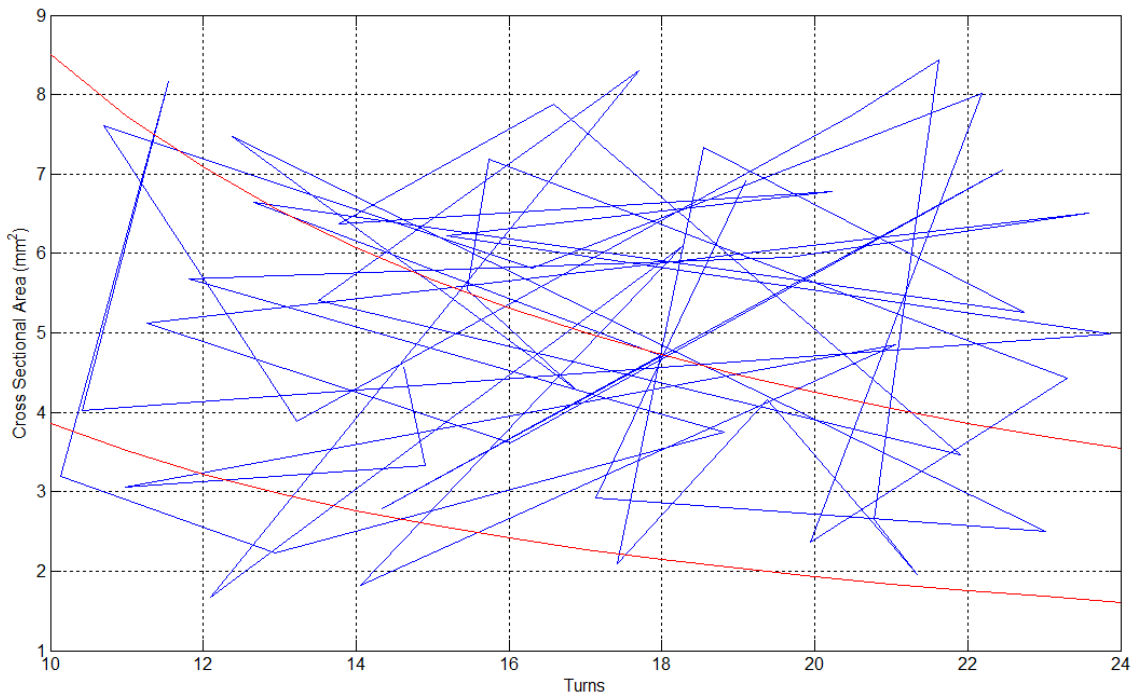


Figure 4.12 Definition of the constraint of stator slot fill factor.

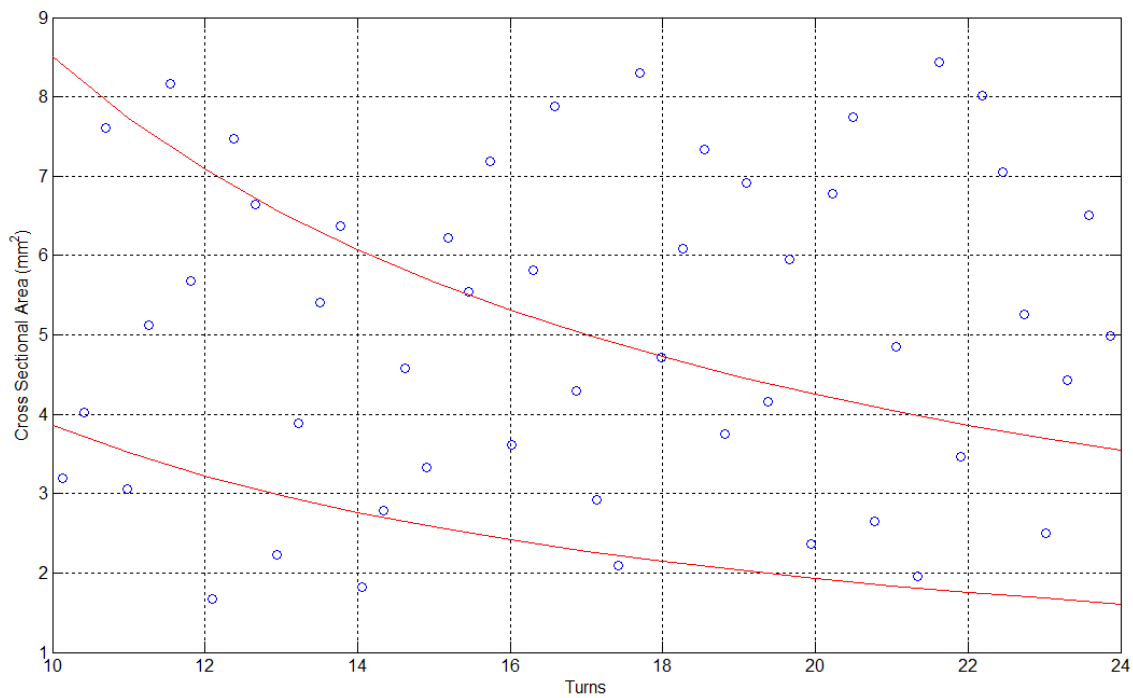


Figure 4.13 Latin hypercube sampling of stator winding optimisation.

### 4.6.3 Construction of Surrogate Model for Stator Winding

According to the Latin hypercube sampling plan for stator winding optimisation with two design variables (stator winding turns and C.S.A), a total of 21 available sampling points have been generated, and then each sampling point is run in the FEM to obtain the results used to



construct the initial surrogate model. Once the simulation results have been calculated, the relationship between efficiency and the two design variables can be plotted precisely, as well as the relationship between the torque and two design variables. The initial efficiency and torque contour of the stator winding optimisation function with two-dimensional variables are displayed in figures 4.14 and 4.15. Hence, the point of the highest efficiency in the initial surrogate model appears in top left corner, the winding parameter is 10 turns with  $8.2 \text{ mm}^2$  cross-sectional area.

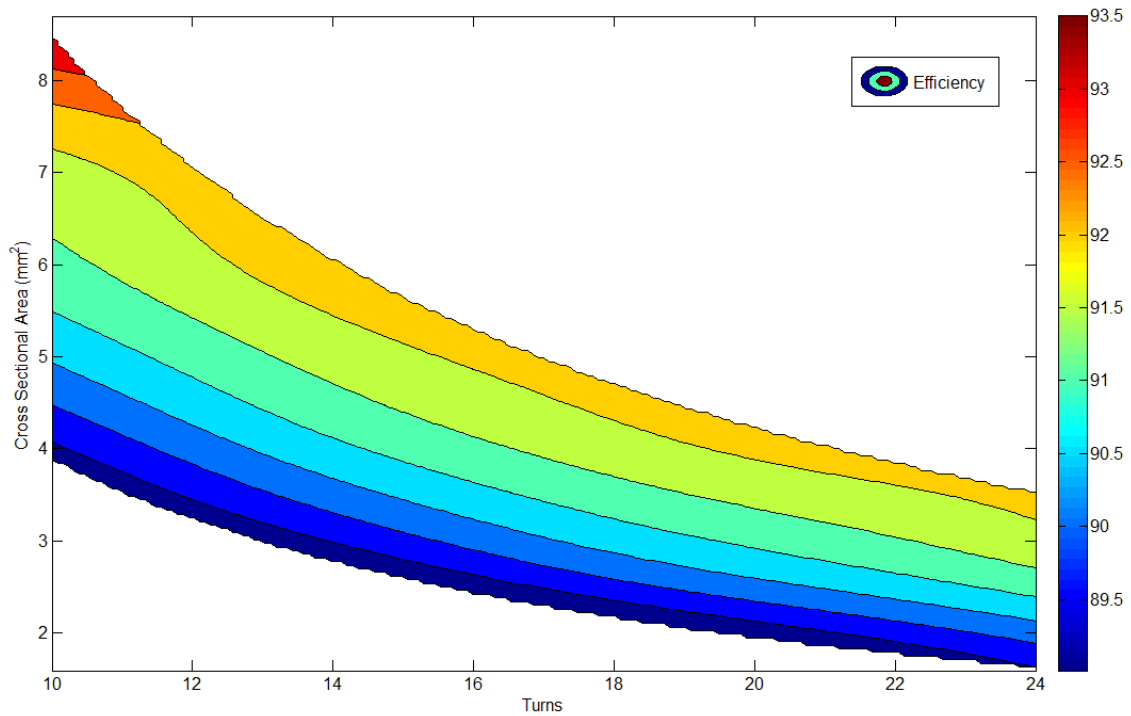


Figure 4.14 Initial efficiency contour of stator winding with two design variables.

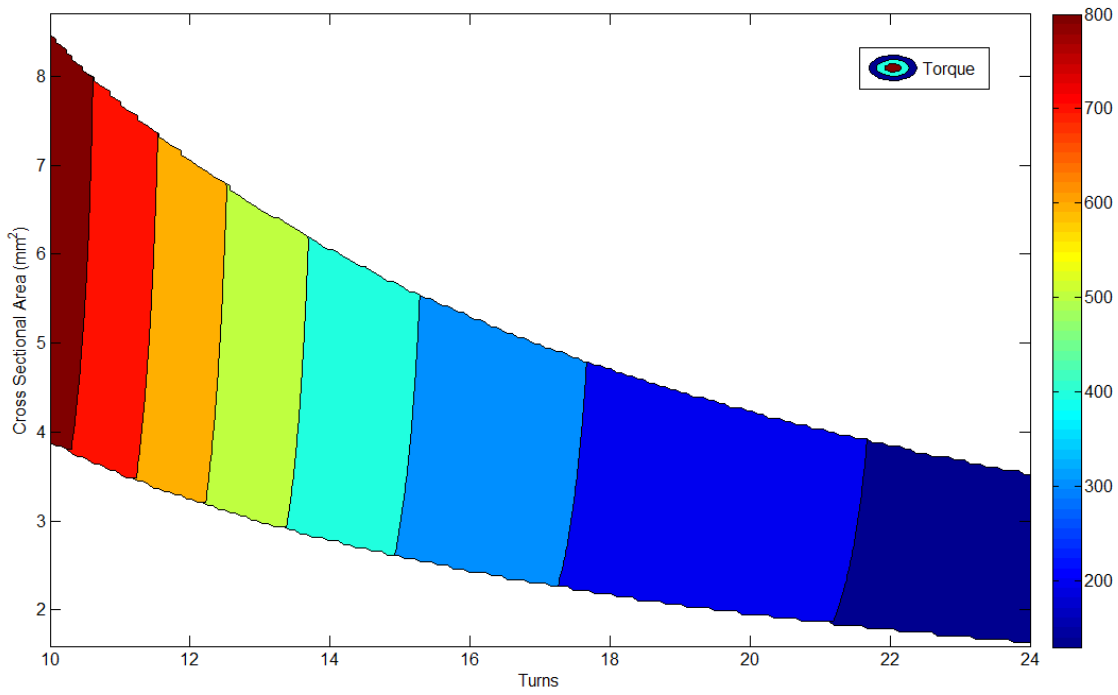


Figure 4.15 Initial torque contour of stator winding with two design variables.

Meanwhile, for a better comprehension of the relationship between efficiency and torque versus the two design variables, the initial three-dimensional distributions presented in figures 4.16 and 4.17.

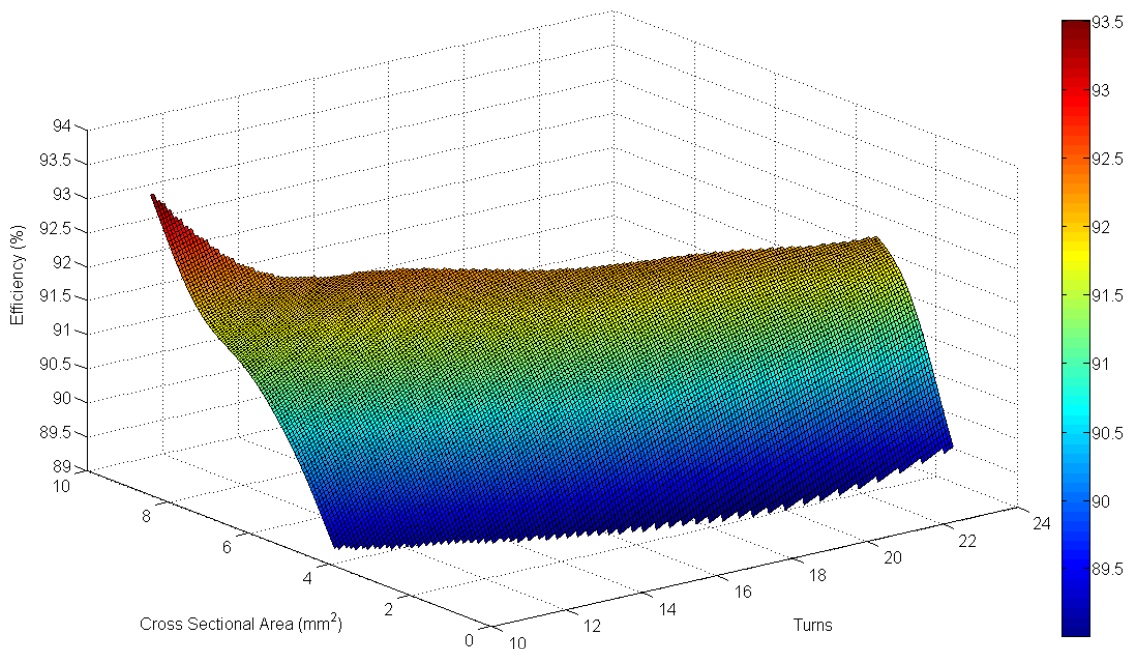


Figure 4.16 Initial three-dimensional efficiency distribution of stator winding with two design variables.

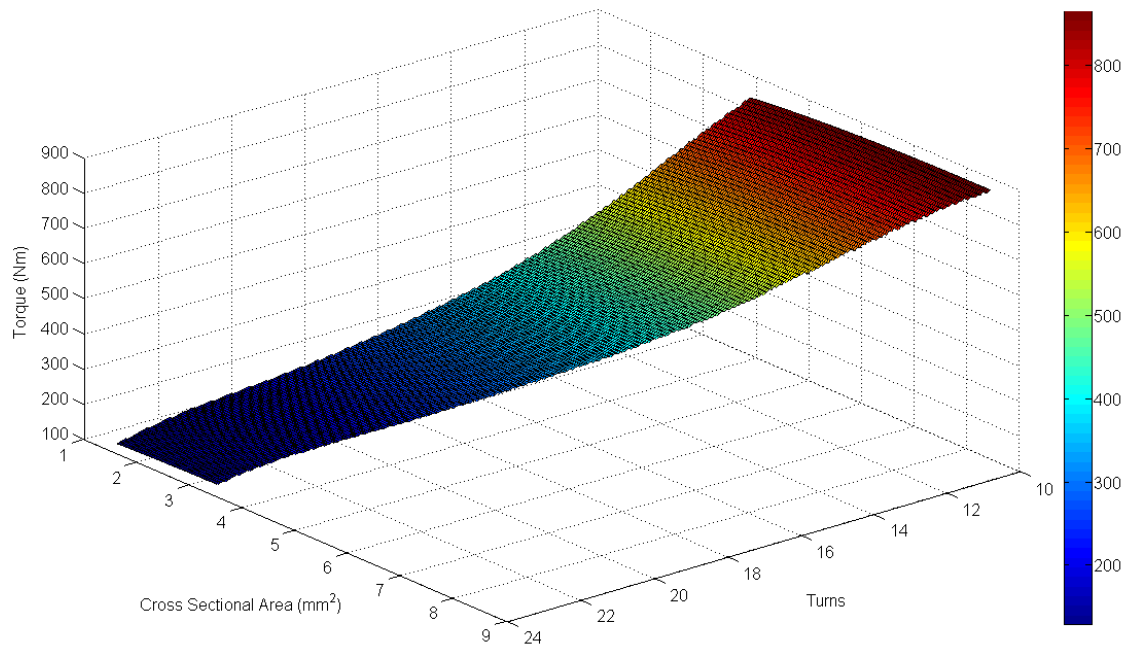


Figure 4.17 Initial three-dimensional torque distribution of stator winding with two design variables.

However, the initial sampling plan is often not very accurate, and at this time the procedure of infilling sampling points is needed. The principle is generally to constrain the boundary of the surrogate model and to try to make the locations of sampling points well-proportioned, which means that infilled sampling points shall be put in obvious blank areas. Based on this principle, another extra 13 sampling points are inserted into the LHS plan for stator winding optimisation, as shown in figure 4.18.

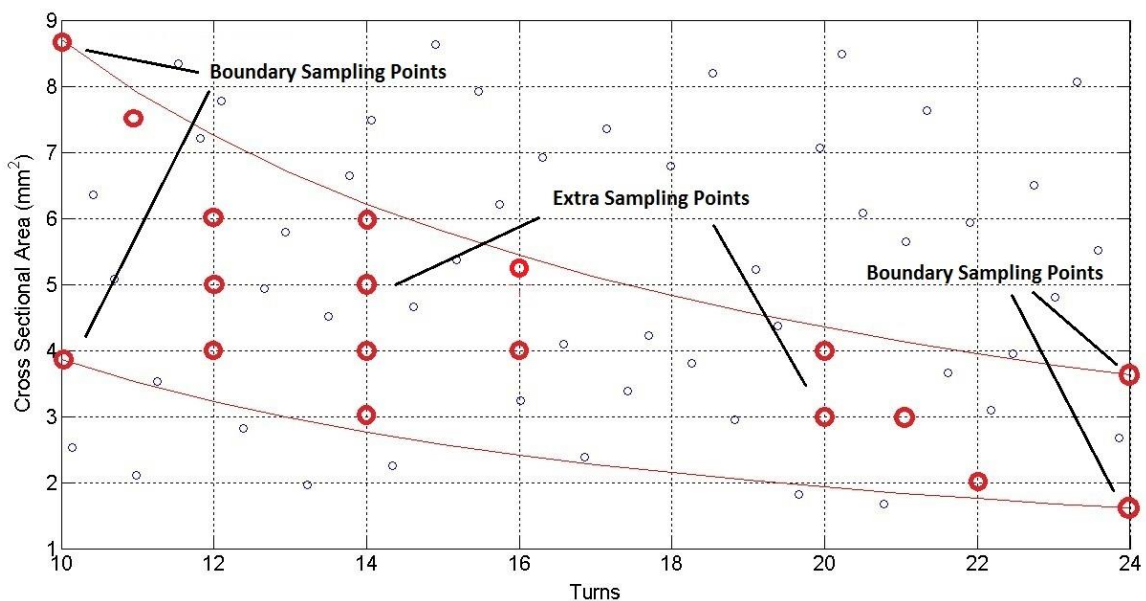


Figure 4.18 Infill sampling points of stator winding optimisation.

Then a new efficiency and torque contour with high precision are built accordingly, as displayed in figures 4.19 and 4.20. Compared to the initial contour, it can easily be seen that the torque contour has scarcely changed; but the efficiency contour appears the wave fluctuation. Now, the surrogate model of stator winding with two variables has already been constructed, which can be searched for the local best point using the PSO method. If the optimal point is not converged when the optimal model is checked for validation, this means that the surrogate model is still not accurate enough, and the ‘best’ point so far will be added into the link of the DoE, in order to repeat the procedures of surrogate model construction until the results are converged, and the local best point has been successfully found.

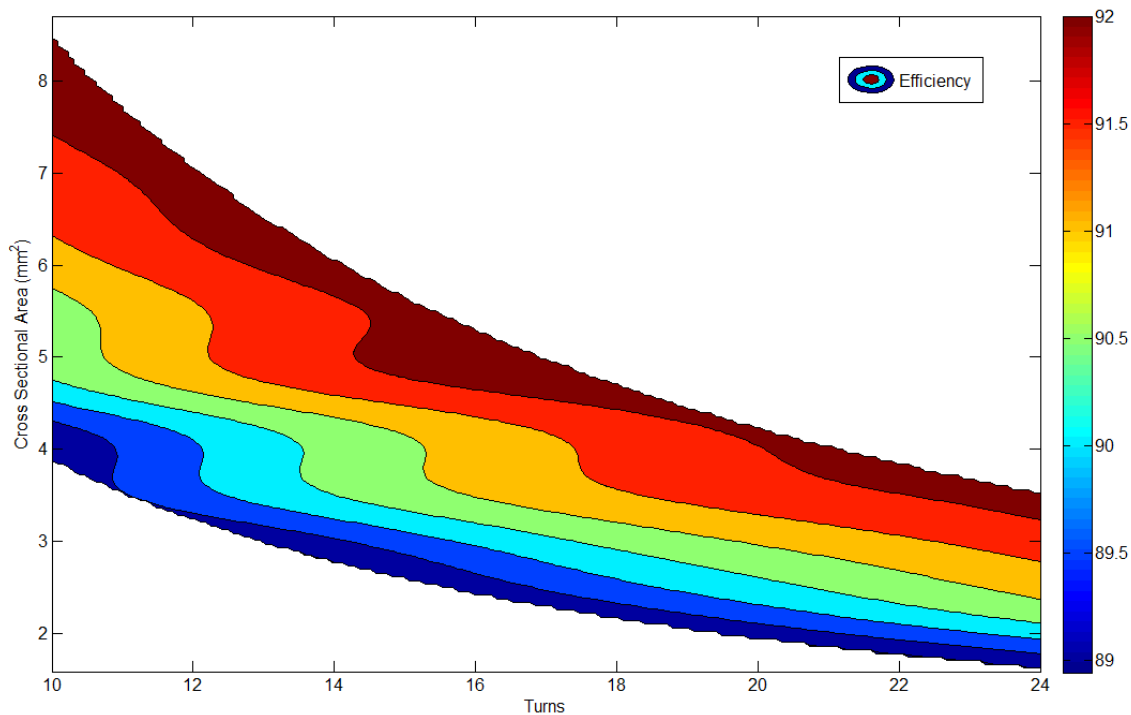


Figure 4.19 Efficiency contour of stator winding with two design variables.

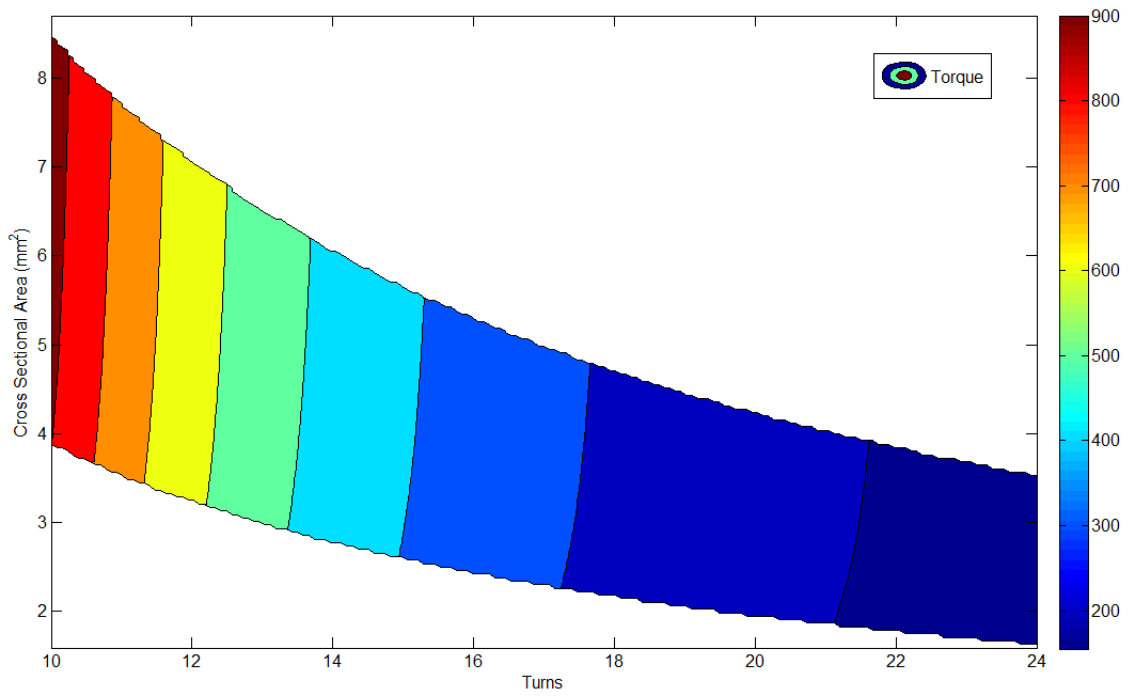


Figure 4.20 Torque contour of stator winding with two design variables.

As in the previous work, the efficiency and torque distribution of stator winding optimisation with two design variables are better shown on 3-dimensional plot, as shown in figures 4.21 and 4.22.

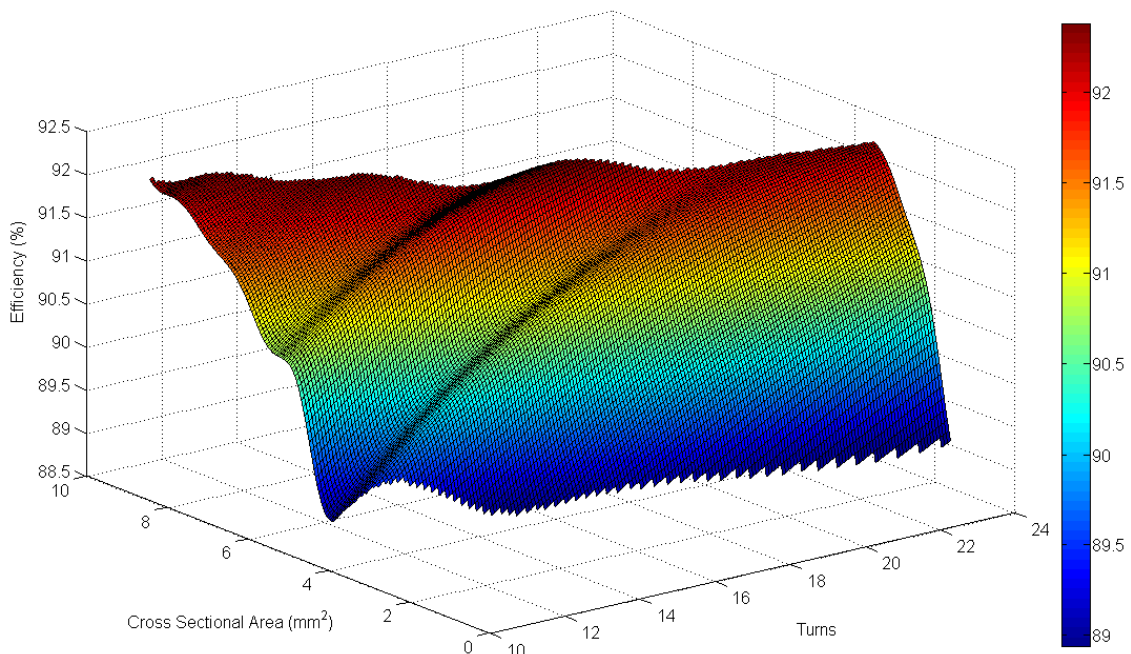


Figure 4.21 Three-dimensional efficiency distribution of stator winding with two design variables.

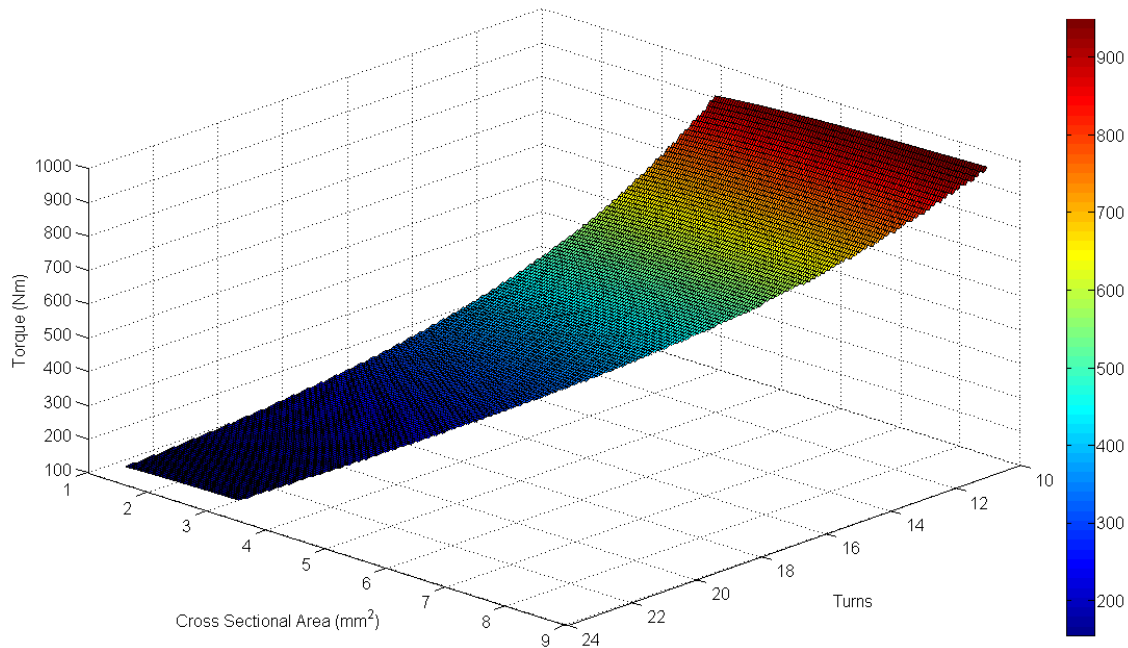


Figure 4.22 Three-dimensional torque distribution of stator winding with two design variables.

#### 4.6.4 Particle Swarm Optimisation

In the previous section on optimisation problem definition, two different constraints are applied due to the installation of a thermocouple. In the PSO, the constraint of maximum fill factor is set to 40% in the thermocouple installed case, which is due to the limitation of the manufacturing process; if the thermocouple is not installed in the stator slot, the upper limit of stator slot fill factor increases to 44%, and other objectives and constraints do not change. The next step is to use PSO to find the best point in this surrogate model of stator winding optimisation with two design variables. In the meanwhile, it has to be mentioned that the optimised winding layout and configuration are kept the same as the original design; they are not changed during the rewinding process.

Therefore, the final best point for stator winding turns and C.S.A with a thermocouple installed is 16 turns and  $4.82 \text{ mm}^2$ . On the other hand, without a thermocouple installed in the stator slot, the best point for stator winding turns and C.S.A is 16 turns and  $5 \text{ mm}^2$  respectively.

#### 4.6.5 Model Validation

From PSO, the two optimisation results are provided with and without a thermocouple installed. In order to verify the precision of the surrogate-based optimised results, finite element software is used to check the machine efficiency with the two optimised design variables. The validation results are illustrated in Table 4.1.

Table 4.1 Model validation of stator winding optimisation

	Stator winding parameter	Fill factor	Validated result
Original design	16 turns 4.29 mm <sup>2</sup>	35.52%	92.9%
Stator rewinding design with thermocouple	16 turns 4.82 mm <sup>2</sup>	39.9%	93.3%
Stator rewinding design without thermocouple	16 turns 5 mm <sup>2</sup>	41.4%	93.5%

Therefore, the optimised model has achieved validation. The SBAO has successfully achieved the optimisation of the stator rewinding.

#### 4.7 Rotor Rewinding Design

As with stator rewinding design, the principles and method are nearly the same for the stator rewinding design. The relevant procedures and results are shown in this section.

##### 4.7.1 Optimisation Problem Definition

The objective here is the same as in stator winding optimisation, apart from some of the constraints being different, due to the different slot area in the rotor. It is impossible to install a thermocouple in the rotor, so the expression for rotor winding optimisation problem definition is listed below.

Objective    Maximise efficiency  $\eta$

Subject to     $20\% \leq ff_{rotor} \leq 39\%$

$$360 \leq T \leq 363 \text{ Nm}$$

$$1.86 \leq A_{rotor} \leq 8.93 \text{ mm}^2$$

$$10 \leq N_{rotor} \leq 24$$

##### 4.7.2 LHS for Rotor Winding Optimisation

Using the same method for stator winding optimisation, the LHS for rotor winding optimisation generates 50 sampling points for two rotor winding design variables: rotor winding turns and C.S.A, as shown in figure 4.23. In figures 4.24 and 4.25, a series of constraints such as the range of two design variables and the rotor slot fill factor are defined. However, the maximum fill

factor of the rotor slot is 39%. Here, the rotor slot fill factor constraint is still set between 20% and 40% during the construction of the surrogate model. Finally, figure 4.26 gives the sampling points available for rotor winding optimisation which will be used to construct the surrogate model of rotor winding optimisation.

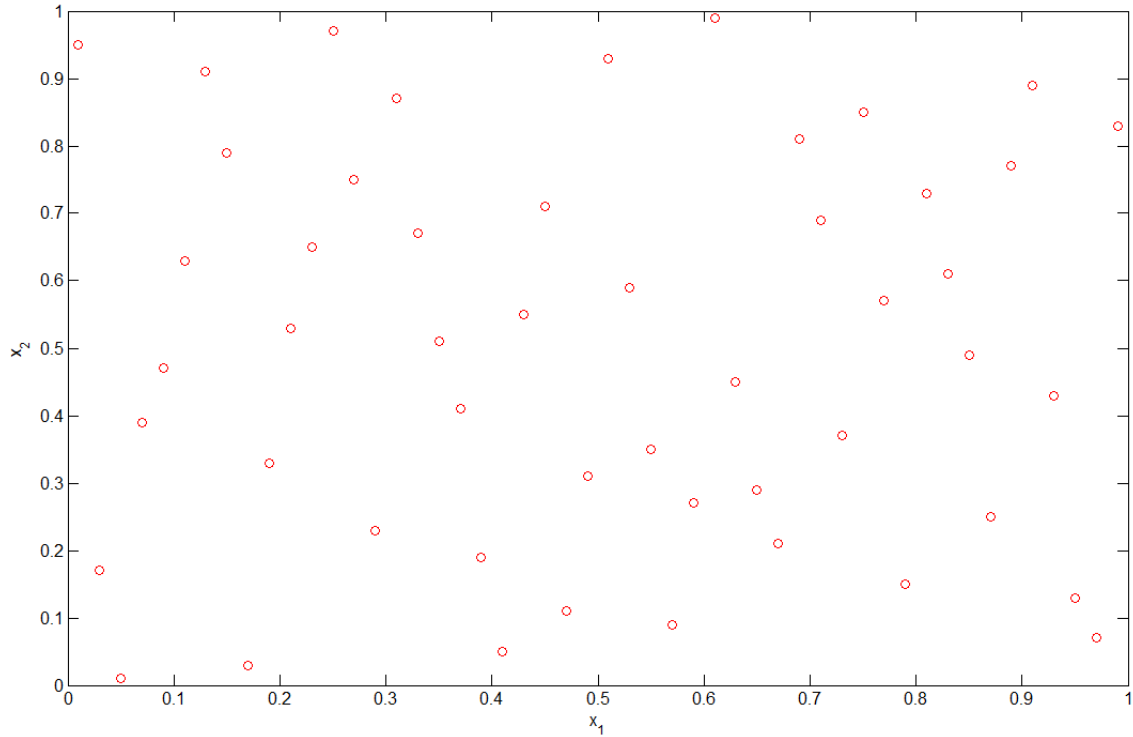


Figure 4.23 Initial Latin hypercube sampling plan for rotor winding optimisation.



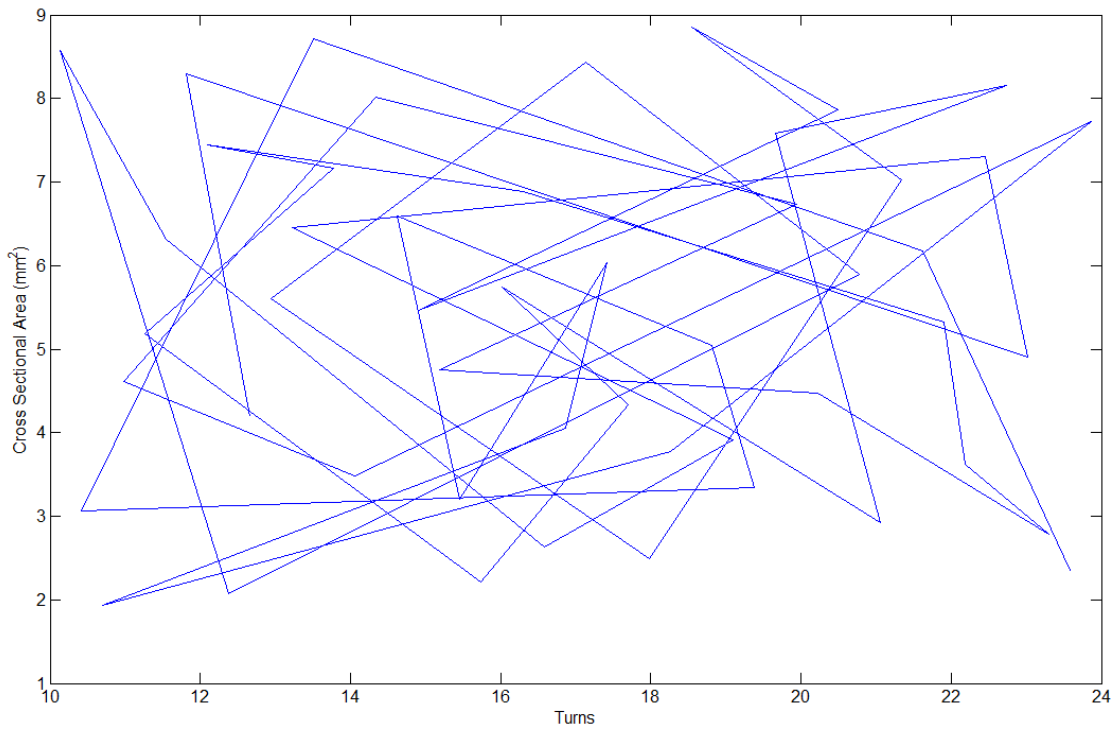


Figure 4.24 Definition of the constraints of rotor winding turns and cross-sectional area.

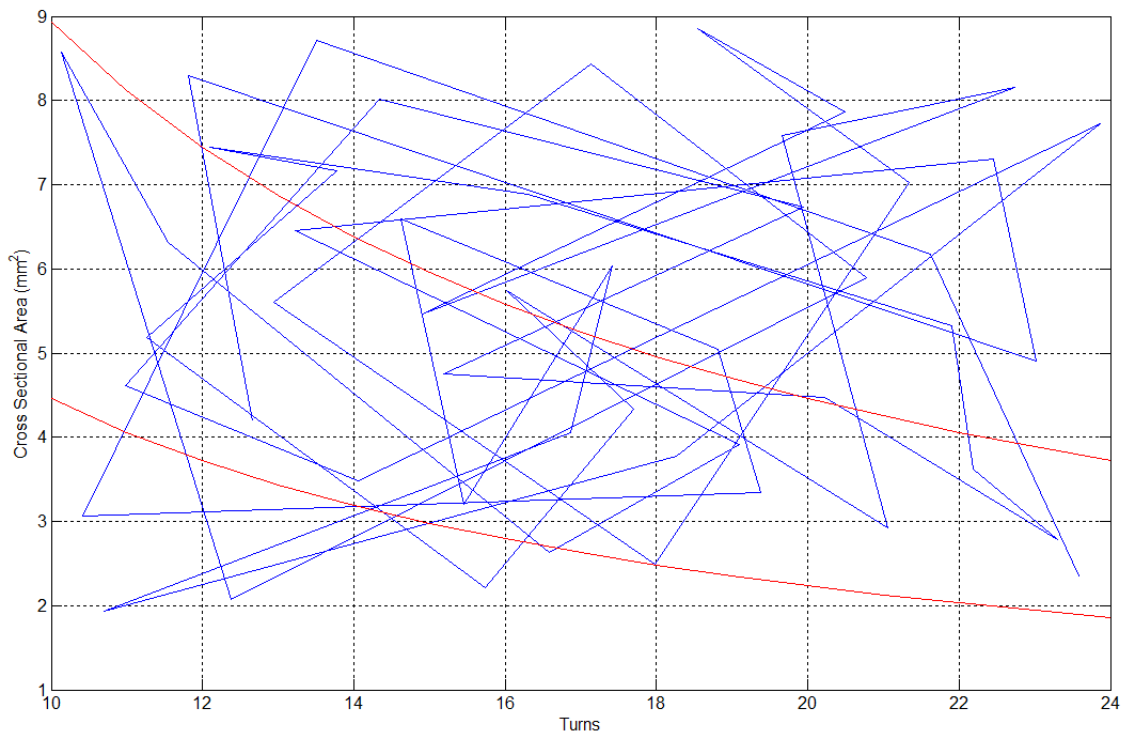


Figure 4.25 Definition of the constraints of rotor slot fill factor.

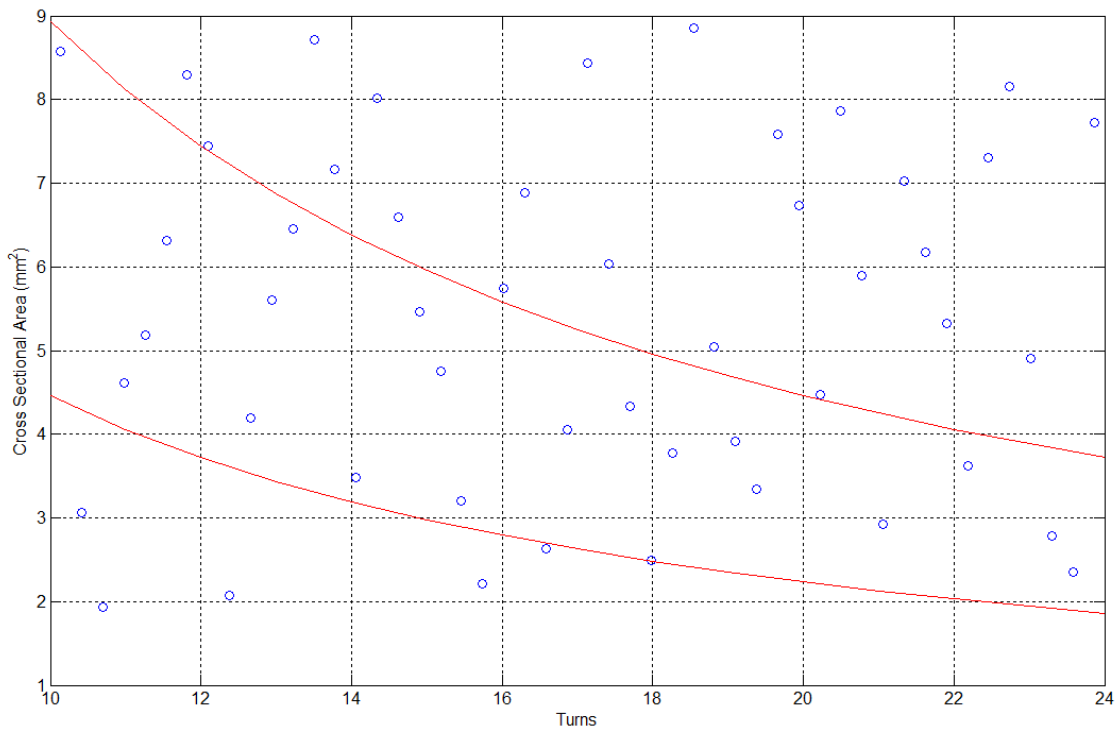


Figure 4.26 Latin hypercube sampling of rotor winding optimisation.

### 4.7.3 Construction of Surrogate Model for Rotor Winding

From the LHS for rotor winding optimisation, 21 available sampling points were found to be used for the initial surrogate model. Figures 4.27-4.30 present initial surrogate model for rotor winding optimisation, showing the initial efficiency contour function, initial torque contour function, three-dimensional efficiency distribution, and three-dimensional torque distribution with two design variables.

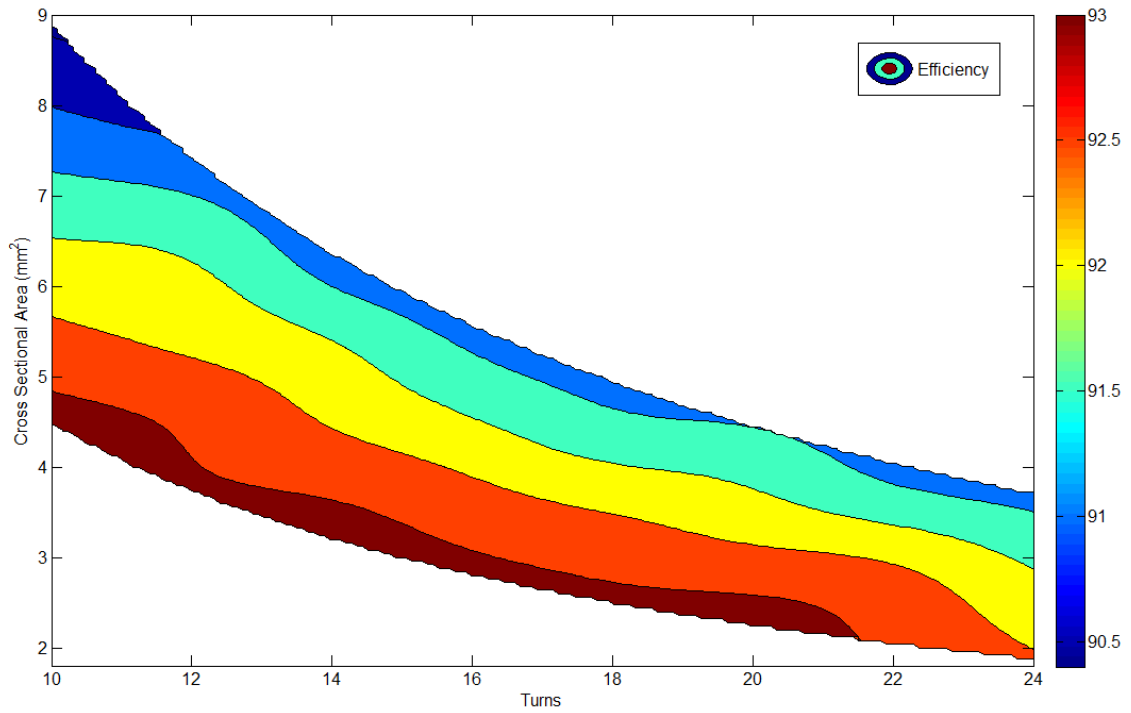


Figure 4.27 Initial efficiency contour of rotor winding with two design variables.

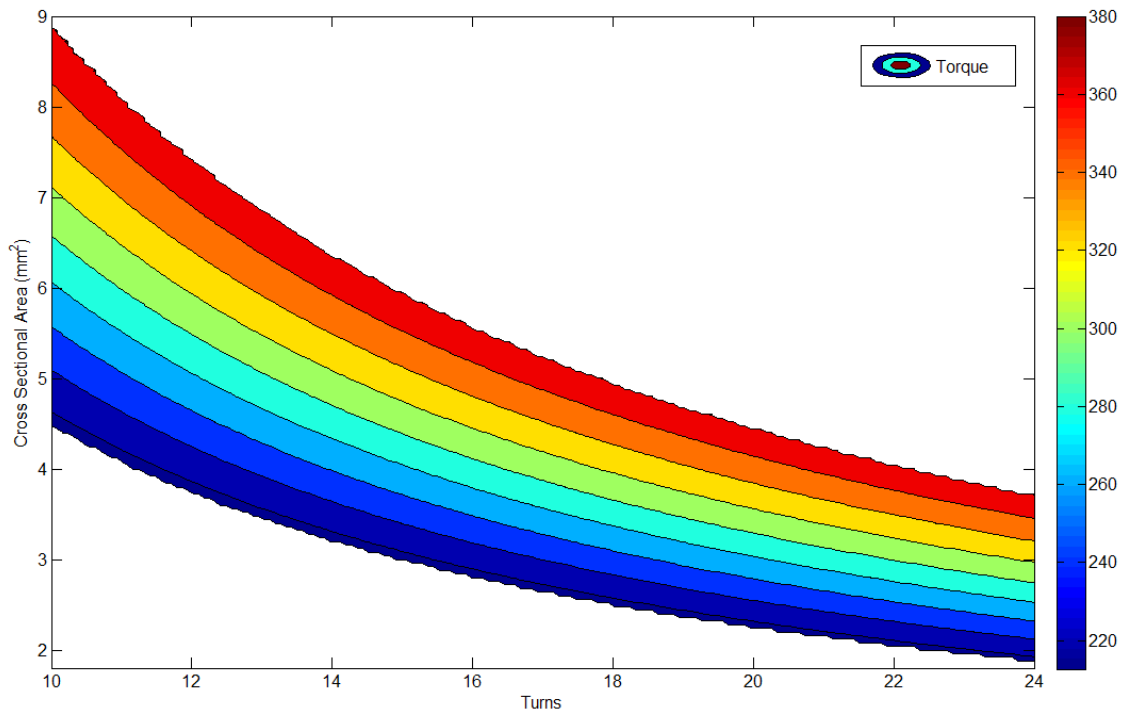


Figure 4.28 Initial torque contour of rotor winding with two design variables.

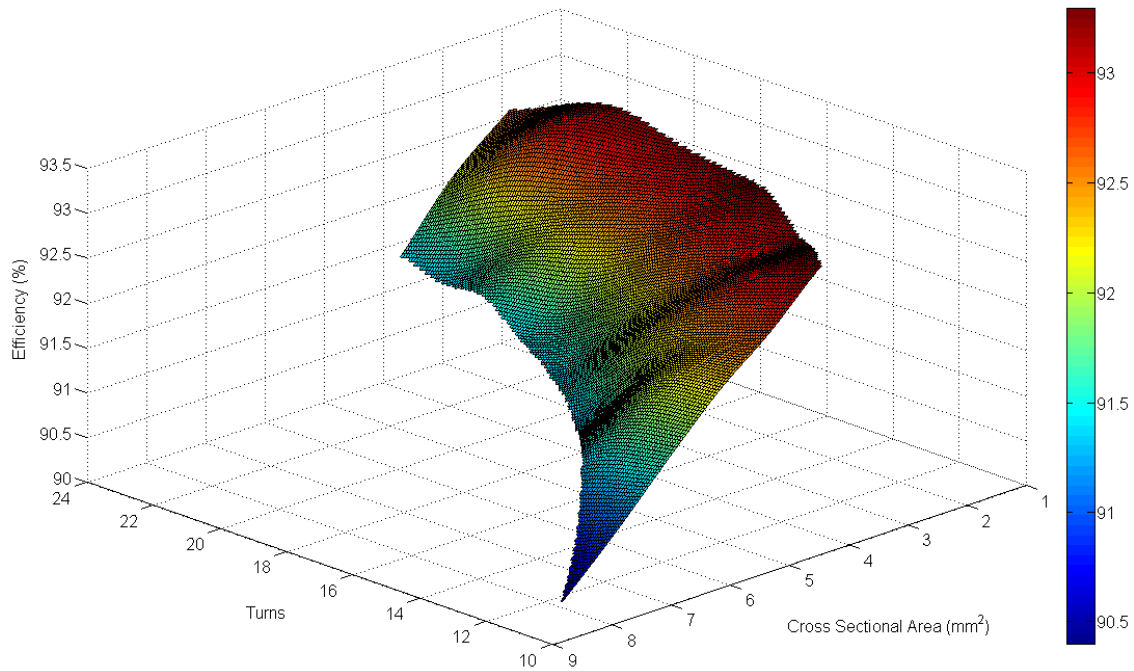


Figure 4.29 Initial three-dimensional efficiency distribution of rotor winding with two design variables.

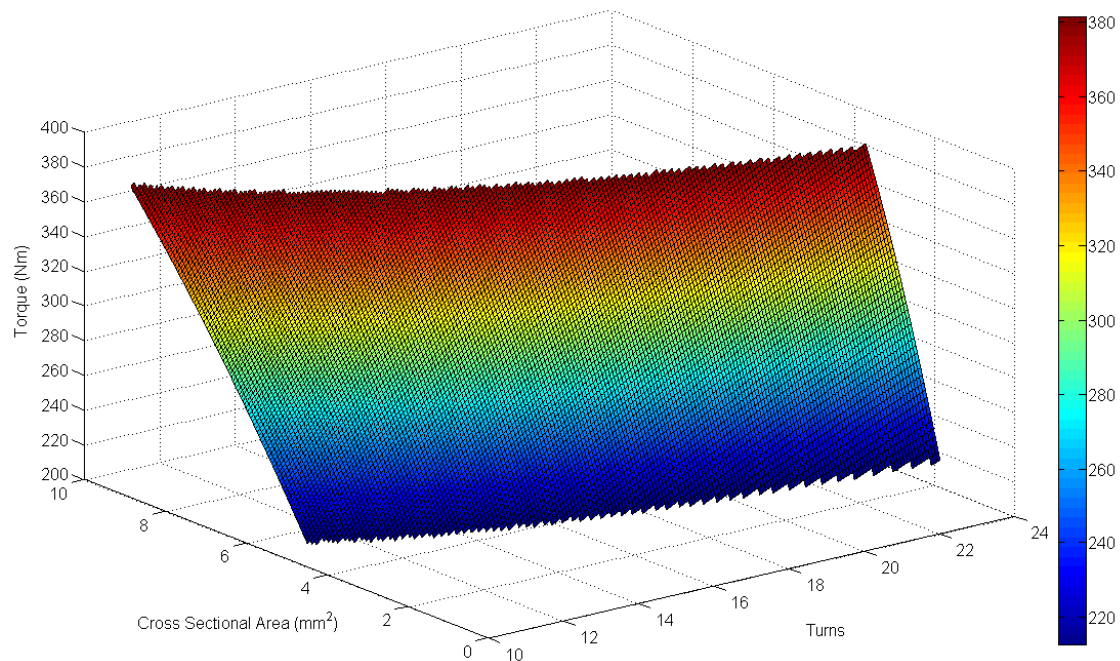


Figure 4.30 Initial three-dimensional torque distribution of rotor winding with two design variables.

In order to make the surrogate model for rotor winding optimisation more accurate, 4 boundary sampling points and 11 extra sampling points are inserted in the LHS of the rotor winding

optimisation via the procedure of infilling sampling points, as shown in figure 4.31. These 15 infill sampling points are run in the finite element software to get further information to estimate precisely the new surrogate model.

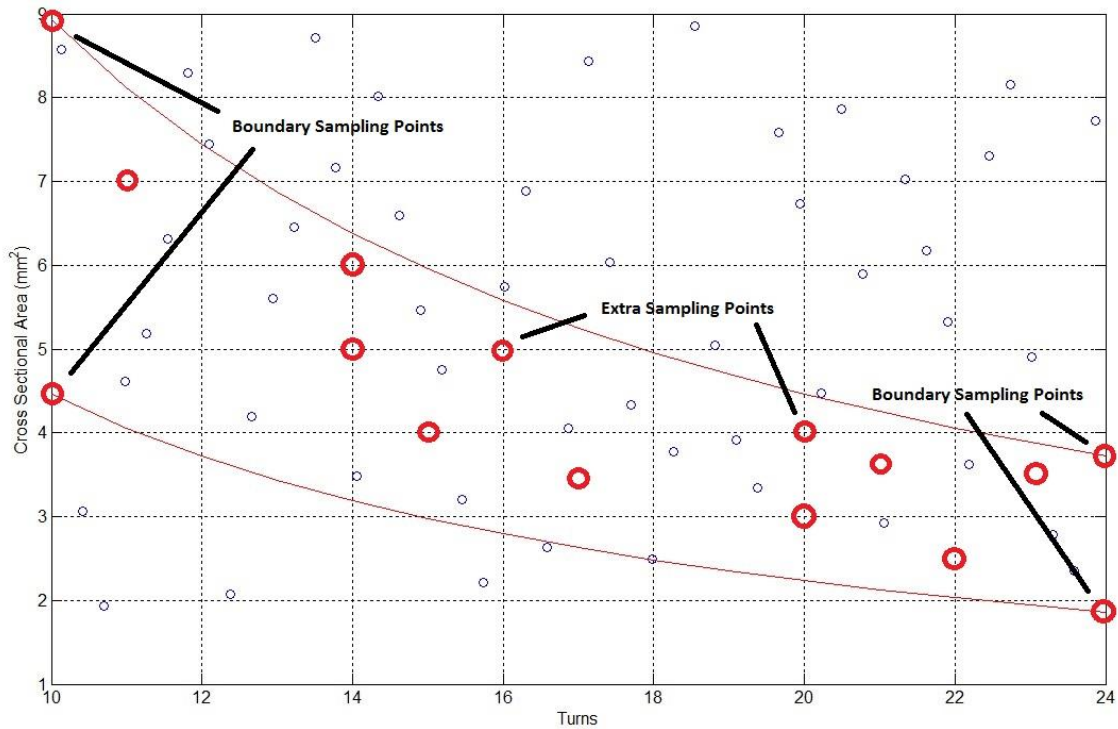


Figure 4.31 Infill sampling points of rotor winding optimisation.

From the infill sampling points, the new surrogate models for rotor winding optimisation, as shown in figures 4.32-4.35 are ready to be validated using the PSO algorithm, and the local peak point can also be found.

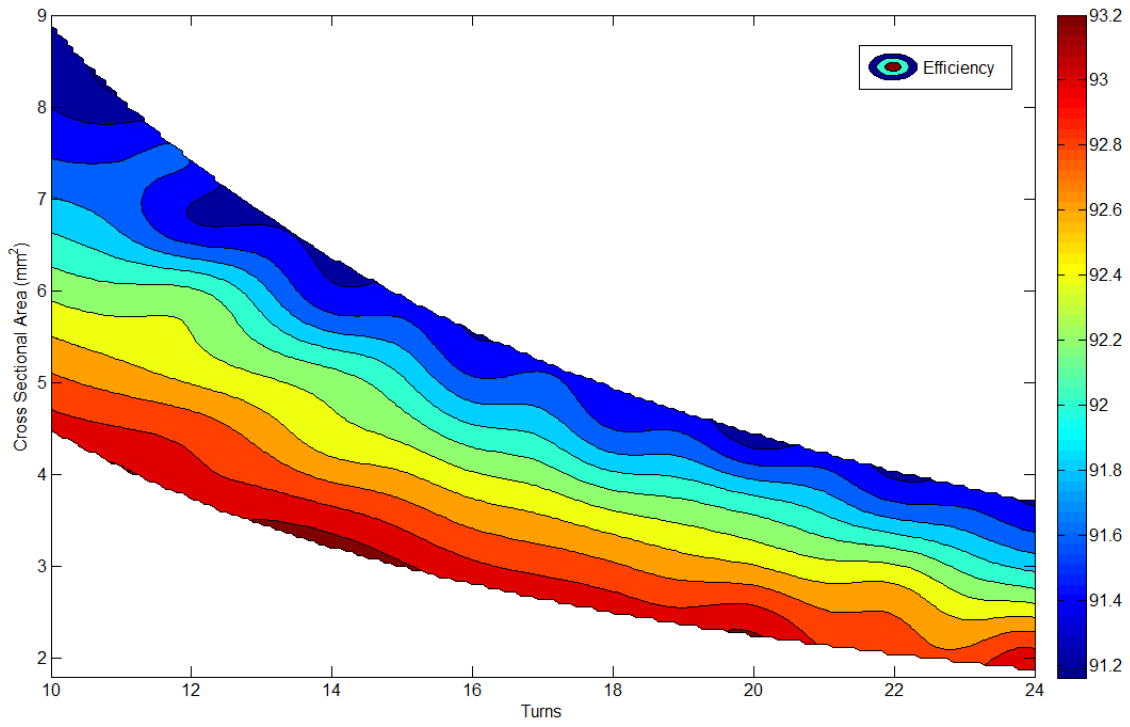


Figure 4.32 Efficiency contour of rotor winding with two design variables.

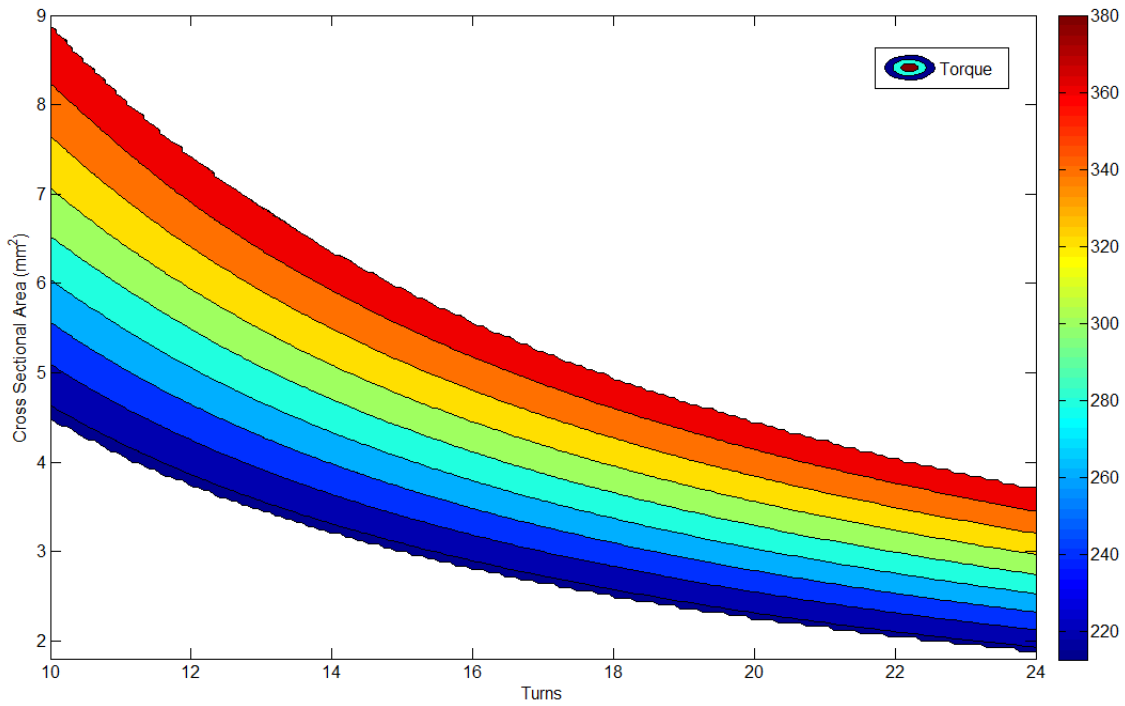


Figure 4.33 Torque contour of rotor winding with two design variables.

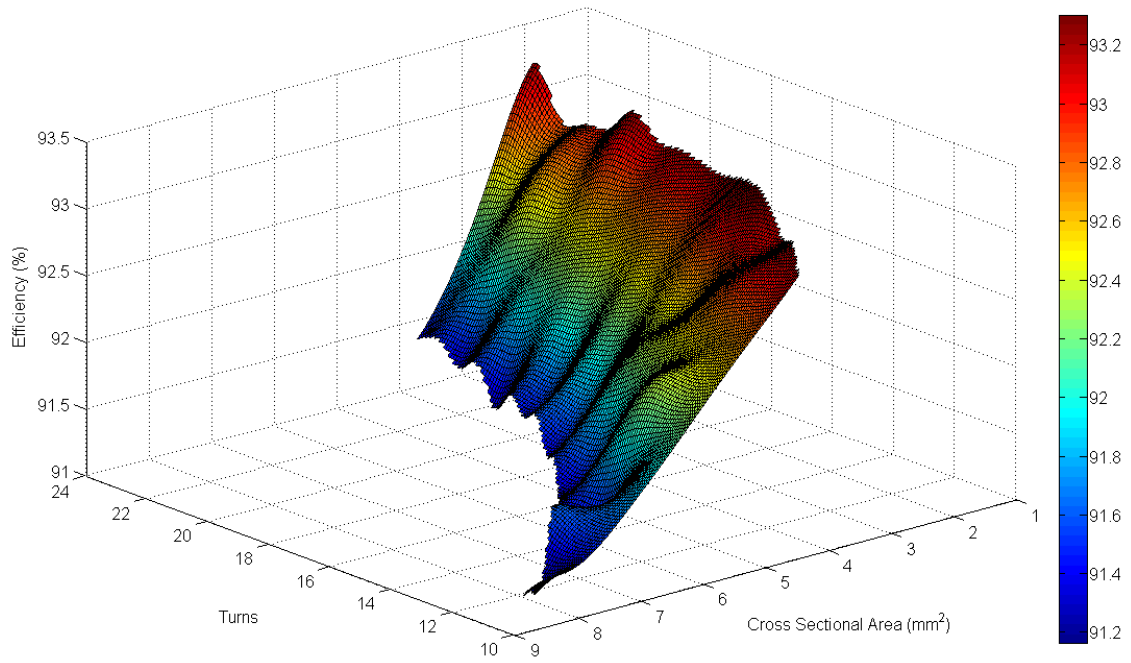


Figure 4.34 three-dimensional efficiency distribution of rotor winding with two design variables.

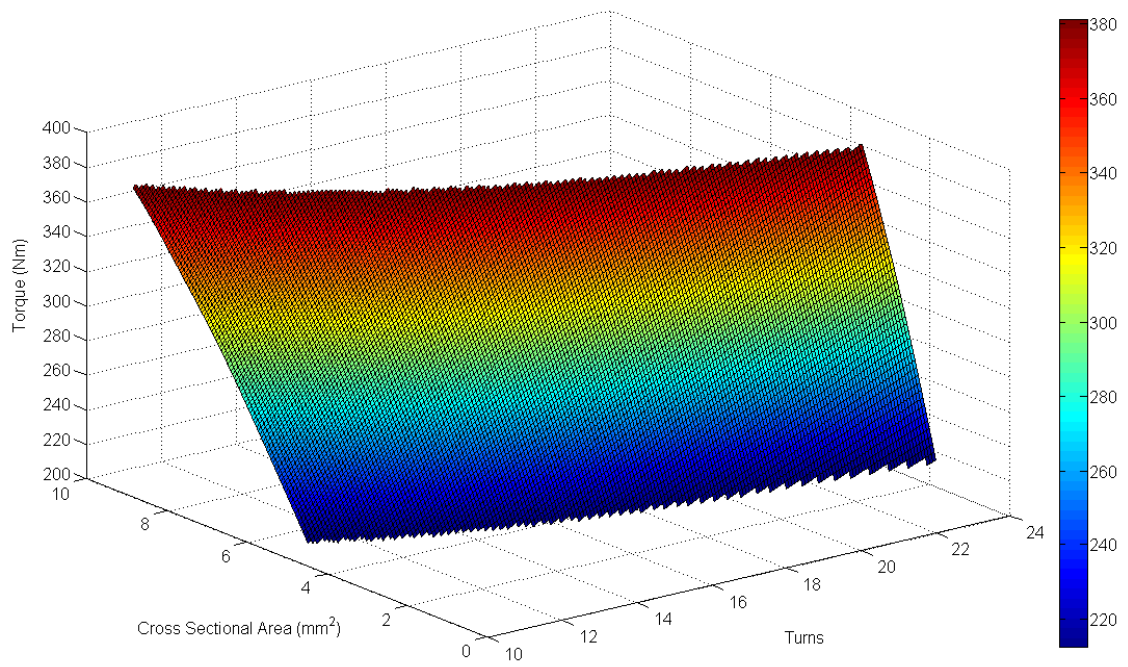


Figure 4.35 three-dimensional efficiency distribution of rotor winding with two design variables.

#### 4.7.4 Particle Swam Optimisation

Before optimisation, the upper constraint of the rotor slot fill factor is altered from 40% down to the actual available value of 39%, because there is no rule in the finite element software to estimate situations which cannot be achieved in the real world. The local peak point for rotor winding optimisation is then provided, where the number of turns is 16 and the C.S.A is 5.19 mm<sup>2</sup> under the condition of unchanged winding layout and configuration.

#### 4.7.5 Model Validation

The final step of rotor winding optimisation is model validation, by feeding the two optimised design variables for rotor winding into finite element software. The validation results are presented in Table 4.2.

Table 4.2 Model validation of rotor winding optimisation

	Rotor winding parameter	Fill factor	Validated result
Original design	12 turns 6.95 mm <sup>2</sup>	37.35%	92.9%
Rotor rewinding design	16 turns 5.19 mm <sup>2</sup>	37.19%	93%

From the stator rewinding and rotor rewinding designs, the feasibility and precision of SBAO has been proven for the electrical machine's winding design. Evidence is also provided about the winding design or redesign, rather than an empirical selection.

#### 4.8 Rewinding Design for Both Stator and Rotor

It has been shown the SBAO is an effective method for the winding design of electrical machines. So, in this section, optimisation is carried out based on the original induction machine with four design variables for both stator and rotor winding. The optimisation procedures are nearly the same as that for two design variables. The first step is to define the optimisation problem. The optimisation of four variables for both stator and rotor winding will then be proven by practical work, and so the upper constraint of the stator slot fill factor has to be limited at 40%, due to the thermocouple being required to ensure the testing precision. The objective of the problem is to maximise efficiency, subject to 9 constraints:

Objective: Maximise efficiency  $\eta$

Subject to:  $20\% \leq ff_{stator} \leq 40\%$

$20\% \leq ff_{rotor} \leq 39\%$



$$358 \leq T \leq 363 \text{ Nm}$$

$$2.98 \leq A_{stator} \leq 7.07 \text{ mm}^2$$

$$2.98 \leq A_{rotor} \leq 7.07 \text{ mm}^2$$

$$8 \leq N_{stator} \leq 24$$

$$8 \leq N_{rotor} \leq 24$$

$$6 \leq J_{stator} \leq 10 \text{ A/mm}^2$$

$$6 \leq J_{rotor} \leq 10 \text{ A/mm}^2$$

where  $J_{stator}$  and  $J_{rotor}$  are the current density of the stator and rotor respectively. The first two constraints are to make sure that the windings can be placed in the slot properly. The third constraint ensures that the machine power rate does not change. The purpose of the last two constraints is to prevent the machine from overheating. The optimisation process determines the following:

- stator and rotor lamination
- air-gap length (0.9 mm)
- slot structure of stator and rotor

The following parameters were variables:

- number of stator winding turns
- stator winding cross-sectional area
- number of rotor winding turns
- rotor winding cross-sectional area

Therefore, this optimisation is a multi-modal and multi-variable problem with four design variables, which means that the LHS and surrogate model is constructed invisible and cannot be expressed in charts. A total of 110 sampling points and an extra 50 infill sampling points are provided by LHS to be used for finding the peak point. Therefore, according to the swarming calculation, the best point is provided as in Table 4.3:

Table 4.3 Optimal plan with 4 design variables compared to the original design

		Turns	C.S.A (mm <sup>2</sup> )
Original machine	Stator	16	4.29
	Rotor	12	6.95
Optimised rewound machine	Stator	14	5.21
	Rotor	10	5.94

As a result, this optimised plan with four design variables (for numbers of turns and cross-sectional areas for both stator and rotor) were adopted to rewind a new machine, and efficiency measurement was conducted on a DFIG test rig. Details are shown in Chapter 6.

#### 4.9 Summary

In Chapter 4 the model of the existing DFIG was presented, keeping the size of the machine structure fixed, and surrogate-based analysis and optimisation were applied to the machine winding re-design and optimisation.

The process of optimisation has been investigated in detail here, and three steps were used in the final optimisation procedure. Design of experiment techniques were presented, whilst one of these – the Latin Hypercube sampling plan was selected to randomly allocate the sampling points, which is not uniform distribution. In the second part, methods of construction of the surrogate model were investigated and compared; the Kriging model was then chosen to construct the surrogate model due to its higher precision. Based on the surrogate model built, an optimisation algorithm was used to find the best location, and in this thesis the particle swarm optimisation algorithm was adopted.

For this novel approach to surrogate optimisation, the optimisation of two variables for either stator winding or rotor winding was investigated, assuming that only part of the winding needs to be repaired or replaced when winding failure occurs in either winding. In addition, the four variable problem has then been extensively optimised for both stator and rotor windings, assuming that all of the generator's windings need to be replaced.

## **Chapter 5 Testing Standards of Doubly Fed Induction Generator**

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Several international testing standards of the polyphase induction machine are compared in this chapter. The American standard IEEE 112-B is carried out in this work due to the higher accuracy compared to the other standards. An improved testing method based on the IEEE 112-B standard is presented to achieve the purpose of doubly fed induction generator testing. The efficiency is determined by the input-output method with loss segregation for sub-synchronous and super-synchronous operational mode; in the meanwhile, the measurement of different losses in machine is separated in detail.

## 5.1 Introduction

Machine losses can usually be either predicted by analytical methods or measured by experiments. The former is usually achieved using FEM to build accurate models and perform electromagnetic analysis. The experimental methods involve three different ways to measure the losses:

- direct measurement of the loss
- direct measurement of the effect of the loss (e.g. calorimetry)
- loss segregation of the input-output method

The induction machine is a mature technology and its performance is now a concern for manufactures, customers, and researchers. There is still no uniform test standard for evaluating machine efficiency, and different standards adopted throughout the world lead to different test results with the same machine. Therefore one is developed here.

Different countries hold their own opinions on the appropriate efficiency test for polyphase induction machines and so several different standards exist. Nearly all the standards fall into the three kinds of test, namely:

- Institution of Electrical and Electronic Engineers (IEEE) 112-B [81]
- International Electrotechnical Commission (IEC) 34-2 [88]
- Japanese Electrotechnical Commission (JEC) 37

Other existing national standards typically resemble these three standards; although in different areas, different standards are adopted. For example, the US National Electrical Manufacturers Association (NEMA) MG-1-1993 standard [89] and Canadian C390-93 [186] are similar to the IEEE standard 112-B in North America. Meanwhile, the European Committee of Manufacturers of Electrical Machines and Power Electronics (CEMEP) and British BS EN 60034-2 standards are analogous to the IEC 34-2.

The primary differences between these standards lie in the accuracy the measurements of loss and efficiency. In order to calculate motor efficiency within 0.5% error, the electrical industry has spent an enormous amount of money working to improve the accuracy of instrumentation [187]. However, it is impossible to acquire an exact value of efficiency with the current standards. At this time, to recognize which standard is more accurate is becoming more important. The major judgment adopted here is to consider the accuracy of loss and efficiency among these test standards.

Efficiency is a measure of the mechanical power which is converted to electrical power by the generator or vice versa by a motor. It is expressed as:

$$\eta = \frac{P_{out}}{P_{in}} = \frac{P_{out}}{P_{out} + P_{loss}} = \frac{P_{in} - P_{loss}}{P_{in}} \quad (5.1)$$

where  $\eta$  is efficiency,  $P_{loss}$  is the total loss in the machine,  $P_{out}$  is output power, and  $P_{in}$  is input power.

This chapter presents an introduction to each individual type of loss in the induction machine. Meanwhile, a brief comparison is presented of the different test standards for induction generators. Also the testing standards used to measure the efficiency of induction generators are described in this chapter. Finally, due to the requirements of the present work, some modifications and supplements are applied to the DFIG test rig, which is based on the current standards for a wound rotor induction generator.

## 5.2 Testing Standards

As introduced in the preceding section, all of the testing standards can be divided into two main forms: the European area and the North American area. In Europe, the British standard BS EN 60034-2 is nearly the same as the European standard IEC 34-2; however, the latter has undergone some modifications in loss determination, and the revised version is called the IEC 61982. In North America, the Canadian C390-1993 national standard corresponds to the American IEEE 112-B, but has a slightly different measurement of windage and friction losses. In the Canadian national standard, windage and friction losses are captured at between 50% and approximately 20% of rated voltage during the no-load test. Furthermore, as the Japanese JEC 37 national standard does not have an English version, so it is not described in this thesis, although the stray load loss (SLL) is completely ignored, and it does not consider the effect of winding temperature on loss calculation. In the following section, the mainstream standards are compared to check their respective precision.

### 5.2.1 Comparison of the Standards

In order to determine which standard has the higher accuracy, many relevant studies have been conducted to verify their reliability. First of all, in comparing the most important worldwide standards, the IEEE 112-B, IEC 34-2, and JEC 37, Renier used the efficiency testing of the 75kW 6 pole induction motor to estimate precision [188]. Figure 5.1 shows that the JEC 37 standard gives the highest value of efficiency, which is about 2% error to the real efficiency

due to neglecting the SLL completely. The measured efficiency of the IEEE 112-B standard is quite close to the theoretical value, so this means the SLL measurement in this standard is more accurate. Although the IEC 34-2 standard considers SLL, it is underestimated and this causes a relatively higher efficiency to be given which is less accurate than the IEEE 112-B standard. Similar work was done by Boglietti in 2003 [189], and the same results for the determination of SLL and efficiency were given when four 10 Hp four pole induction motors were tested using these standards. Because the Japanese JEC 37 standard does not include SLL measurement, so the test results of machine efficiency and losses is not accurate, which means that it is not recommended for practical evaluations of machine efficiency. As a result, the JEC 37 standard is the most inaccurate standard to use in evaluating the efficiency and should be ignored.

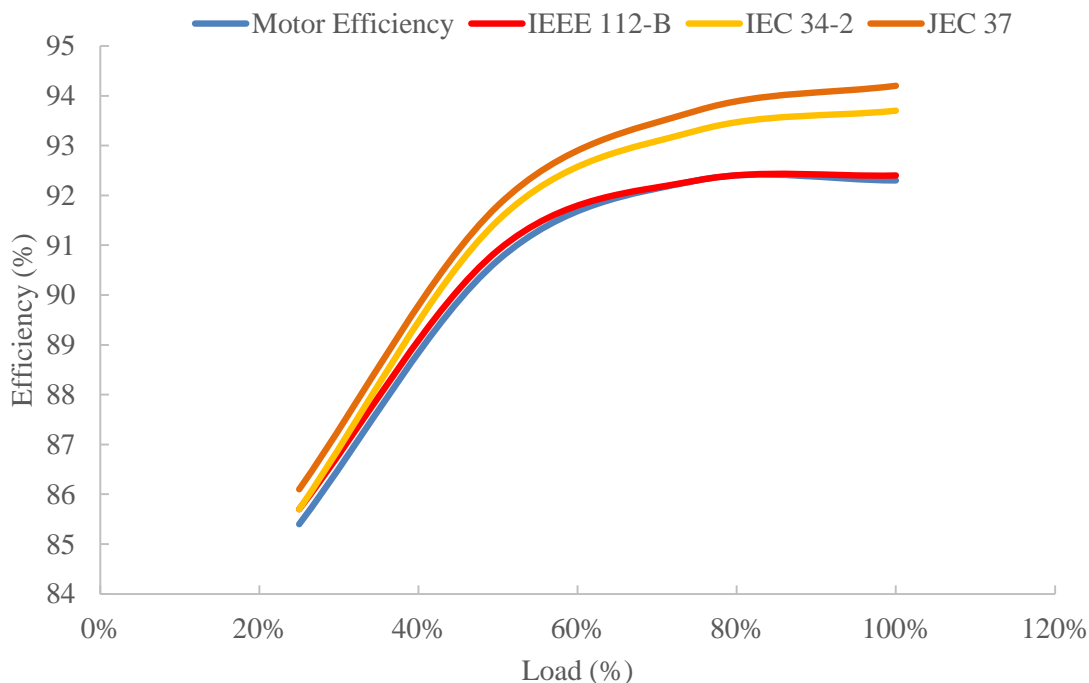


Figure 5.1 Comparison of different international testing standards.

For this reason, more attention is paid to the IEEE 112-B and IEC 34-2 standards. In work comparing these two standards, Roy [190] tested three kinds of induction motors with different power rating, which were 11 kW (7 motors), 55 kW (6 motors), and 75 kW (5 motors). According to the results shown in figure 5.2, the efficiency of the IEC 34-2 standard on the left side was consistently higher than the efficiency values given by the IEEE 112-B standard on the right side by about 1%, due to the error in SLL measurement, except for one 55 kW induction motor. Similar work also in [191-193], has also declared that the IEC 34-2 standard is discredited and inadequate. Therefore, the IEEE 112-B standard is obviously more accurate

than both the IEC 34-2 standard and the JEC 37 standard on the evaluation of efficiency and loss. So, in this work, the IEEE standard 112-B is adopted in the testing method.

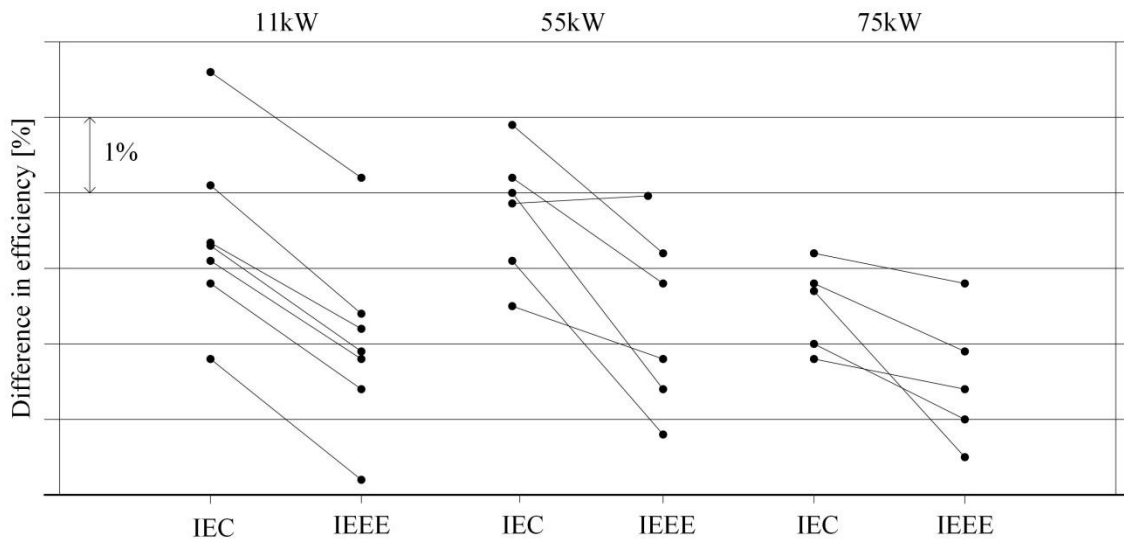


Figure 5.2 Comparison of IEEE 112-B and IEC 34-2 standards [190].

### 5.2.2 IEEE 112-B Standards

The IEEE 112-B Standard was developed by the IEEE Power Engineering Society, which is an American national standard to provide applicable and acceptable tests of polyphase induction motors and generators between 1 and 250 Hp. Currently, almost all tests of medium AC motors are conducted with reference to the IEEE 112-B in the US [187]. In this standard, the main method used to determine efficiency is the input-output measurement with loss segregation. The input power of induction generators is measured according to rotational speed and a torque transducer and output power is captured by a high accuracy wattmeter. So the total loss could be calculated by input power minus output power, which includes conventional losses and SLL. As the conventional losses are segregated, the residual SLL could be determined against torque squared, and linear regression is adopted to reduce the error. Meanwhile, the temperature of the stator and rotor conductors should be corrected based on ambient temperature to precisely calculate total loss and efficiency. The detailed tests are illustrated as follows.

#### 5.2.2.1 Preliminary Test

Commonly, the first step test is to measure the winding resistance. At ambient temperature, the terminal-to-terminal winding resistance is measured for using in the following efficiency test, and meanwhile the structure of winding connection (winding circuits) is taken into consideration. If the thermal detector (PT100 thermistor or thermocouples) is embedded in the machine, the winding temperature could be monitored during the machine's operation, or even

during the machine test. Beside this, the recorded temperature can be used to determine the winding resistance correction under different temperature conditions (where the ambient temperature is measured using the procedure of the IEEE Standard 119-1974). For the detection of winding temperature, three thermal detectors are normally selected to be installed along the coil sides in the stator slot, but in different positions. Two of them are located at the two sides of winding, another is in the middle of the winding. And thus, the average temperature reading of the winding can be calculated by measuring the three different temperatures. Also, the winding resistance at a known temperature can be determined by comparison with the winding resistance at known ambient temperature.

### 5.2.2.2 No-load test

In this test, the induction machine is operated as a motor under the rated voltage and frequency condition without any mechanical load being connected. The purpose of the no-load test is to determine the core loss, windage and friction losses. By adjusting the variac (adjustable voltage source) at rated frequency, the input value of voltage is changed from 125% of the rated voltage down to a lowest point, which will raise the current with further voltage reduction. The test must be run until the bearing loss and winding temperature become stable, in order to read the value of input power, voltage, current, and winding temperature. Total losses in the motor running without load are equal to the measured input power. So, according to this data, the no-load losses can be segregated as stator conductor loss, core loss, windage and friction losses.

To determine the windage and friction losses, first of all, based on the value of input power, minus the stator conductor copper loss ( $I^2R$ ) at all the different voltage points to acquire the summation of core loss, windage and friction losses. Secondly, the curve of power versus voltage squared ( $P_{in} - P_{stator\ copper}$  vs.  $U^2$ ) can be plotted, then select more than three lower points are selected to draw the curve to zero voltage using linear regression analysis. Finally, the windage and friction losses can be deduced as the area where the curve of power versus voltage squared crosses the voltage axis at the zero voltage point.

The core loss is determined by the same principle as in the calculation of windage and friction losses. Subtracting the stator conductor copper loss ( $I^2R$ ) and the value of windage and friction losses from the input power leaves the core loss. Then, the curve of core loss versus voltage is plotted, so that the value of core loss can be expressed at any voltage.



### 5.2.2.3 Load Test

The load test is often used to determine machine efficiency. In this test, the machine is connected to a mechanical load, and supplied at the rated voltage and rated frequency. Meanwhile, the machine is operated with four different load points, which are equally spaced from no less than 25% load to including 100% load (25%, 50%, 75%, 100%); and also two overload points are measured as well, but their loading range is no more than 150% load, so that 120% load and 140% load are usually selected as test points. The test is run until a thermal balance is reached, and then records the data of voltage, current, power, and winding temperature are recorded at each load point, and data of speed and torque are also collected by accurate sensors.

### 5.2.2.4 Data Correction

In order to obtain the highest accuracy of the test in this standard, some data analysis is required to apply a correction based on different temperatures.

- Reference ambient temperature

The ambient temperature is defined as 25°C. If the temperature during the tests differs from the ambient temperature, so the measured performance is corrected based on the ambient temperature.

- Winding resistance correction

The stator winding resistance value at any other temperature is corrected as in the equation 5.2 shown below:

$$R_c = \frac{R_0 (t_c + k_1)}{t_0 + k_1} \quad (5.2)$$

where  $t_0$  is the winding temperature, in°C, as the reference value.

$R_0$  is the winding resistance, in ohms, at temperature  $t_0$ .

$t_c$  is the winding temperature, in°C, for the corrected value of temperature.

$R_c$  is the winding resistance, in ohms, to be corrected at temperature  $t_c$ .

$k_1$  is a constant coefficient, which is 234.5 for 100% IACS conductivity copper or 225 for aluminium.

- Stator winding copper loss correction

When the winding resistance value is corrected at different temperatures, the winding copper

loss ( $I^2R$ ) at the specific temperature could be determined again.

- Slip correction

As mentioned in section 3.3.2 above, the slip has a direct relationship with rotor resistance. As long as the temperature changes, the slip can be corrected with rotor resistance changing.

$$s_c = \frac{s_o (t_c + k_1)}{t_o + k_1} \quad (5.3)$$

where  $t_o$  is the winding temperature, in $^{\circ}$ C, as the reference value.

$s_o$  is the slip, measured at stator winding temperature  $t_o$ .

$t_c$  is the winding temperature, corrected to the value of temperature, in $^{\circ}$ C.

$s_c$  is the slip, corrected at the stator winding temperature  $t_c$ .

$t_c$  is the winding resistance, in ohms, to be corrected at temperature  $t_c$ .

$k_1$  is a constant coefficient, which is 234.5 for 100% IACS conductivity copper or 225 for aluminium.

- Rotor winding copper loss correction

Because the stator winding copper loss correction and slip correction are measured based on the specific temperature, the rotor winding copper loss is determined by equations 3.6 and 3.7.

- Stray load loss correction

Determination of SLL is a function of the residual loss versus torque squared. In order to smooth the curve to linearity, linear regression is used to precisely measure the SLL. The SLL is expressed in equation 5.4.

$$P_{SL} = AT^2 + B \quad (5.4)$$

where  $A$  is the slope.

$T$  is the torque, in Nm.

$B$  is the error, which is the intercept with the zero torque line.

To check the reliability of the SLL function, if the slope is negative or the correlation factor is less than 0.9, the worst point is deleted and the linear regression procedure is repeated. If the value is still negative, the test has to be repeated again. On the other hand, the SLL will be corrected by moving the curve to cross the original point, which means to neglect the error. So the SLL is shown in equation 5.5.

$$P_{SLL} = AT^2 \quad (5.5)$$

### 5.2.3 Improved Testing Method for DFIG

As referred to in the previous section, there are differences in the existing standards in the accuracy of induction generator efficiency. Among these standards, the IEEE 112-B provides relatively more precise measurements of generator efficiency, and it is commonly selected as the global testing standard. However, this standard is generally used for testing conventional polyphase wound rotor induction generators only. However, this thesis focuses on DFIG testing and there is no relevant standard to measure the losses and the efficiency of the DFIG either. So this means that the existing standards cannot satisfy the requirements of this work. Therefore, an approach for testing the DFIG is presented and revised based on the IEEE 112-B standard for this purpose.

The DFIG has two different operational modes: the super-synchronous and sub-synchronous modes. In the super-synchronous mode, the rotor power is fed out from the induction generator to the grid; on the other hand, the rotor power is fed into the induction generator when the DFIG operates in the sub-synchronous mode. The two modes have to be measured and analysed separately, whilst the improved testing method is quite complex and differs from the testing standard for the conventional wound rotor induction generator.

Some parts of the test procedure in the improved testing method are the same as in the IEEE 112-B standard, which involve the preliminary test and the no-load test. In the meantime, the induction machine test is performed by running a motor without any load connection. According to the preliminary test, both stator and rotor winding resistance could be measured to calculate the stator and rotor conductor losses later. And then, the core loss and windage and friction loss are measured separately using the no-load test, and these are used for the determination of efficiency. Furthermore, the input power is measured using rotational speed and torque in both methods.

However, the differences between the improved testing method and the IEEE 112-B standard mainly concern the load test. In the conventional wound rotor induction generator tests based on the IEEE 112-B standard, the total power output is the stator output power, and the rotor conductor loss is estimated by using an indirect method, which is calculated using slip. Both the machine structure and testing procedure are relatively simpler than most for the DFIG, and so some important modifications have to be highlighted during the DFIG testing.

First of all, extra experimental data need to be collected, which is different from the IEEE 112-B standard test on the conventional WRIG. In total five experimental data need to be measured

in detail, as shown in figure 5.3, which is important in precisely determining the DFIG efficiency.

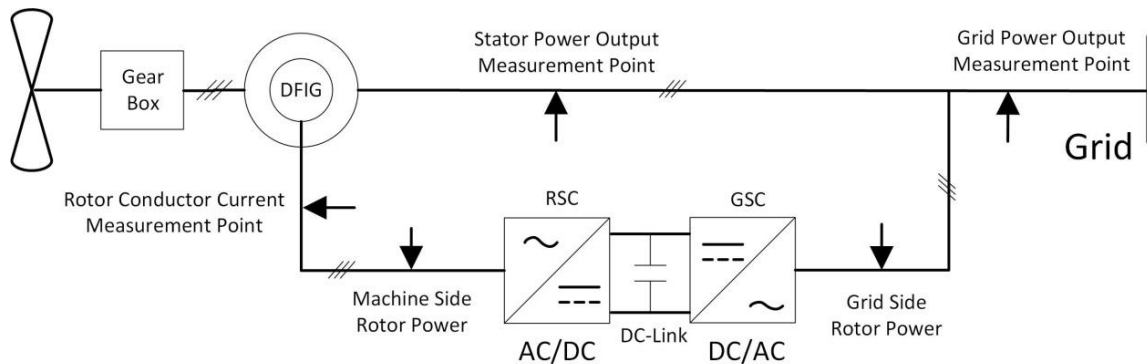


Figure 5.3 Measurement locations for DFIG testing.

- Stator power output:**  
 The power output is generated from the stator of the induction generator, which is used to determine the amount of power output delivered to the grid during operation.
- Grid power output:**  
 Grid power output is the amount of power output delivered to the grid, which is either larger or smaller than the stator power output due to the different operational modes.
- Rotor conductor current**  
 Rotor conductor loss is difficult to determine directly in the WRIG based on IEEE 112-B standard, as the exact value of rotor current cannot be easily obtained. So it has to be determined by an indirect method using slip. But it is quite different in the DFIG, because its rotor is connected to the grid through a DC link to achieve power transmission. So a part of the power will flow through the rotor whether fed in or fed out. The rotor current could be obtained using an accurate current clamp, which means that the rotor conductor loss could be calculated directly. However, the current clamp should be selected carefully, because if the rotational speed of the induction generator is very close to the synchronous speed, the frequency will nearly be the same as the synchronous frequency. Accordingly, in this case, the AC current clamp would not be able to measure the rotor current, where as a DC current clamp could achieve the test's purpose.
- Grid side rotor power**  
 The sum of grid side rotor power and stator power output is the grid side power output. As mentioned above, the stator power output could be measured directly, so the grid side rotor power is simple to calculate.

- **Machine side rotor power**

This part of the power is located between the DC link and the induction generator. Unfortunately, the measuring equipment cannot obtain its value and so it has to be measured by an indirect method. Therefore, the stator power output, grid power output, and efficiency of the DC link is used to calculate the machine side rotor power.

Furthermore, the DFIG test with two different operational modes must be tested separately, due to the requirements of the data analysis. If the DFIG is running in different operational modes, the method of calculating efficiency and power conversion in the induction generator are quite different. The detailed principles of the DFIG for both operational modes are introduced below.

- **Sub-synchronous operational mode:**

When the rotation speed of the induction generator is lower than the rated synchronous speed, the DFIG will operate in sub-synchronous mode, where the rotor power is fed into the induction generator through the DC link. At this time, the stator power output is larger than the grid power output, and is equal to the grid power output plus the grid side rotor power. Therefore, the machine side rotor power can be calculated based on the efficiency of the DC link. A brief summary of power conversion in the DFIG under sub-synchronous operation is illustrated in figure 5.4, showing that the input power and rotor power fed in equals the stator power output and all of the losses in the induction generator.

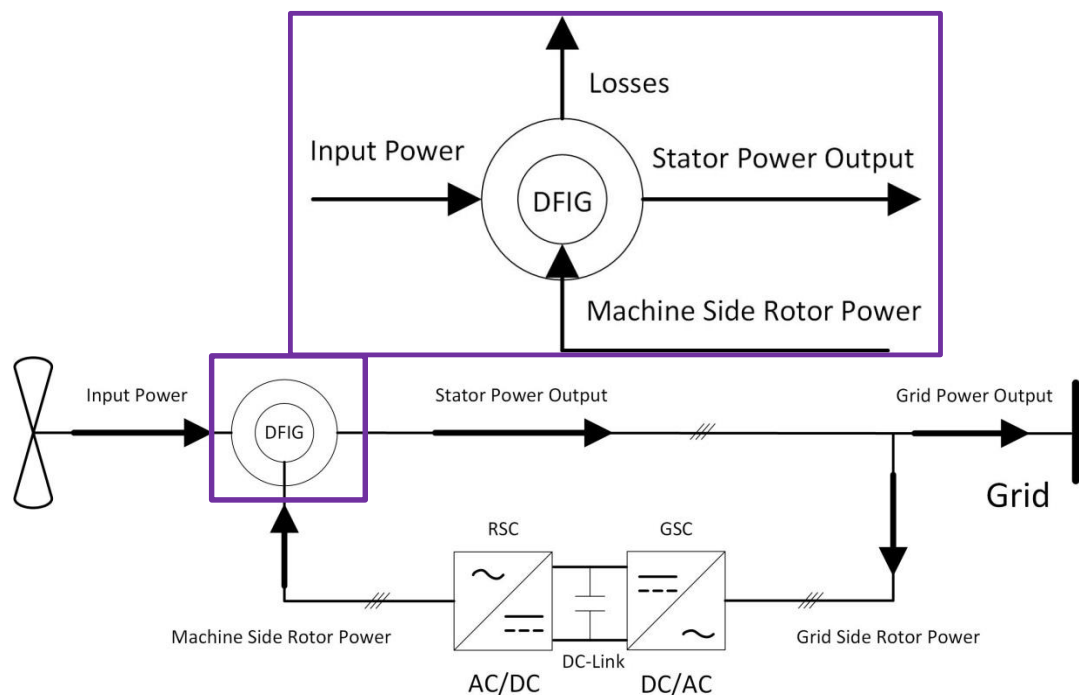


Figure 5.4 Power flow inside DFIG in sub-synchronous mode.

- **Super-synchronous operational mode:**

Super-synchronous mode starts when the rotation speed of the induction generator is higher than the rated synchronous speed, and the rotor power is fed out from the induction generator to the grid. The amount of grid power output equals the amount of stator power output plus the grid side rotor power, because both stator and rotor deliver power to the grid together. The determination of the machine side rotor power is similar to the situation in sub-synchronous operation. So power conversion in the DFIG is slightly different from that in the sub-synchronous operational mode, and is shown in figure 5.5. The input power is now the amount of stator power output, machine side rotor power, and all the losses in induction generator; or it is the amount of grid power output plus all of the losses in the induction generator.

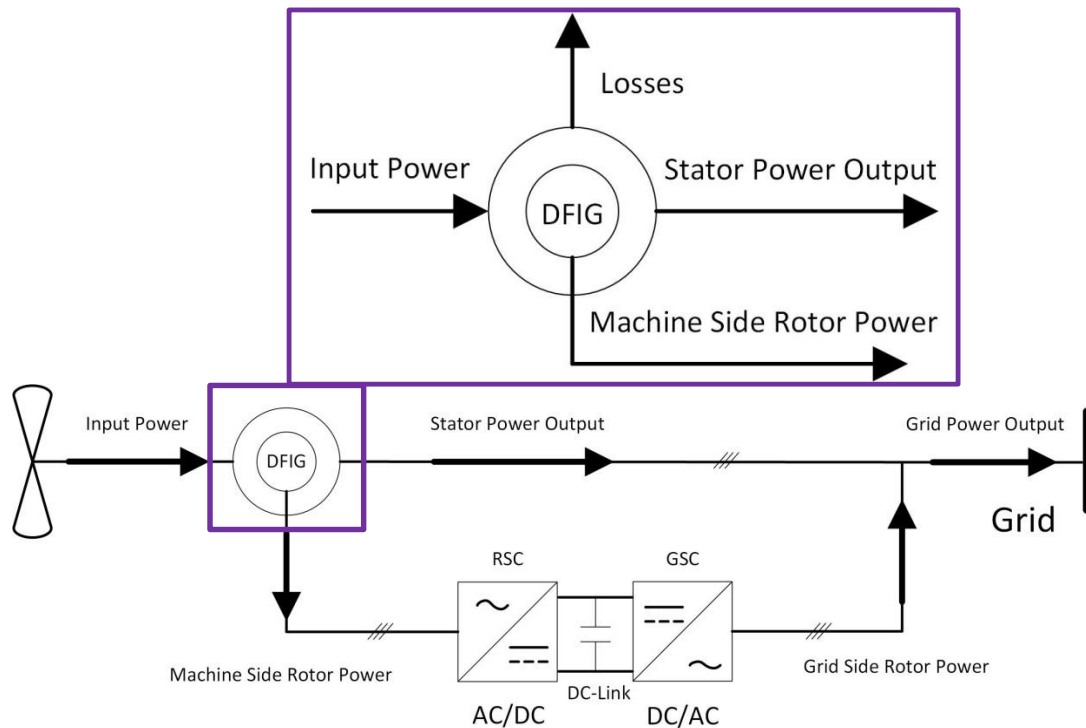


Figure 5.5 Power flow inside the DFIG in super-synchronous mode.

As a result, some measurements and modifications for DFIG testing have been presented based on the IEEE 112-B standard. There is no change to the no-load test, the main work is focused on the section of load test. So in DFIG testing, a lot of extra experimental data needs to be measured, which are not required in conventional WRIG testing. Furthermore as the efficiency of the DFIG is determined based on which operational mode is active, due to the differences in power conversion in the induction generator.

### 5.3 Determination of Efficiency

The determination of efficiency combines the IEEE 112-B standard and the improved test method to achieve an accurate measurement. All experimental data was collected with the induction machine operating either as a motor or as a generator. The input-output method was selected with loss segregation to distinguish all the losses in the induction generator into their individual components such as stator and rotor conductor loss, core loss, windage and friction losses, and SLL. The sum of these losses is the total loss and output power is found by subtracting the total loss from the input power. A curve of SLL is plotted versus torque squared. In order to reduce the error in the measurements and obtain the accurate curve of SLL, linear regression is adopted. Importantly, the temperature must be recorded in any test of this work, which is going to be used on data correction to make sure the experiment with high precise. The following section describes the detailed procedure for efficiency determination.

#### 5.3.1 Resistance Measurement

The winding resistances of both the stator and rotor in the induction machine are too small to be measured precisely, so to achieve more accurate measurements, a Kelvin Bridge was adopted to measure winding resistance. The Kelvin Double Bridge is generally used to measure resistance below 1 Ohm. The principle of the Kelvin Double Bridge is quite similar to that of the Wheatstone bridge, and its circuit diagram is shown in figure 5.6.

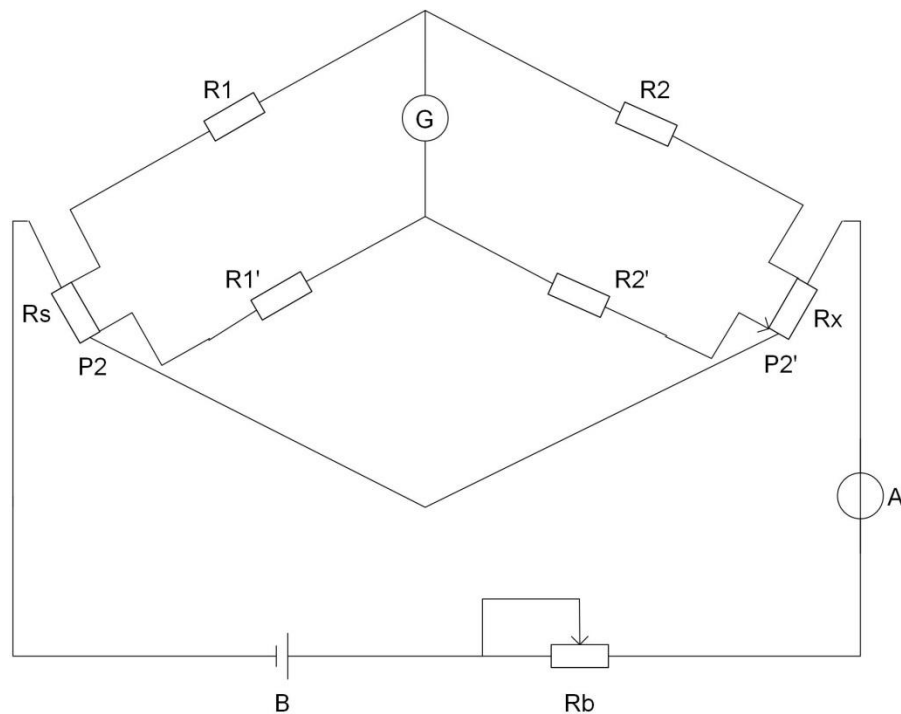


Figure 5.6 Diagram of Kelvin Double Bridge.

In the circuit, two additional resistors  $R_1$  and  $R_2$  are connected to the four different terminals  $R_S$  and  $R_X$ , where  $R_X$  is the unknown resistor and the target to be tested, and  $R_S$  is the standard resistor whose value is known. Usually, the Wheatstone bridge is comprised of  $R_1$ ,  $R_2$ ,  $R_S$ , and  $R_X$ . But a parasitic resistance between  $R_S$  and  $R_X$  is included in the relevant measurement of the circuit, which can affect the testing accuracy. To overcome this problem, the concept of second arms of the bridge is presented by using a second pair of resistors  $R'_1$  and  $R'_2$ , which are connected to the inner terminals of  $R_S$  and  $R_X$ . Furthermore, the galvanometer is located between the junctions of  $R_1R_2$  and  $R'_1R'_2$ . When the galvanometer reads zero, the ratio of the resistors has reached a balance condition, which is expressed in the following equation:

$$\frac{R_X}{R_S} = \frac{R_2}{R_1} \quad (5.6)$$

So the unknown resistance is calculated from the balance equation as:

$$R_X = R_S \times \frac{R_2}{R_1} \quad (5.7)$$

Therefore, if the ratio is the same, this means that the error is quite small, and the test results are very precise. So in practice, the aim is to make the error as small as possible, and then to take the resistance reading as the winding resistance.

As mentioned above, when the induction machine is standstill at ambient temperature, the winding resistances are measured and recorded using the Kelvin Double Bridge as well as the ambient temperature.

### 5.3.2 No-load test

The purpose of the no-load test is to determine the core loss, windage and friction losses. In the no-load test, the induction machine operates as a motor at the rated voltage and frequency without any load connected to the rotor. Decreasing the voltage from 125% of the rated level to the point where the rotational speed shows a significant change, which is approximately 30% of rated voltage in general. In the meantime, the information of temperature, voltage, current, and power input at rated frequency must be recorded.

#### 5.3.2.1 Windage and Friction Loss Determination

During the no-load test, the input power of the induction motor is mainly consumed by stator conductor loss, core loss, and windage and friction losses. Due to the very small rotor current,



rotor conductor loss can be neglected. So the input power in the motor in the no-load condition equals the total losses, which consist of stator conductor loss, core loss, and windage and friction losses.

$$P_{in} = 3I_{phase}^2 R_s + P_{core} + P_{WF} \quad (5.8)$$

To determine the windage and friction loss, firstly the stator conductor loss is subtracted from the input power, so the rest of losses are the core loss and windage and friction loss, due to the stator conductor loss could be measured directly, which can be shown in the following equation.

$$P_{in} - 3I_{phase}^2 R_s = P_{core} + P_{WF} \quad (5.9)$$

So the power curve versus voltage squared is plotted in figure 5.7, to determine the windage and friction loss. Linear regression analysis is then used by three or more lower points to extend the curve to zero voltage. The intercept distance with the zero voltage axis is then the windage and friction losses.

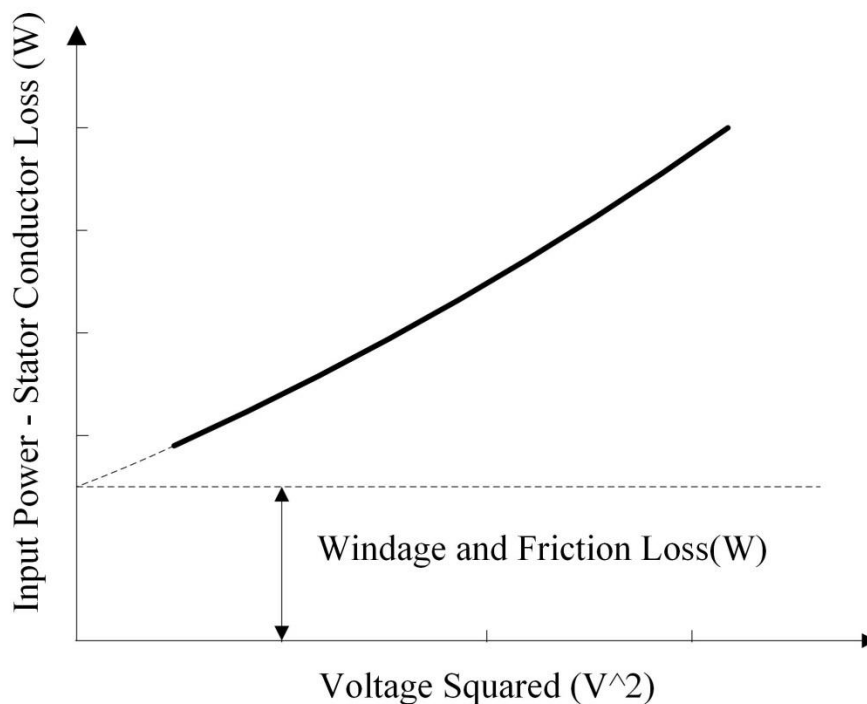


Figure 5.7 Determination of windage and friction Loss.

### 5.3.2.2 Core Loss Determination

Windage and friction losses are determined by a linear regression analysis, as detailed in section 3.3.3. So the core loss is equal to the input power minus the stator conductor loss and windage and friction losses, as shown in the following equation.

$$P_{in} - 3I_{phase}^2 R_s - P_{WF} = P_{core} \quad (5.10)$$

The power curve of core loss versus voltage is plotted, as shown in figure 5.8, and thus the value of core loss at any voltage can be obtained directly.

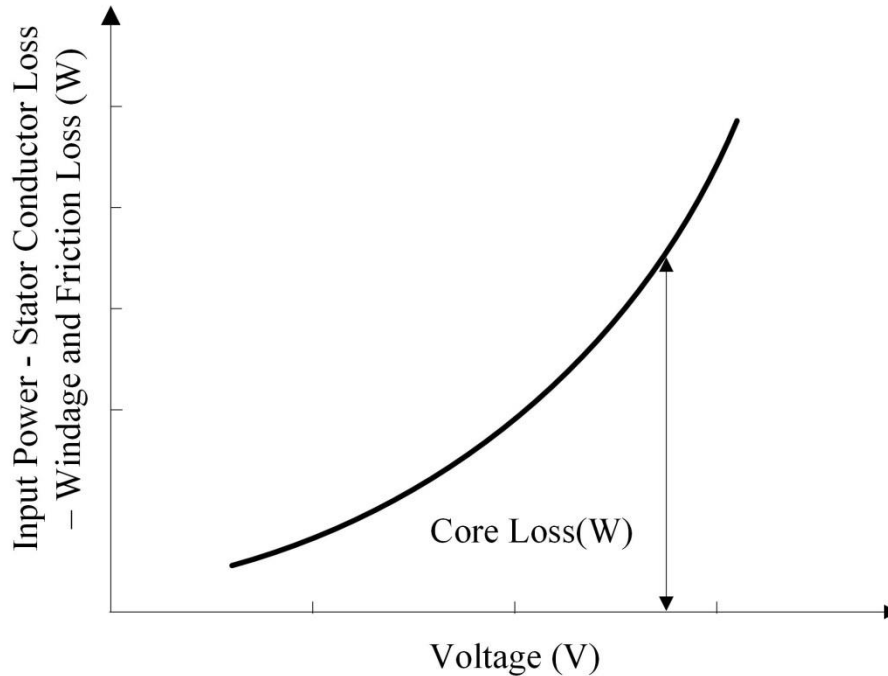


Figure 5.8 Determination of core loss.

### 5.3.3 Load Test

To determine the generator efficiency and SLL, a load test is required. Load points are selected between approximately 25% and 100% of full load, and it is recommended in the IEEE 112-B standard to select four equally spaced load points in this range, because it is necessary to measure efficiency precisely to cover the entire load range of the induction generator. Even more load points can be selected if desired. The test starts at the highest load and proceeds down to the lowest load. Furthermore, it is most important in the load test to record the temperature, due to the correction is needed to ensure the precision of the test. Finally, speed, torque, power output, current, voltage, and temperature must be measured at each load point.

However, the principle of the operation of the DFIG is more complex than that of the conventional WRIG, and in order to obtain accurate efficiency assessments, the two different operational modes of the DFIG have to be analysed separately in determining efficiency and SLL.

The operational modes and power signs of the DFIG are shown in Table 5.1.

Table 5.1 Operational speed modes and power signs of DFIG

Slip	Operational Mode	$P_{in}$	$P_{stator}$	$P_{rotor}$
$0 < s < 1$	Sub-synchronous	$< 0$	$> 0$	$< 0$
$s < 0$	Super-synchronous	$< 0$	$> 0$	$> 0$

### 5.3.3.1 Sub-synchronous Operational Mode

Figure 5.9 shows that when the DFIG operates under in the sub-synchronous operational mode, the rotor power is fed into the induction generator.

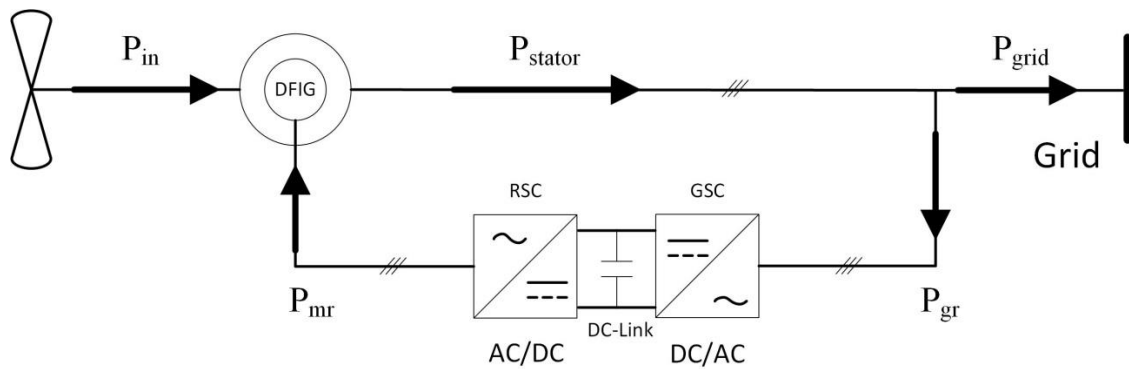


Figure 5.9. Diagram of DFIG in sub-synchronous mode.

The total input power  $P_{in}$  in the system is produced by torque  $T$  and rotational speed  $\omega$ , as defined in the equation:

$$P_{in} = \omega T \quad (5.11)$$

The power delivered to the grid  $P_{grid}$  is less than the stator power output  $P_{stator}$ , because part of the power is fed back into the induction generator. This is called the grid side rotor power  $P_{gr}$ . However, the grid side rotor power cannot be fully fed back to the induction generator, because the DC link causes slight losses too. In this project, the efficiency of rotor converter in the DC link is approximately 95%, which is provided by the manufacturer. So the machine side rotor power  $P_{mr}$  is 95% of the grid side rotor power. Therefore, the power balanced equation in the induction generator can be calculated as in the following equation.

$$P_{in} = P_{loss} + P_{stator} - P_{mr} \quad (5.12)$$

The total losses in the sub-synchronous mode can be expressed as follows:

$$P_{loss} = \omega T + P_{mr} - P_{stator} = \omega T + 0.95 \times P_{gr} - P_{stator} \quad (5.13)$$

$$P_{loss} = \omega T + 0.95 \times (P_{stator} - P_{grid}) - P_{stator} \quad (5.14)$$

So the efficiency of the DFIG under the sub-synchronous operation using the input-output method with loss segregation can be expressed as the following:

$$\eta = \frac{P_{grid}}{P_{grid} + P_{loss}} = \frac{P_{grid}}{P_{grid} + \omega T + 0.95 \times (P_{stator} - P_{grid}) - P_{stator}} \quad (5.15)$$

The total losses  $P_{loss}$  consist of the stator and rotor conductor losses, core loss, windage and friction losses, and SLL. So the SLL is calculated separately at each load point by subtracting the stator and rotor conductor losses, core loss, and windage and friction losses, as shown below:

$$P_{SLL} = P_{loss} - 3I_s^2 R_s - 3I_r^2 R_r - P_{core} - P_{WF} \quad (5.16)$$

$$P_{SLL} = \omega T + 0.95 \times (P_{stator} - P_{grid}) - P_{stator} - 3I_s^2 R_s - 3I_r^2 R_r - P_{core} - P_{WF} \quad (5.17)$$

where  $I_s$  and  $I_r$  are the stator and rotor current respectively, and  $R_s$  and  $R_r$  are the stator and rotor winding resistance. Now the value of SLL at different load points is acquired, and the curve of smoothed SLL versus torque squared is plotted using linear regression analysis. The function of SLL is expressed as:

$$P_{SL} = AT^2 + B \quad (5.18)$$

where  $T$  is the torque in Nm,  $A$  is the slope, and  $B$  is the error at the intersect with the zero torque line. The final step is to validate the function of SLL. If the slope is negative, so the worst point shall be deleted and the procedure of linear regression is repeated. If the value is still negative, the test is unsatisfactory. On the other hand, the SLL can be corrected by moving the curve to cross the original point, which means to neglect the error. So the corrected function of SLL goes through the original point, and the corrected equation 5.19 is used to determine the corrected value of SLL  $P_{SLL}$  for each load point.

$$P_{SLL} = AT^2 \quad (5.19)$$

### 5.3.3.2 Super-synchronous Operational mode

With increasing rotational speed, the operational mode of the DFIG changes from sub-synchronous to super-synchronous. Now the rotor power is no longer fed into the induction generator, but on the contrary is fed out from the induction generator to the grid through the DC link. Figure 5.10 illustrates the super-synchronous operational mode of the DFIG.

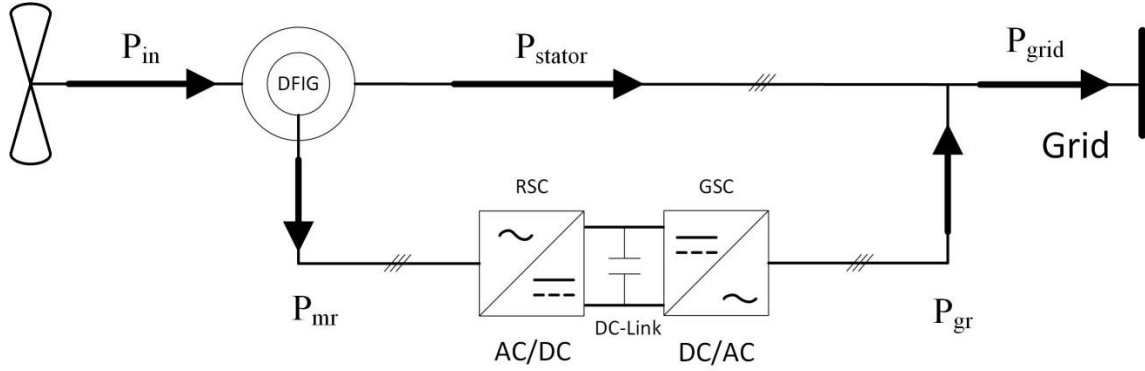


Figure 5.10 Diagram of DFIG in super-synchronous mode.

Because the rotor power is delivered to the grid, so the grid power  $P_{grid}$  is the amount of stator power output  $P_{stator}$  plus the grid side rotor power  $P_{gr}$ . The grid side rotor power is 95% of the machine side rotor power, due to the DC link loss. So the power balance in the DFIG in the super-synchronous operational mode is shown as follows:

$$P_{in} = P_{loss} + P_{stator} + P_{mr} \quad (5.20)$$

Therefore, the total loss in the induction generator operating in super-synchronous mode can be expressed as:

$$P_{loss} = \omega T - P_{stator} - P_{mr} = \omega T - P_{stator} - \frac{P_{gr}}{0.95} \quad (5.21)$$

$$P_{loss} = \omega T - P_{stator} - \frac{(P_{grid} - P_{stator})}{0.95} \quad (5.22)$$

The efficiency of the DFIG in sub-synchronous operation using the input-output method with loss segregation can then be expressed as follows:

$$\eta = \frac{P_{grid}}{P_{grid} + P_{loss}} = \frac{P_{grid}}{P_{grid} + \omega T - P_{stator} - \frac{(P_{grid} - P_{stator})}{0.95}} \quad (5.23)$$

The composition of the total losses does not change, but the estimation of SLL is not the same as in the sub-synchronous mode because the power conversion is in the induction generator differs as shown in the following equation:

$$P_{SLL} = \omega T - P_{stator} - \frac{(P_{grid} - P_{stator})}{0.95} - 3I_s^2 R_s - 3I_r^2 R_r - P_{core} - P_{WF} \quad (5.24)$$

The smoothing of the function of SLL is the same as in the sub-synchronous operational mode. Hence, the precise value of SLL at any load point can be obtained accordingly.

#### 5.4 Summary

This chapter is concerned with the characteristics of various machine testing standards, and especially on the three major standards IEEE 112-B, IEC 34-2, and JEC 37. Through analysis and a comparison of these major standards, the IEEE 112-B is chosen as the most accurate standard in this thesis. Also loss determination and efficiency measurement using the input-output method with loss segregation have been introduced in detail. However, the current version of IEEE 112-B applies to conventional induction machine testing, and does not fully cover the testing of DFIG machines. Also no specific testing standard for the DFIG could be found in the literature. Therefore, an improved testing standard for the DFIG was purposed and carried out based on the IEEE 112-B standard, which separates the DFIG test into two main tests of the sub-synchronous and super-synchronous modes. In the improved standard, by conducting no-load and load tests of the DFIG, all of the different losses can be segregated and efficiency determined while the machine operates in the sub-synchronous and super synchronous modes.

## **Chapter 6 Results and Analysis**

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This chapter compares simulated and experimental results of the original and optimised rewinding design for the 4-pole 55 kW DFIG presented in Chapter 3 and re-designed in Chapter 4. The various tests are carried out for both the original and the optimised machines; the results are also compared to that of a machine built with optimised design plan. All tests are performed on a test rig, both the original machine and optimised machine were driven by a DC motor through a torque transducer and the following tests are carried out:

- No-load tests to determine the winding resistance, core loss, windage and friction loss.
- Load test to determine the efficiency of DFIG and stray load loss.

## 6.1 Introduction

The simulation and testing results of the original DFIG winding design and optimised rewind DFIG are presented in this chapter. Firstly, the FE calculated results of losses, efficiency, and air-gap flux density are carried out to validate the model. Then, the final built DFIG with an optimal number of wind turns and cross-sectional area (C.S.A) combinations was extensively tested and the results are presented later in this chapter. These results are used for comparison with the initial designed DFIG, with the aim of achieving high efficiency for a wind turbine generator. Finally, the improvement in the annual maximum power output of the wind turbine is calculated in detail.

## 6.2 Simulated Results

In chapter 4, the optimal results were provided using a surrogate-based optimisation algorithm. This section presents the validation of the model by conducting FE predictions of machine losses, efficiency, and air-gap flux density in the original and optimised rewind machines at rated speed of 1457 rpm.

### 6.2.1 Analysis of Losses and Efficiency

The various losses are caused due to the varying air-gap field and conductor losses, where the latter consist of the stator conductor loss, rotor conductor loss, and core loss. A transient 2D with motion model was solved to determine the contribution of the various losses, and a balanced three-phase voltage source was applied to the phases of the machine. Among these losses, the conductor losses ( $I^2R$ ) are hugely important and are determined using the winding resistance below:

$$R = \frac{\rho_e \times L_w \times N}{C.S.A} \quad (6.1)$$

where  $L$  is the axial length of the conductor,  $N$  is the number of winding turns, and  $\rho_e$  is the resistivity of the conductor. Figure 6.1 shows the FE analysed results for the differences in losses in the two machines at a rated frequency of 50 Hz.



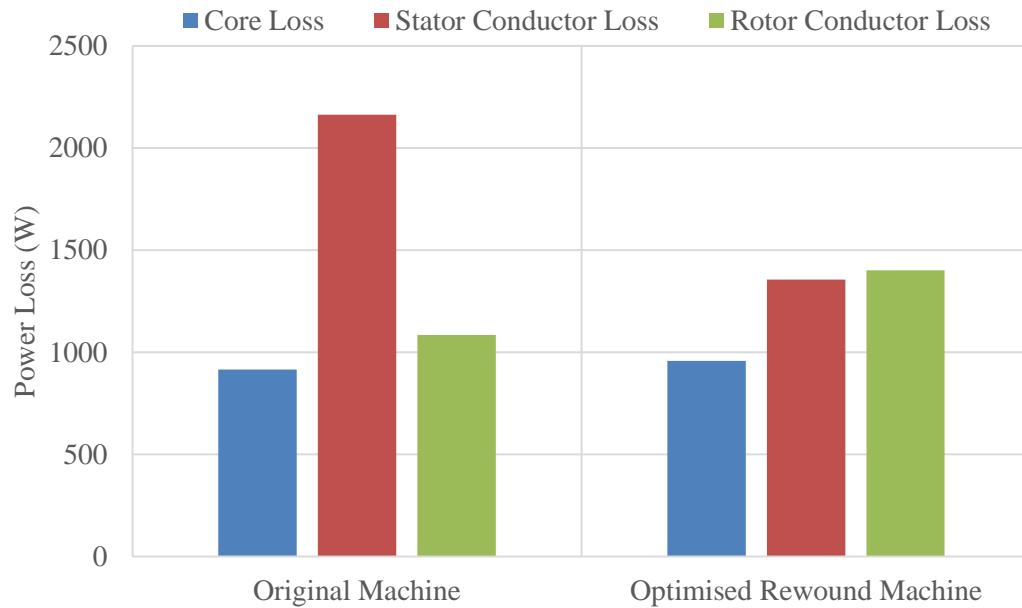


Figure 6.1 Comparison of simulated losses of original and optimised rewind machines at 1457 rpm.

According to the comparison of the FEM results, the core loss of the optimised rewind machine is still close to that of the original, showing an increase from 915W to 958W. But conductor losses have changed markedly. The stator conductor loss has decreased from 2164W in the original machine to 1357W, because the optimised design plan reduces the stator winding resistance by about  $0.05\Omega$  per phase. Beside this, although the optimised resistance value of the rotor winding is still quite close to the original, the reductions of winding turns and C.S.A in the optimised design plan causes the higher current in rotor winding, so the rotor conductor loss in optimised rewind machine is higher by about 316W than in the original machine. Hence, the total losses in the optimised rewind machine are reduced by about 448W than compared to the original machine. However, the electromagnetic analysis of the FEM is not able to calculate the SLL, and it also would be unlikely to be affected by a change in windage and friction losses.

The output power in the original and the optimised design plan are 55223W and 54932W respectively, and so the efficiency can be calculated. The optimised design plan improves the efficiency of the original design by approximately 0.6% at the rated conditions from 93% to 93.6%. Therefore, the efficiency comparison of the original and optimised rewind DFIGs could then be shown in figure 6.2.

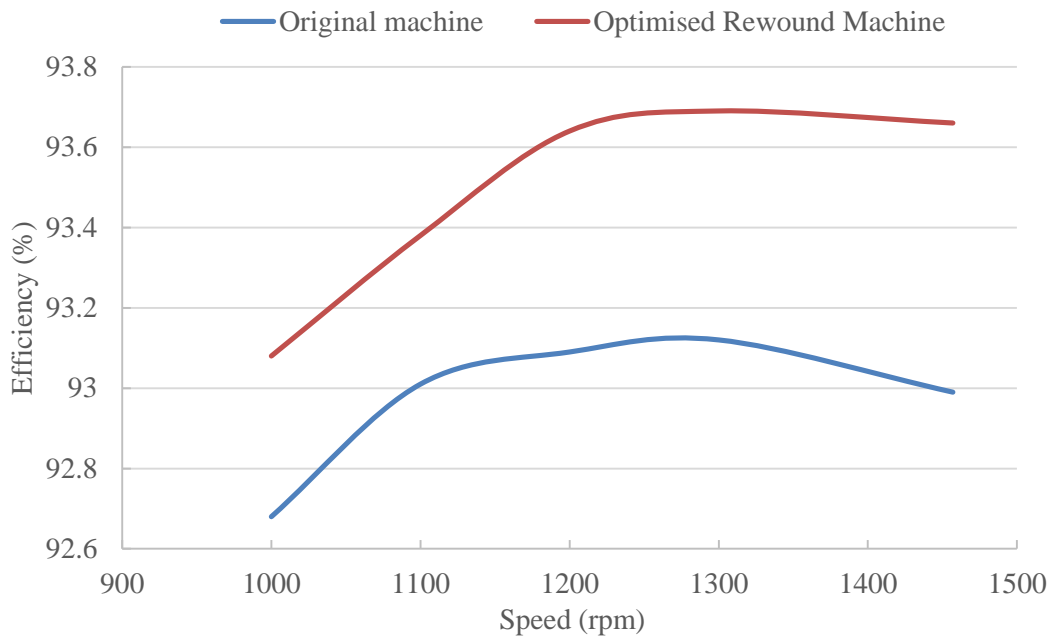


Figure 6.2 Comparison of efficiency of original and optimised rewind machines.

### 6.2.2 Air-gap Flux Density Analysis

In this test, the original and optimal design plans were simulated to check their individual air-gap flux densities. Flux affects the electrical and magnetic loading of the machine, since the electrical loading depends on the available slot area and the flux per pole depends on the amount of flux that links a tooth from the magnet pole. If the number of winding turns is doubled in motor mode, the air-gap flux density is halved, and the torque output is reduced accordingly. So, in this design, to guarantee the air-gap flux density is also quite important.

Therefore, a simple comparison has been carried out between the original and the optimised rewind machines. Figure 6.3 shows the air-gap flux density with the two different winding design plans in the original and optimised machines. It is clear that the values of air-gap flux density are quite close to each other, where the peak air-gap flux density in the original machine is 0.75T, and that in the optimised rewind machine is 0.73T. Including the errors, the fluctuation range is about 2%, which is acceptable.

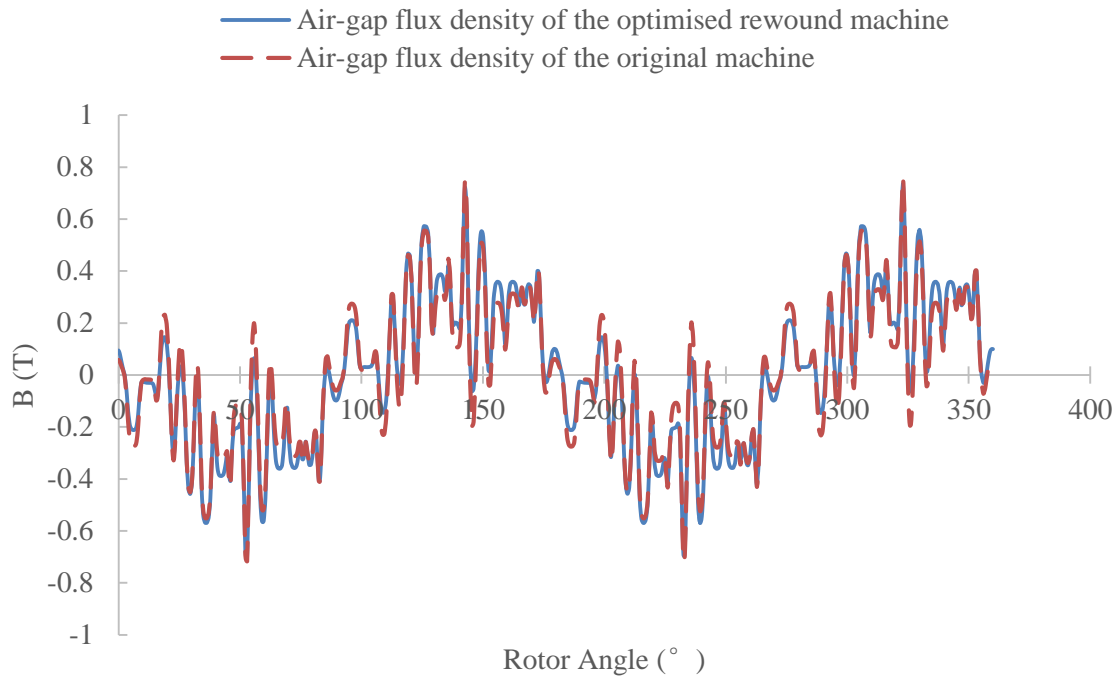


Figure 6.3 Air-gap flux density in original machine.

## 6.3 Experimental Test and Performance

### 6.3.1 Test Bench

A DFIG laboratory test bench was set up as shown in figure 6.4 to validate FEM results, and more details are given in Appendix. The DFIG was driven by a DC machine through a torque transducer at various speeds and loads. The stator power output of the induction generator achieved the energy conversion with rotor power, whilst the rotor was connected to the grid via a DC link. A three phase power analyser was used to measure the output voltage, current, and the power of the stator and grid using two-wattmeter method. Beside this, a DC current clamp is used to measure the rotor current between the generator and the DC link. Beside this, the test rig adopts the vector control techniques, which control the rotor currents to control the torque and speed of the DFIG, to achieve the output power control. And also, vector control enables the decoupled control of stator flux and electromagnetic torque.

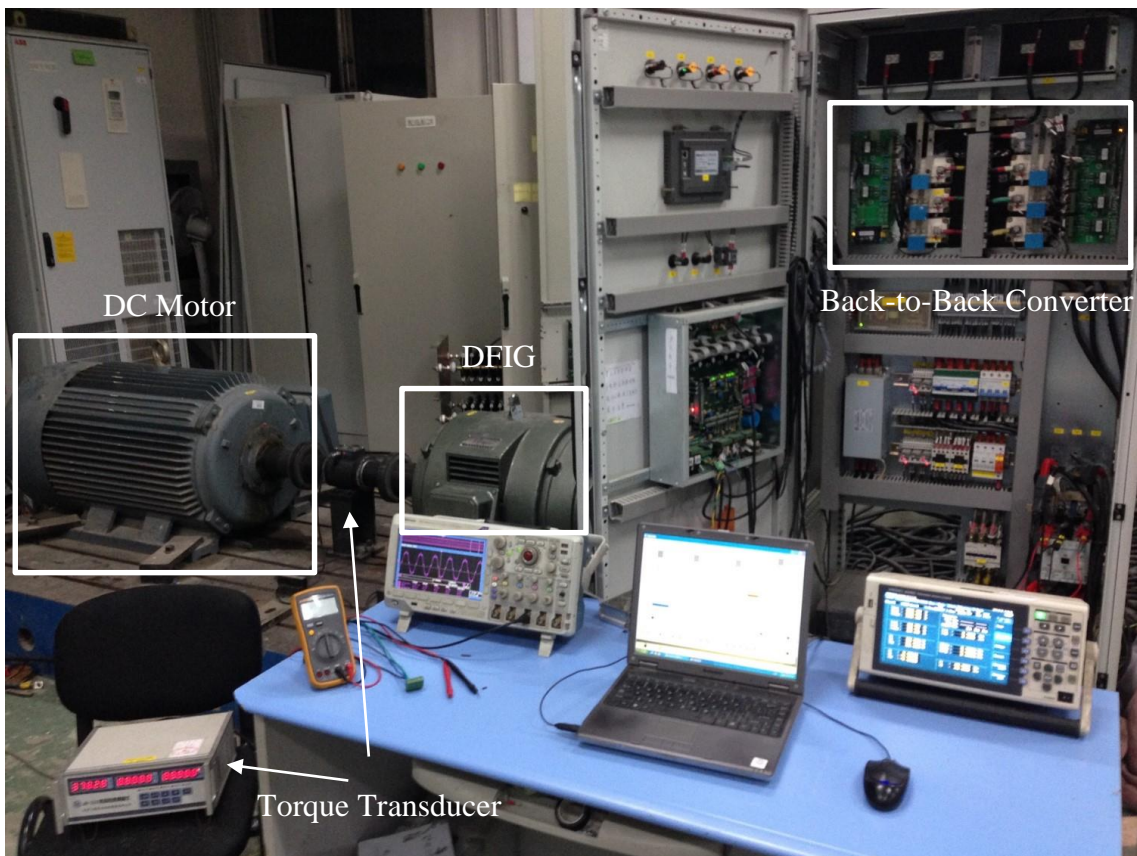


Figure 6.4 DFIG test rig

Both the original and the optimised rewind machine were built to compare the performance of the machine designs, which have the same structure of stator and rotor and are mounted on same jackets too; however, the winding designs of both the stator and rotor are different. Hence, in order to compare the results for the two designs, the readings of electrical output power, current, voltage, torque, speed, and winding temperature were recorded precisely at each load point. Furthermore, the rotational speed of DFIG used in wind turbine is commonly between 1200 rpm and 1800 rpm, so in this work the selection of experimental rotation speeds selected were 1200, 1300, 1457, 1600, 1700, and 1800 rpm.

### 6.3.2 No-load test

The no-load test is one of the most important parts of machine testing, and should be conducted first. Generally, no-load tests can be divided into two tests: static and running no-load test. The purpose of the static no-load test is to measure the winding resistance of both the stator and rotor, while the running no-load test is used to evaluate the core loss and windage and friction losses in the machine.

### 6.3.2.1 Static no-load test

The measurement of resistance was performed first on the original and newly built rewind machines during the no-load test, using the Kelvin Double Bridge since the resistance was lower than 1 Ohm. These measurements are taken on the fully assembled machine, which means that the windings have been inserted into the tooth slots of both stator and rotor, so that any short-circuit or open-circuit of the coil or phase connections in the machine can be identified.

Tables 6.1 and 6.2 compare the values of calculated and measured resistances. The phase values were measured with the machine delta connection in the stator and the star connection in the rotor.

Table 6.1 Stator Winding Resistance Values of Original Machine

	Single Phase Resistance			Line Resistance (Delta Connection)		
<b>Calculated resistance (<math>\Omega</math>) at 21°C</b>	0.1624			0.1083		
<b>Measured resistance (<math>\Omega</math>) at 21°C</b>	<b>Phase A</b>	<b>Phase B</b>	<b>Phase C</b>	<b>Phase A&amp;B</b>	<b>Phase B&amp;C</b>	<b>Phase A&amp;C</b>
	0.1591	0.1588	0.1588	0.111	0.1191	0.1089
	<b>Average</b>		0.1589	<b>Average</b>		0.113
<b>Error</b>	2%			4%		

Table 6.2 Rotor Winding Resistance Values of Original Machine

	Single Phase Resistance			Line Resistance (Star Connection)		
<b>Calculated resistance (<math>\Omega</math>) at 21°C</b>	0.0560			0.1119		
<b>Measured resistance (<math>\Omega</math>) at 21°C</b>	/			<b>Phase A&amp;B</b>	<b>Phase B&amp;C</b>	<b>Phase A&amp;C</b>
				0.1057	0.1059	0.1058
				<b>Average</b>		0.1058
<b>Error</b>	N/A			5%		

However, the single phase of the rotor winding cannot be measured directly because the machine is fully assembled and there is no rotor winding terminal which could be used for testing, so it has to be calculated using the experimental data of rotor winding phase resistance with the star connection. So, the measured single phase resistance of the rotor winding is approximately  $0.0529\Omega$ .

Furthermore, the calculated and measured winding resistance of the optimised machine is tested using the same principles and procedures, and the comparison of the calculated and measured resistances of the optimised machine is shown in Tables 6.3 and 6.4.

Table 6.3 Stator winding resistance values of optimised rewind machine

	Single Phase Resistance			Line Resistance (Delta Connection)		
<b>Calculated resistance (<math>\Omega</math>) at 21°C</b>	0.1172			0.0781		
<b>Measured resistance (<math>\Omega</math>) at 21°C</b>	<b>Phase A</b>	<b>Phase B</b>	<b>Phase C</b>	<b>Phase A&amp;B</b>	<b>Phase B&amp;C</b>	<b>Phase A&amp;C</b>
	0.1119	0.1117	0.1118	0.07513	0.07484	0.07511
	<b>Average</b>		0.1118	<b>Average</b>		0.075
<b>Error</b>	4%			3%		

Table 6.4 Rotor winding resistance values of optimised rewind machine

	Single Phase Resistance			Line Resistance (Star Connection)		
<b>Calculated resistance (<math>\Omega</math>) at 21°C</b>	0.0546			0.1091		
<b>Measured resistance (<math>\Omega</math>) at 21°C</b>	/			<b>Phase A&amp;B</b>	<b>Phase B&amp;C</b>	<b>Phase A&amp;C</b>
				0.1014	0.1015	0.1015
				<b>Average</b>		0.1015
<b>Error</b>	N/A			6%		

Determining the resistance of the single phase in the optimised machine is similar to the measurement in the original machine, which is performed using experimental data based on the

new winding parameters. So the measured single coil resistance of the rotor winding is approximately  $0.0507\Omega$ .

According to the no-load test, core loss and windage and friction losses could be segregated from the total loss in the DFIG. The calculated resistance values of the stator and rotor for both machines were estimated using theoretical equations, and so the errors between the measured and calculated values may be caused by the estimation of the actual total length of the wire, temperature effects, and the accuracy of the testing equipment.

### ***6.3.2.2 Running No-Load Test***

The running no-load test was performed when the induction machine was fully assembled and mounted on the test rig and the machine was operated as an induction motor at the rated frequency and voltage without any load carried. The purpose of the running no-load test is to measure the core loss, and windage and friction losses.

When the machine is running in a no-load condition, the losses are generated in its different components, and include the core loss, windage loss, frictional loss, and stator conductor loss. During this test, the test machine was configured as a motor, while the variable voltage power supply was connected to the stator, which provides the rated frequency and voltage. Furthermore, the rotor shaft is not connected to any load, whilst the three-phase rotor is short-circuited. So, with the input of the rated frequency and voltage, the rotor will rotate at a fixed speed which depends on the frequency. Generally the rotation speed is 1500 rpm with 50 Hz and 1800 rpm with 60 Hz.

Then, the input voltage is varied from 100% of rated voltage down to the point where the speed shows a significant decrease, which is approximately 30% of the rated voltage in this work. Voltage, input power and current were measured using a high-precision power analyser. Also, because a change in temperature could affect the value of winding resistance, it has to be measured and recorded in order to ensure experimental accuracy. Figures 6.5 and 6.6 compare the values of uncorrected winding resistance and corrected winding resistance at different temperatures for the original and optimised rewound machines respectively, and the correction method of winding resistance is expressed in equation 5.2.

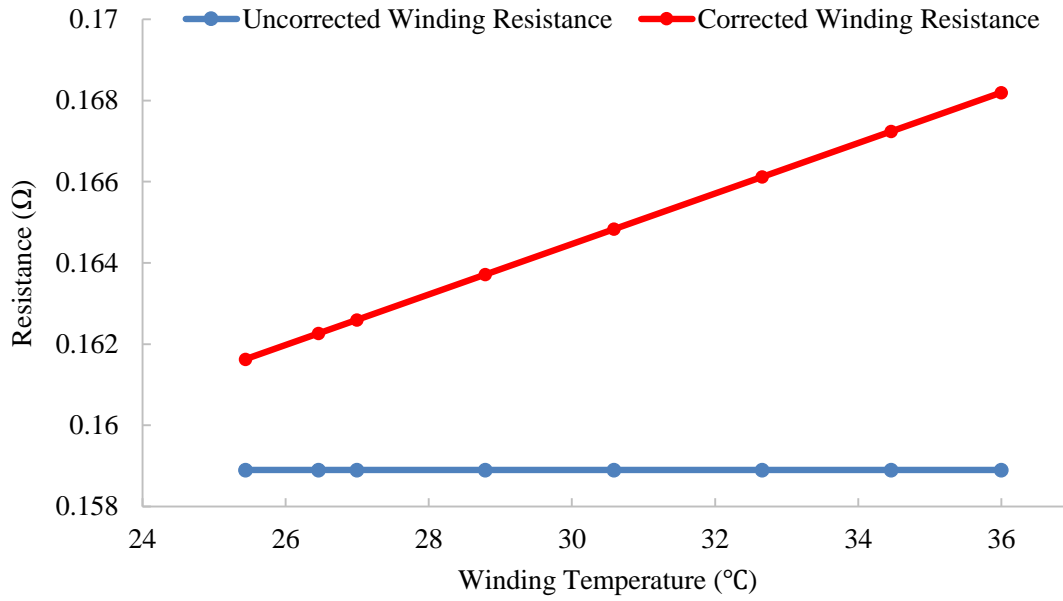


Figure 6.5 Stator winding resistance correction per phase in original machine.

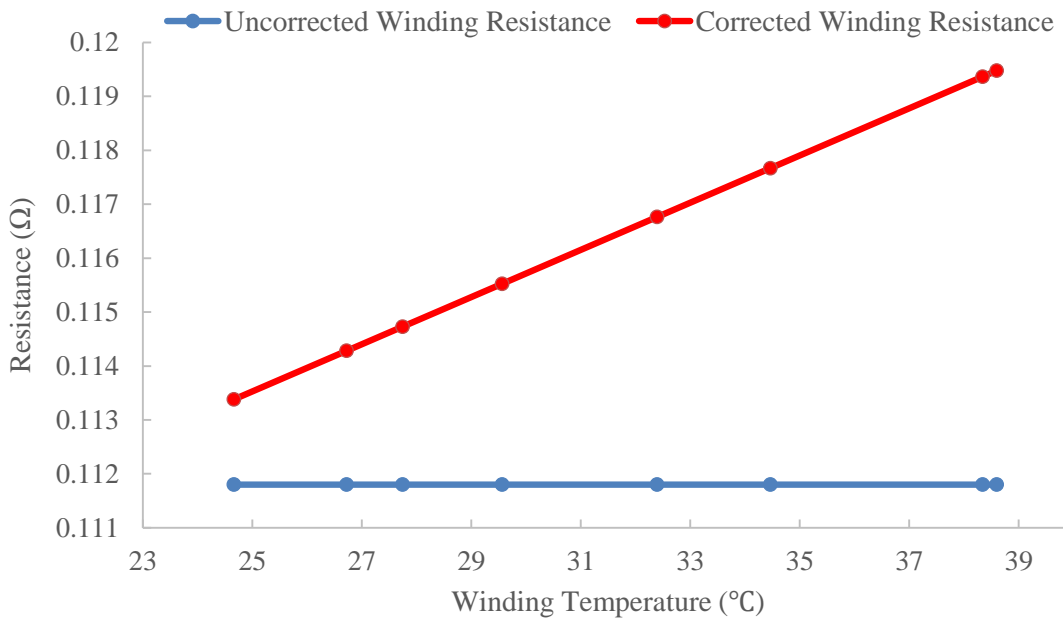


Figure 6.6 Stator winding resistance correction per phase in optimised rewind machine.

Furthermore, for the different winding parameter designs, the balanced temperature at different voltage points is compared in the original and optimised machines under the no-load condition, as shown in figure 6.7. In the no-load test, the temperature data is recorded rapidly when the wind temperature is stable by running machine for a while at different voltage points.



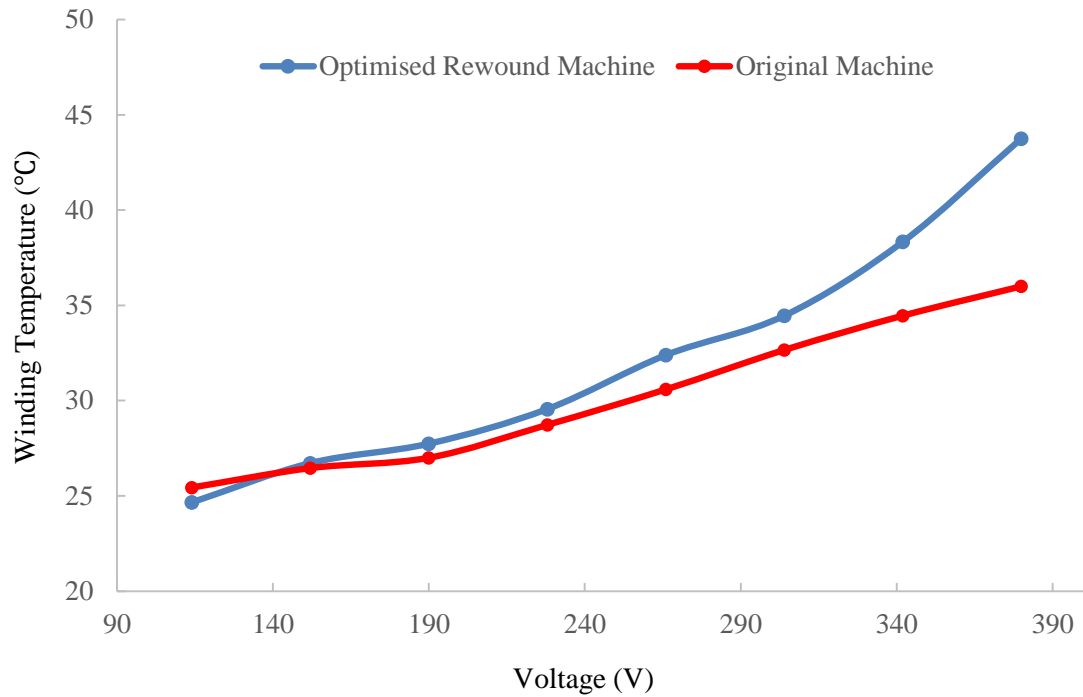


Figure 6.7 Winding temperature at different voltage points in no-load test.

The balanced temperature is known during the no-load test, and therefore the winding resistance is corrected to determine the conductor loss. In this test, the rotor current is very small due to no load being carried, and so the rotor conductor loss can be neglected. Hence, the stator conductor loss is the main conductor loss, which can be measured using the stator phase current and corrected winding resistance. Therefore, the stator conductor loss can be obtained at any voltage point. Figure 6.8 illustrates the stator conductor loss in the range of voltages.

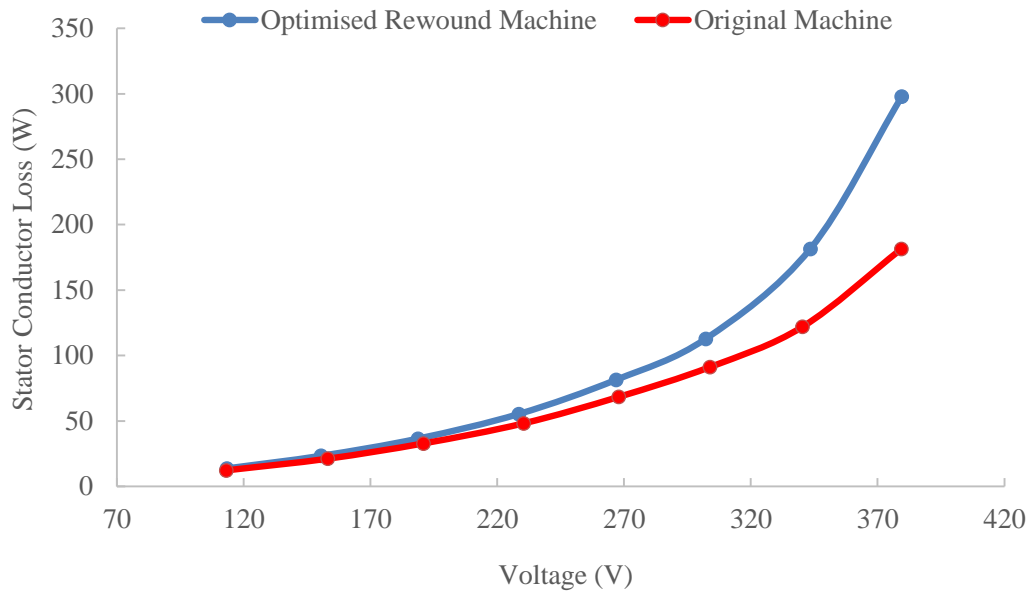


Figure 6.8 Comparison of stator conductor loss in original machine and optimised rewind machine in no-load test.

During a no-load test, it is well known that the input power is consumed entirely in the form of losses from the different components of a machine. Hence, according to the practical work, the input power as shown in figure 6.9 shown could be measured directly. With the same voltage supply, the input power of the optimised rewind machine is higher than the original.

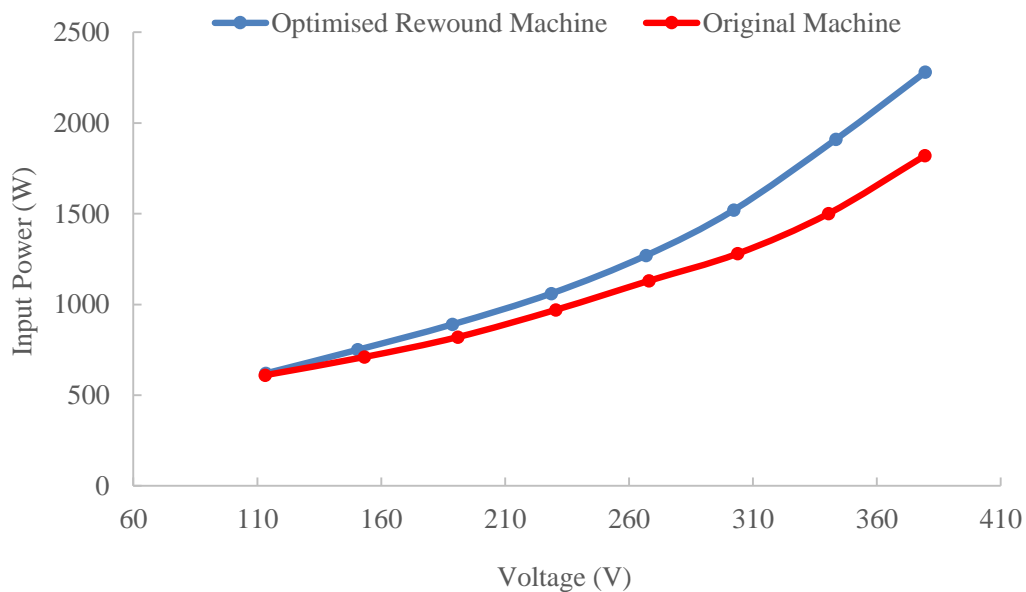


Figure 6.9 Input power at different voltage point.

So, after subtracting the stator conductor loss from the input power at each of the test voltage points, the remaining losses are the core loss, and windage and friction loss. Meanwhile, the power curve of core loss and windage and friction loss versus voltage squared are plotted accordingly, and then linear regression analysis is used to extend the curve to zero voltage, so that the point of intersection with the Y axis is the value of windage and friction losses. From figure 6.10, the windage and friction losses of original machine is about 501.95 W.

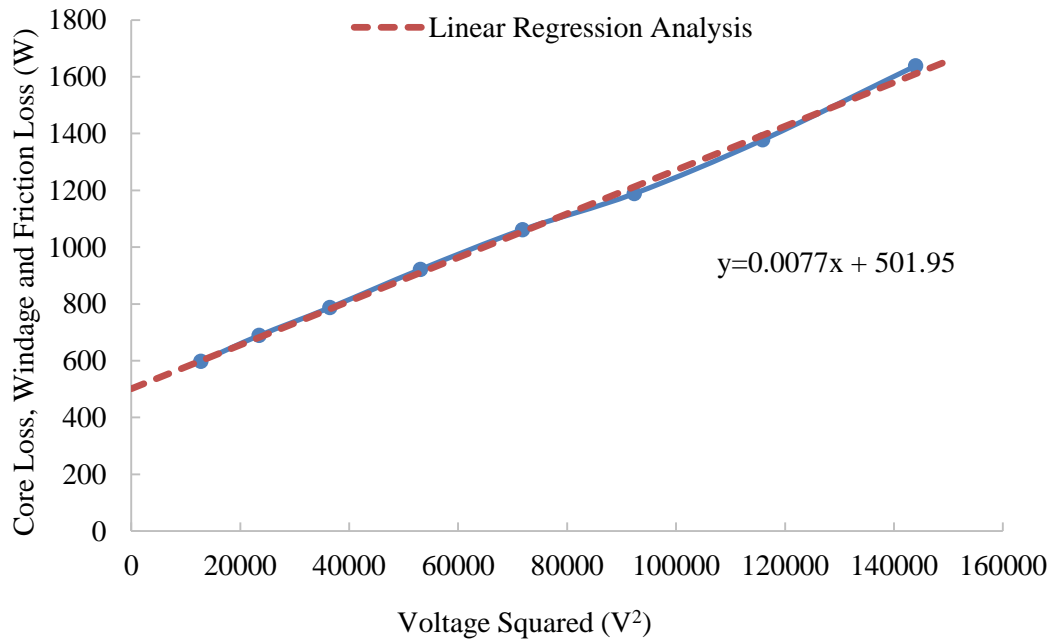


Figure 6.10 Determination of the core loss and windage and friction loss of the original machine.

During the machine in operation, the windage and friction loss is a constant value at any desired voltage, if it is subtracted along with the stator conductor loss from the input power, so the resulting power value represents the core loss. Figure 6.11, the core loss in the original machine can be measured directly at any desired voltage. Assuming the voltage is 380 V, and then the core loss in the original machine is 1136.44 W.

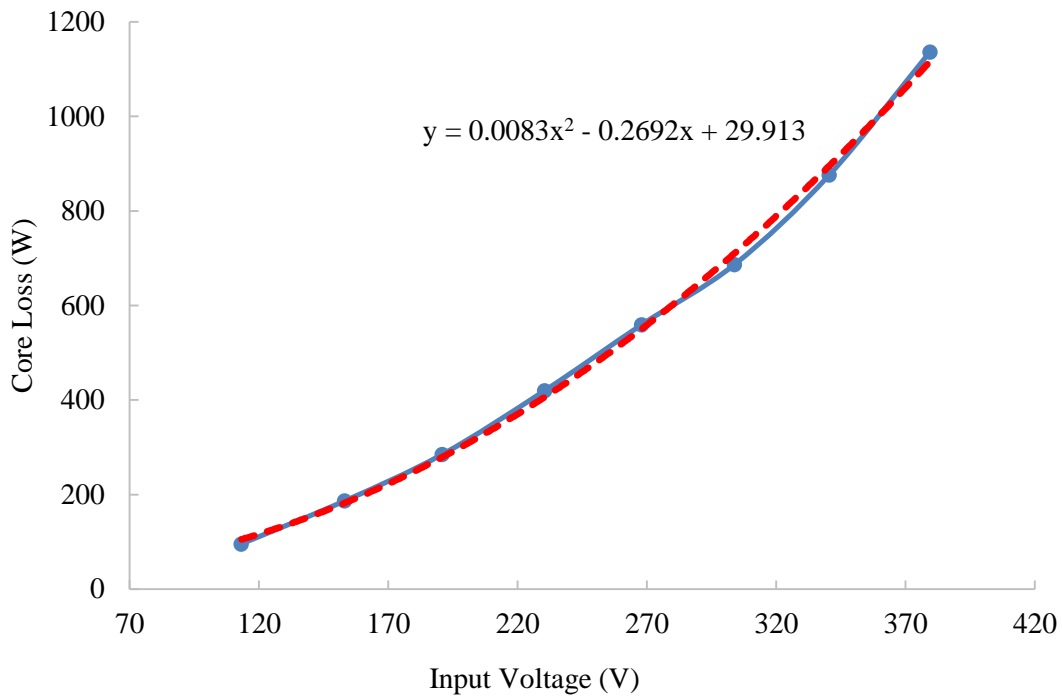


Figure 6.11 Determination of the core loss of the original machine.

The same calculation and measurement of core loss and windage and friction loss is then adopted for the optimised rewind machine. Therefore, the windage and friction loss is about 521.47 W, and the core loss is approximately 1280.61 W when the voltage is 380 V. The relevant results are displayed below in figures 6.12 and 6.13.

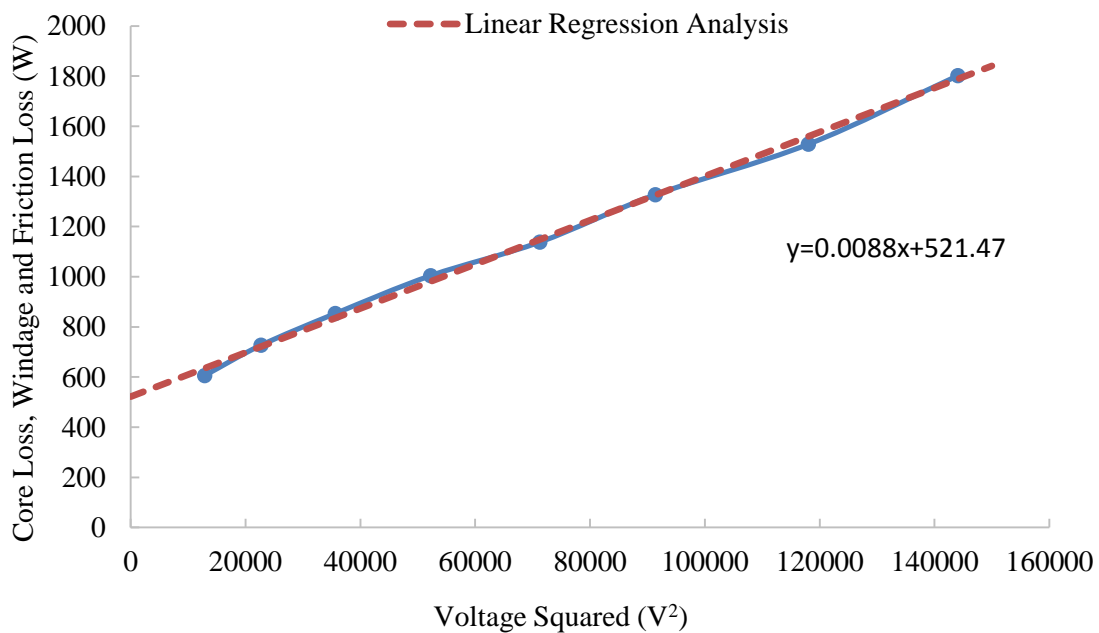


Figure 6.12 Determination of the core loss and windage and friction loss of the optimised rewind machine.

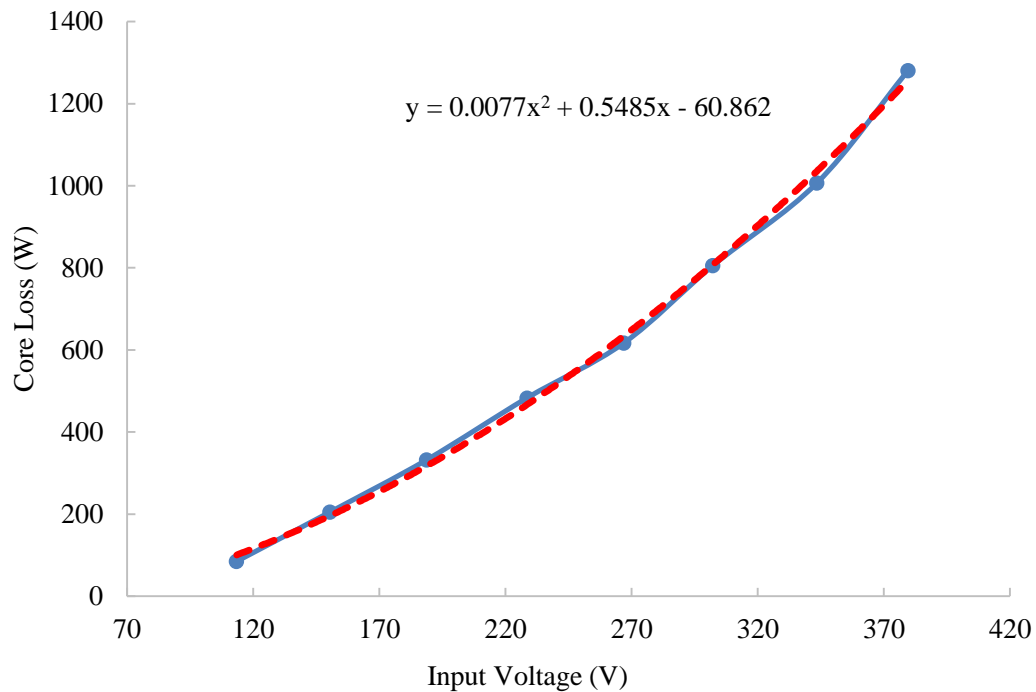


Figure 6.13 Determination of the core loss of the optimised rewind machine.

According to the comparison of the original and optimised rewind DFIG in no-load test, the core loss and windage and friction loss of the optimised rewind DFIG has a slight increasing of 170 W than the original when the supply voltage is 380 V.

### 6.3.3 Load Test

The load test is performed with the induction generator at a range of speeds with varying loads. In this section, the efficiency of the DFIG and determination of stray load loss are presented, which will provide a general idea of the machine's performance over its operating range and loss segregation in the DFIG.

#### 6.3.3.1 Test Limitations

For a number of reasons the scope of the load test was limited:

- The operational speed of the induction generator is limited to between 1200 rpm and 1800 rpm.
- For safety reasons it was decided to limit the rotor RMS current to less than 100 A. This was to prevent the overcurrent causing the breakdown of the IGBT in the back-to-back converter, where the rotor is connected to the grid through a back-to-back converter.

### 6.3.3.2 Temperature Measurement

The temperature measurement is used to correct the winding resistance so as to ensure the precision of stator and rotor conduction loss measurements when the generator is in operation, which has a significant direct effect on the determination of efficiency. So in this work, PT 100 thermocouples were embedded between the coil sides within a stator slot to monitor the stator winding temperature during the testing of both the original and the optimised rewind machines. Furthermore, the machines were run for a while during the test, until the coil temperature achieved the balance, in order to measure the temperature as quickly as possible so as to minimise any temperature change in the DFIG during the load test. This means that the experimental data will be more accurate.

Balanced coil temperatures were recorded at different load points at a variety of speeds, as shown in figures 6.14 and 6.15. The coil temperature of the original machine is relatively higher than in the optimised rewind machine at the different load points, which is due to the winding parameter design. Beside this, when machine speed increases, the winding temperature shows a slight decrease at the same load points.

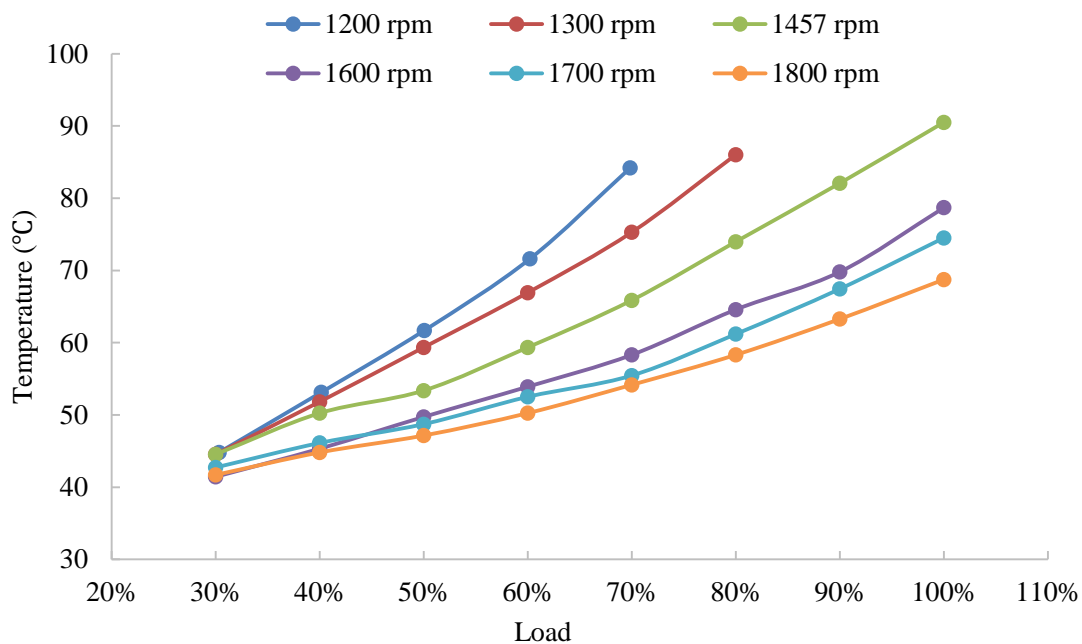


Figure 6.14 Winding temperature of original machine with different rotational speeds.

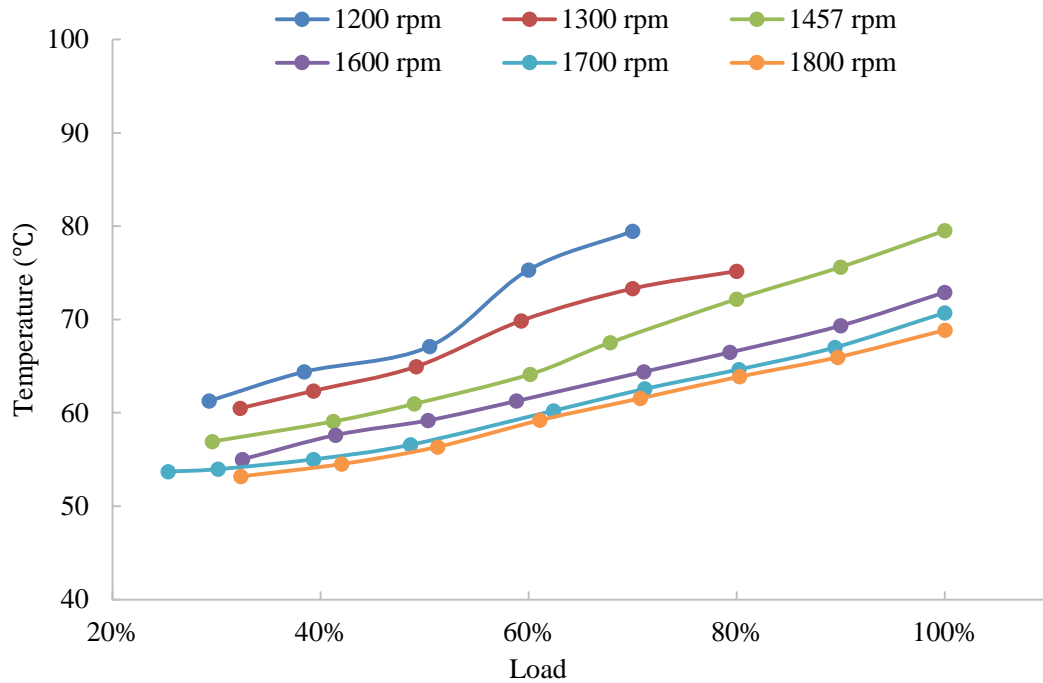


Figure 6.15 Winding temperature of optimised rewind machine with different rotational speeds.

### 6.3.3.3 Conductor Losses Measurement

As described in the previous section, some parts of the conventional loss have been obtained in the no-load test, such as core loss and windage and friction loss. Conductor losses are one of the most important conventional losses in the DFIG and consist of stator conductor loss and rotor conductor loss. These can only be measured accurately in load test. During the test, conductor losses vary with the load carried due to the changes in current and temperature. Figures 6.16 and 6.17 compare the stator conductor loss and rotor conductor loss of the original and optimised rewind machines at the rated speed of 1457 rpm at different load points.

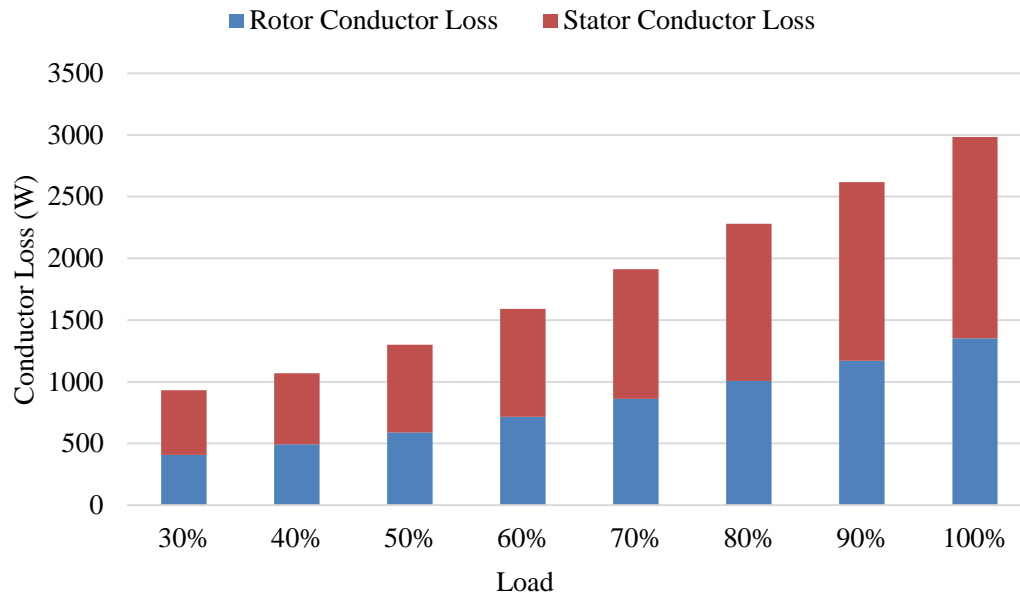


Figure 6.16 Conductor losses at 1457 rpm in original machine.

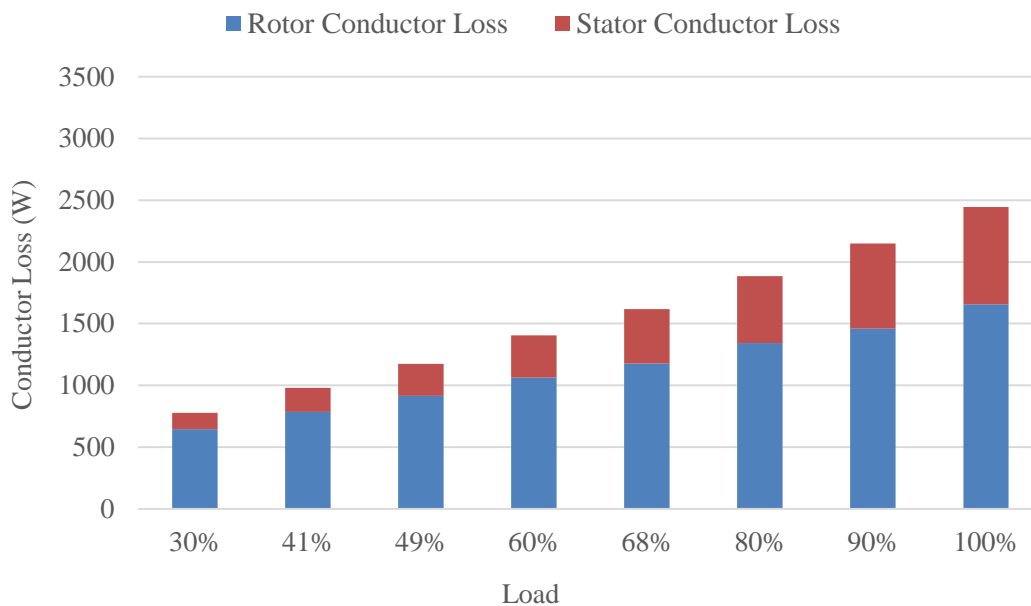


Figure 6.17 Conductor losses at 1457 rpm in optimised rewind machine.

According to the comparison, the total conductor losses of the original machine are higher than in the rewind design, by approximately 500 W, and the rotor conductor loss in the optimised rewind machine shows a significant increase compared to the original machine due to the higher current density. Furthermore, the variation in total conductor losses in the original machine is presented in figure 6.18, while figure 6.19 shows the total conductor losses in the rewind machine operating at various speeds and different load points.



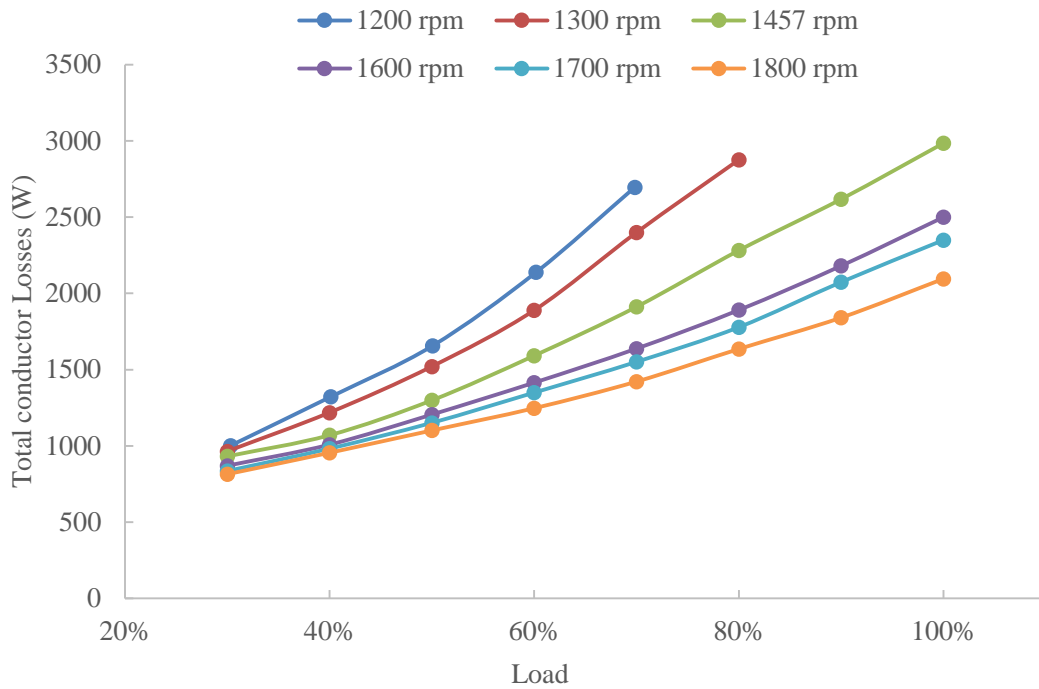


Figure 6.18 Total conductor losses in original machine.

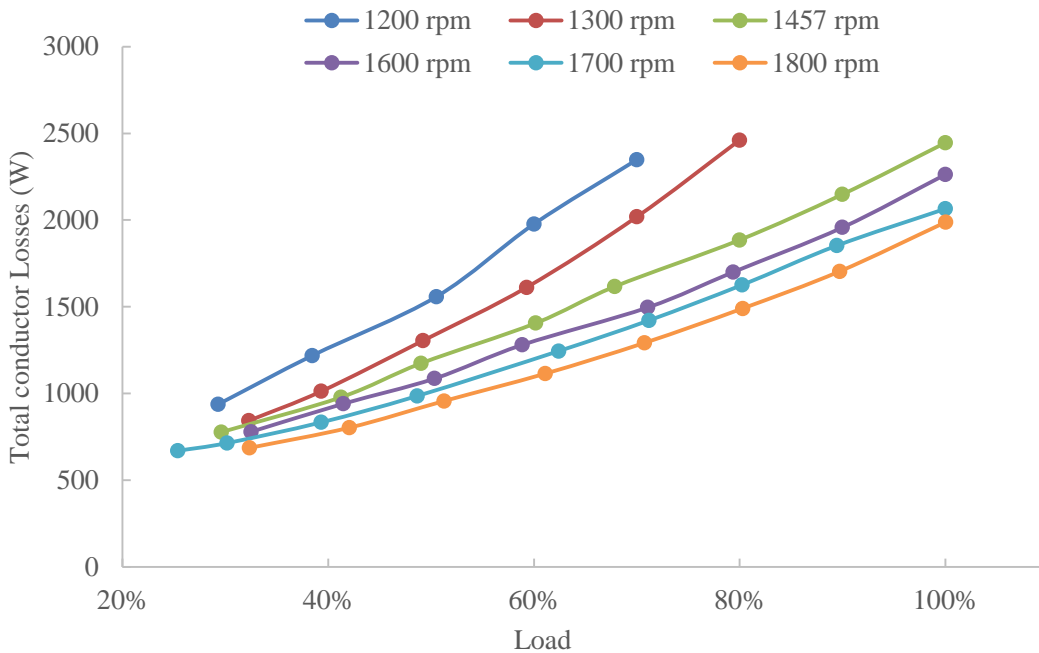


Figure 6.19 Total conductor losses in optimised rewind machine.

#### 6.3.3.4 Stray Load Loss

Stray load loss (SLL) is the most elusive part of the losses in the DFIG, and it is hard to directly and precisely measure using the experimental method. Loss segregation is a good way to evaluate the SLL from the total losses based on the IEEE 112-B method. So before that, the

various conventional losses must be clearly measured. Referring to chapter 6, the estimation of SLL is proportional to torque squared and its slope has a significant effect on the value of SLL. After neglecting the errors at various speeds, the corrected function of stray load loss goes through the original point as presented in figures 6.20 to 6.23. The slope increases from 0.006 at 1200 rpm to 0.0243 at 1800 rpm in the original machine, and from 0.0097 at 1200 rpm to 0.0171 at 1800 rpm. There is an obvious trend for the slope of SLL to increase with rotational speed at the same load point. Therefore, the SLL could be obtained by using the corrected SLL function at any load point at various speeds.

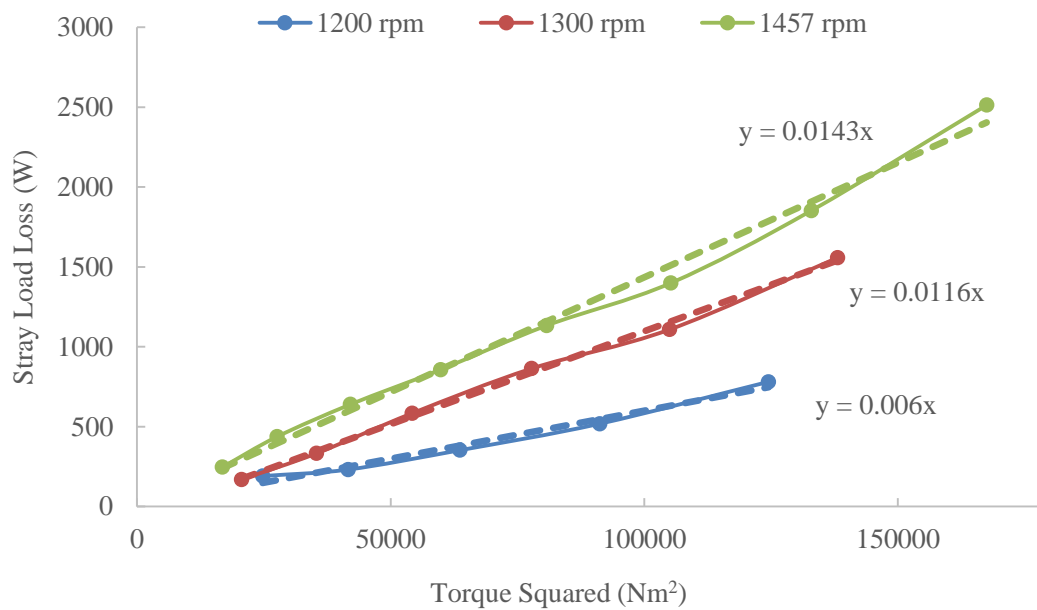


Figure 6.20 Analysis of stray load loss in sub-synchronous original machine.

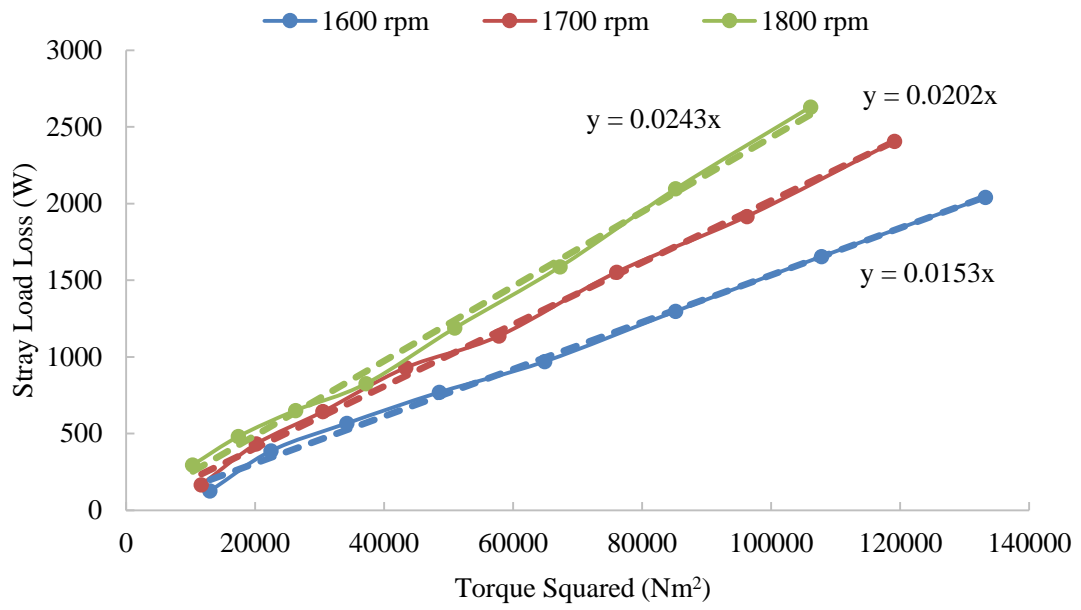


Figure 6.21 Analysis of stray load loss in super-synchronous original machine.

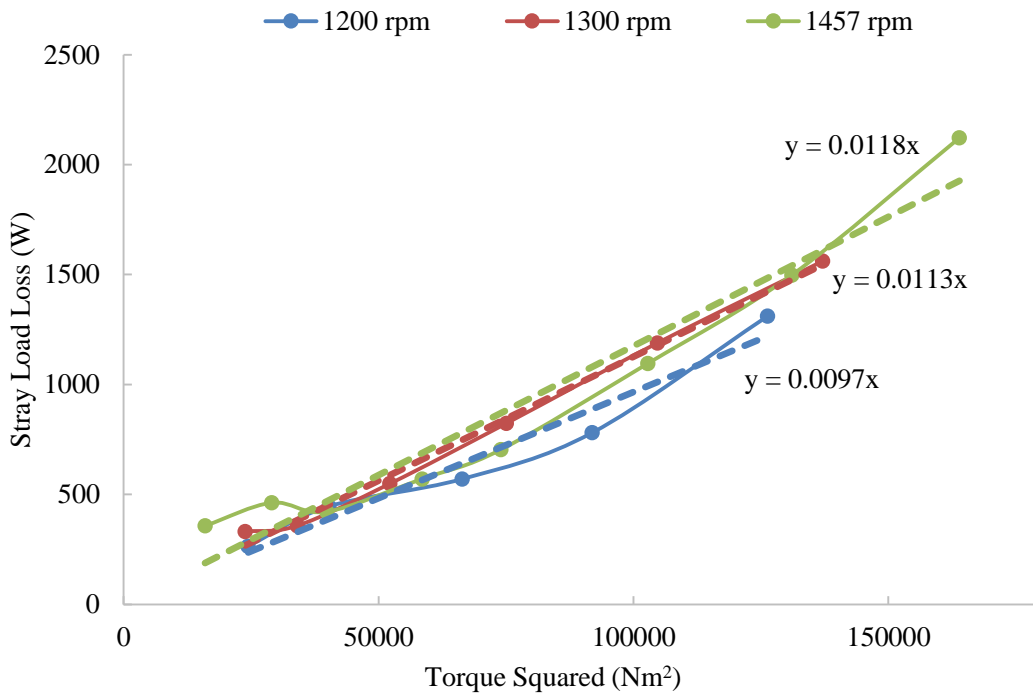


Figure 6.22 Analysis of stray load loss in sub-synchronous rewind machine.

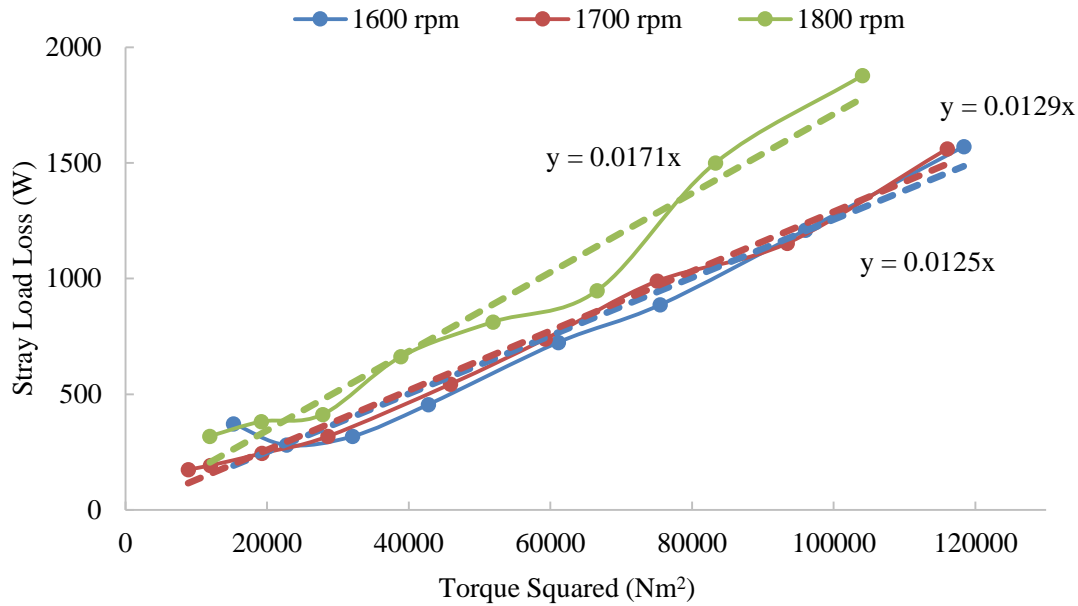


Figure 6.23 Analysis of stray load loss in super-synchronous rewind machine.

### 6.3.3.5 Efficiency Determination

This section determines the efficiency of the original and optimised rewind machine based on the improved testing method. Following the method introduced in Chapter 5, efficiency can be calculated after all parts of the losses have been segregated and measured precisely. It is worth noting that the determination of efficiency is quite different in the two operational modes, and so it has to be measured and calculated separately. Hence, in this section the efficiency of the two machines is compared and presented in two different parts.

- Efficiency in sub-synchronous mode

This section compares the efficiency of the original machine and the optimised rewind machine during sub-synchronous operation. Figures 6.24 to 6.26 show the measured efficiency with varying load when the rotational speed is selected as 1200 rpm, 1300 rpm, and the rated 1457 rpm to support the running of the sub-synchronous mode.

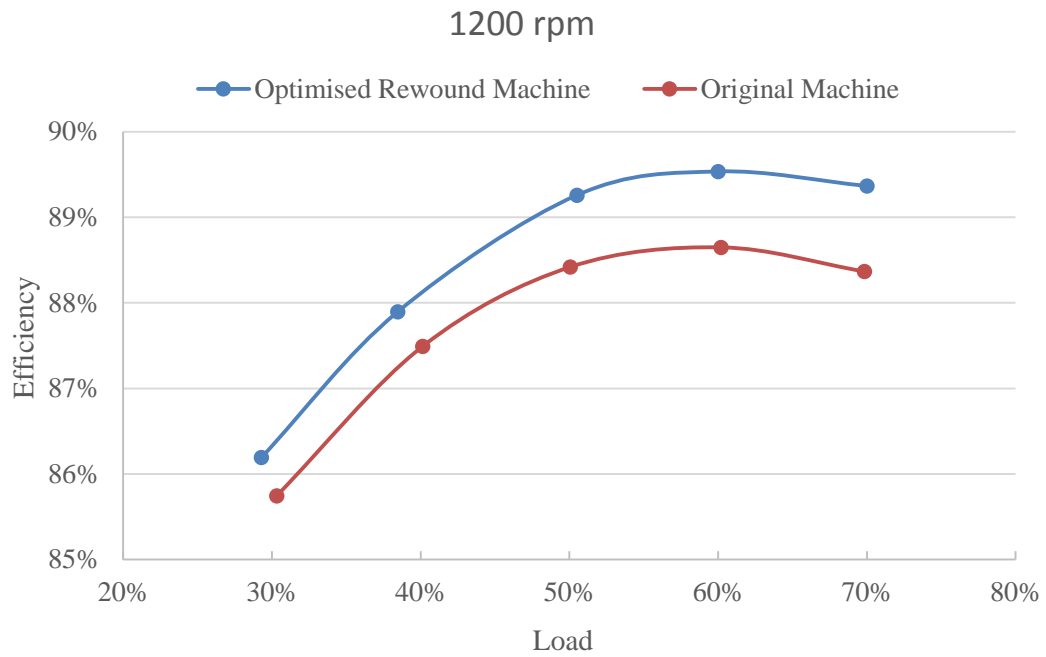


Figure 6.24 Comparison of original machine and optimised rewind machine at 1200 rpm.

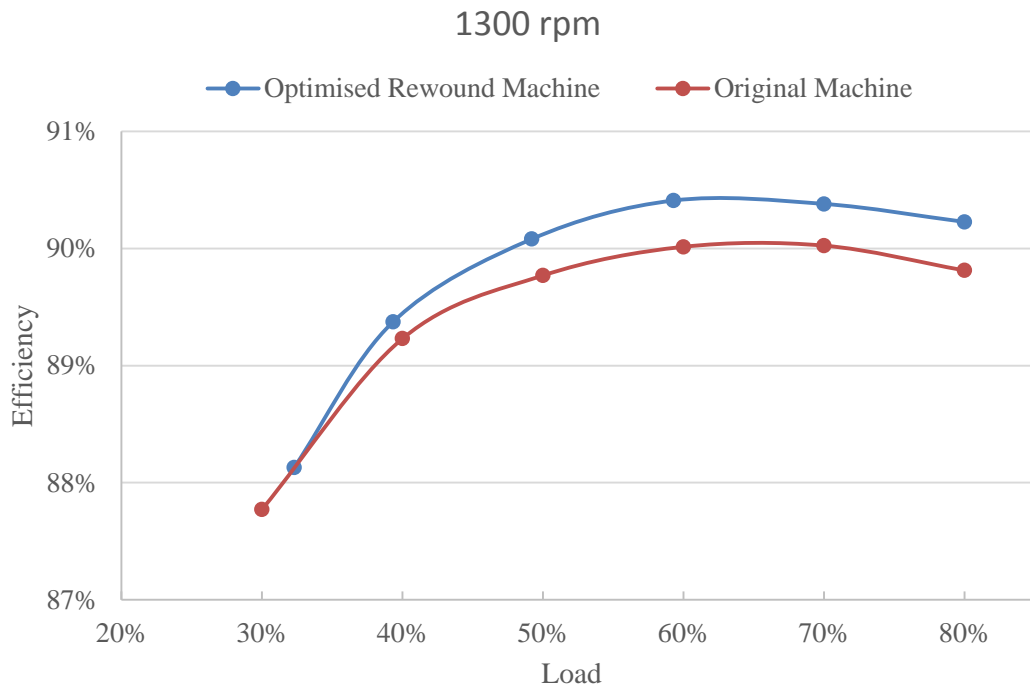


Figure 6.25 Comparison of original machine and optimised rewind machine at 1300 rpm.

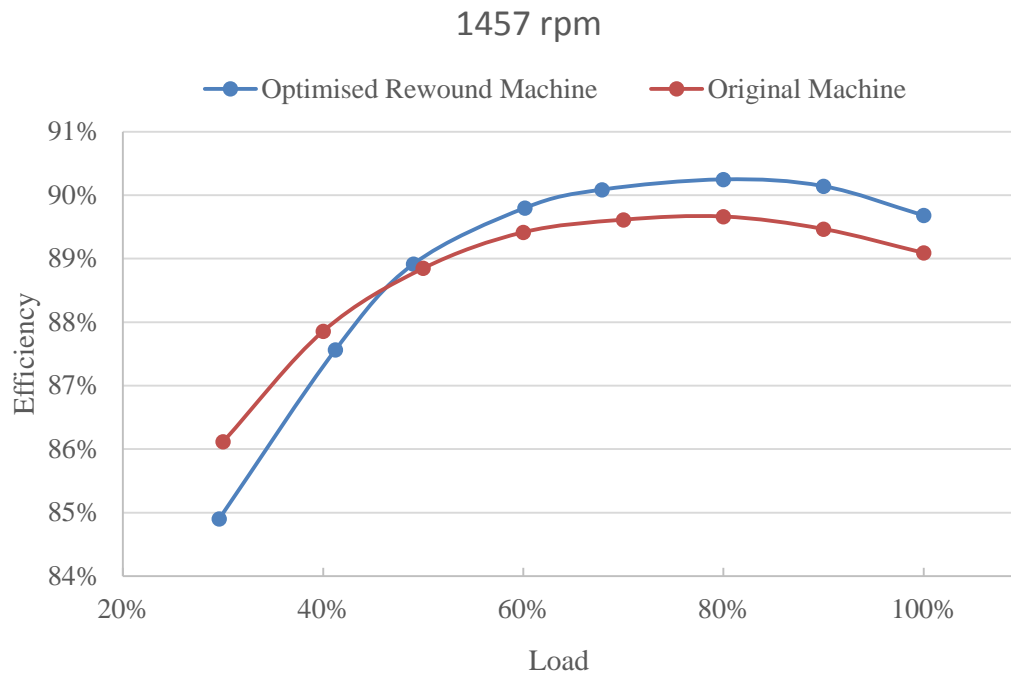


Figure 6.26 Comparison of original machine and optimised rewind machine at 1457 rpm.

According to the results in sub-synchronous mode, the optimised rewind machine has a higher efficiency than the original machine. From the figures above, the improvement in efficiency is about 0.9% from 88.4% to 89.3% when the rotational speed is 1200 rpm and approximately 0.4% from 89.8% to 90.2% at 1300 rpm when fully loaded. Beside this, when the rotational speed increases to the rated 1457 rpm, the efficiency of the original machine is higher than the rewind machine with a lower load carried, but with increasing load until nearly 50% load, the value of efficiency are close to each other. Then the rewind machine has better efficiency than the original at high loads representing an improvement of approximately 0.6% from 89.1% to 89.7%.

- Efficiency in super-synchronous mode

Similarly, in the super-synchronous mode, the rotational speeds are set as 1600 rpm, 1700 rpm, and 1800 rpm to carry varying loads. Figures 6.27 to 6.30 present the efficiency comparison of the original and optimal rewind machine. The biggest improvement in efficiency is at 1800 rpm, with an approximately 1.3% efficiency increase compared to the original machine when fully loaded. Beside this, there is about a 1% efficiency improvement at both 1600 rpm and 1700 rpm. During super-synchronous mode, the DFIG is more efficient at lower speed.

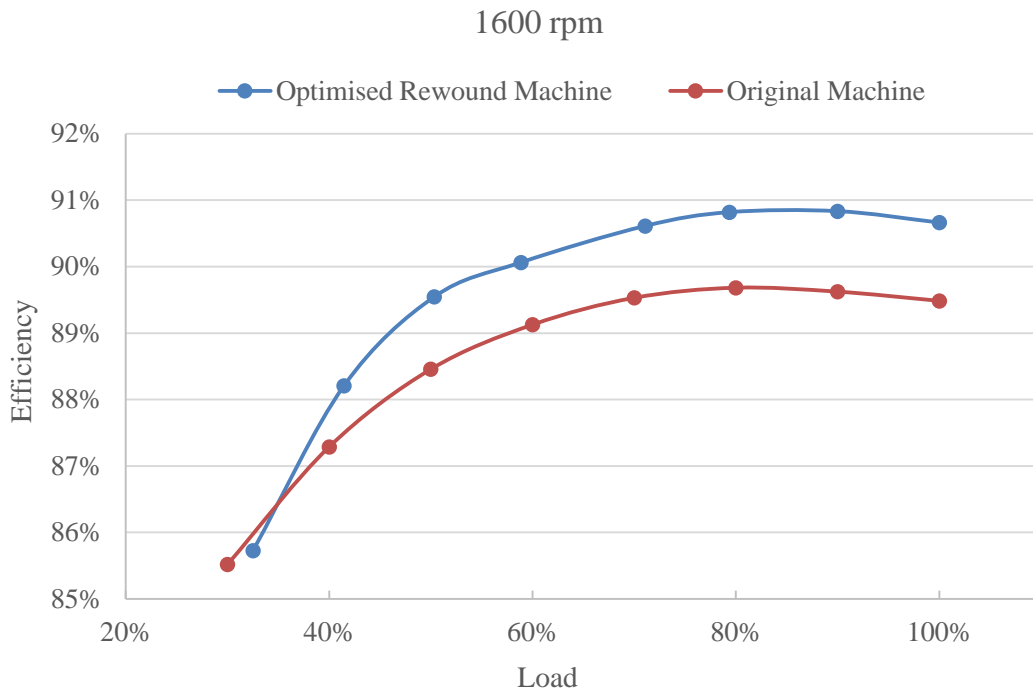


Figure 6.27 Comparison of original machine and optimised rewind machine at 1600 rpm.

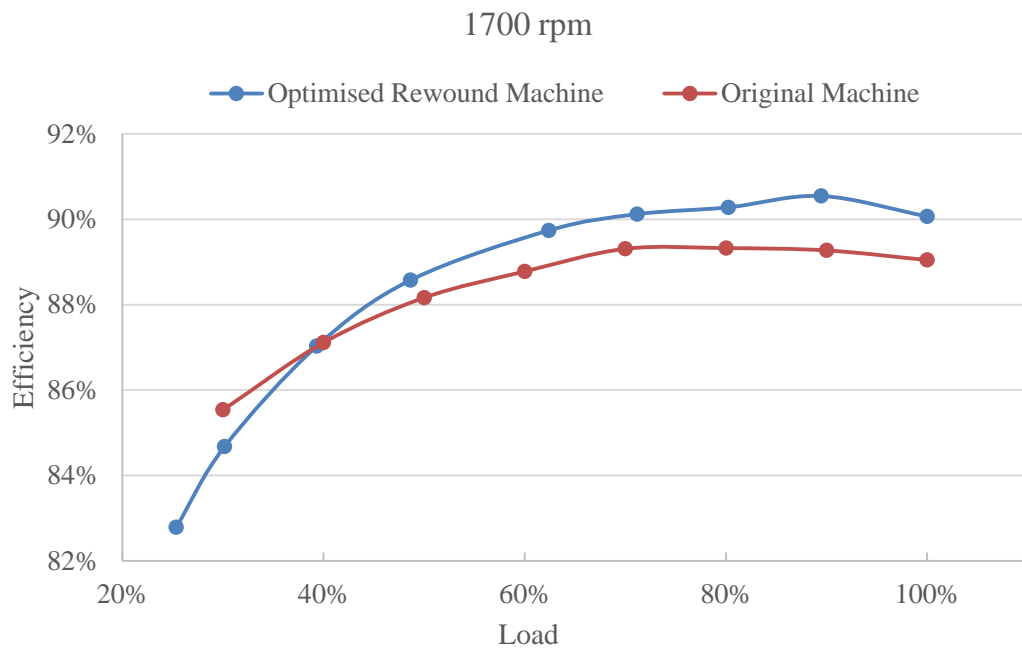


Figure 6.28 Comparison of original machine and optimised rewind machine at 1700 rpm.

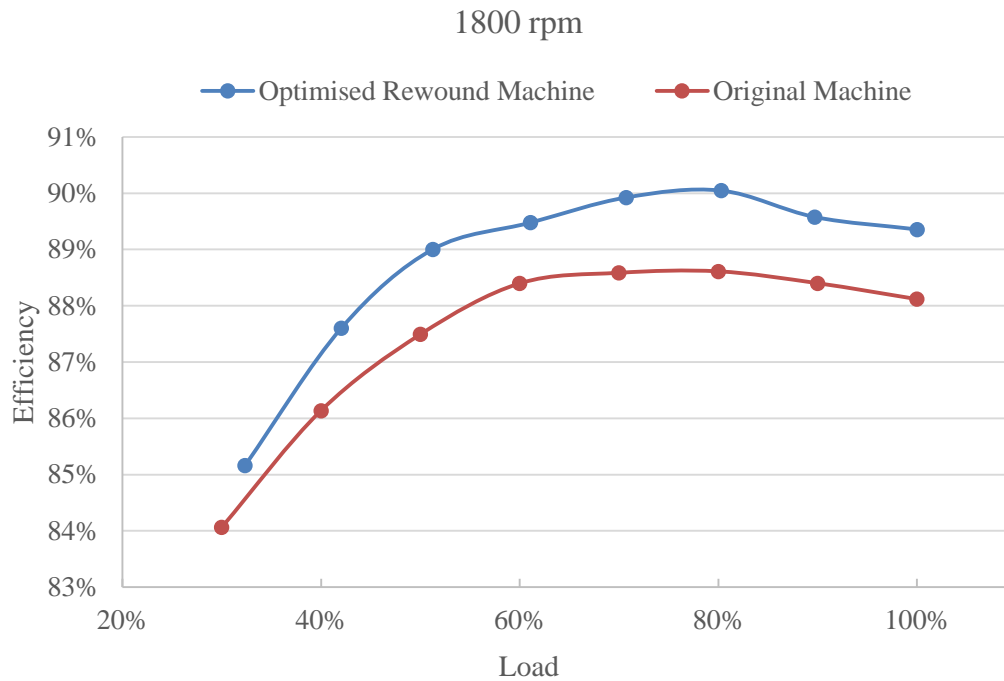


Figure 6.29 Comparison of original machine and optimised rewind machine at 1800 rpm.

Although the numerical and experimental results show similar trends in the two machine designs, the numerical results do not precisely coincide with the experimental results. The difference between the FEM and experimental results may be caused by several factors. Firstly, the stator power loss is dependent on the winding temperature, and there is no guarantee that the numerical and experimental tests were conducted at exactly the same winding temperature. Secondly, there is no sensor to measure the rotor temperature, and so the rotor copper loss is determined using IEEE standard methods. Thirdly, windage and friction and stray load losses are also not measured in the numerical studies, and are a function of operational speed and load.

#### 6.4 Summary

The results from simulation and practical work with both the original machine and the optimised rewind machine have been presented in this chapter. The experimental results were used to verify the FE predictions.

The no-load test compared the value of core loss and windage and friction losses in the original and optimised rewind machines. It was found that the core loss and windage and friction losses of the optimised rewind machine slightly increase. The load test was used to achieve the segregation of losses such as conductor losses and stray load loss, whilst measuring machine efficiency. The comparison of load test results was carried out on both machines under the same experimental condition and with the same methods. This has shown that the stator conductor



loss in the optimised rewind machine is much lower than in the original machine, but the rotor conductor loss in the optimised rewind machine has slightly increases due to the higher current density in the rotor winding. Beside this, the analysis of stray load loss was carried out using the total losses in the DFIG. It was found that the efficiency of the optimised rewind machine was about 0.6% better than that of the original machine in the sub-synchronous mode, and about 1% better in the super-synchronous mode.

## **Chapter 7 Wind Energy Production**

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An estimation of the annual wind energy production of a wind turbine at a specific location is presented in this chapter. The wind resource and its characteristics are investigated to estimate the actual wind power in the air using the wind speed profile from a testing point. Annual wind speed data is analysed using a statistical estimation method to determine the probability density function of wind speed at a specific site. The annual power output of a wind turbine at the Albemarle site is determined, along with studies of the Betz Law, Power Law, and turbine power curve. A comparison of the annual wind energy production using the original and the optimised rewind turbine generator is then presented. Meanwhile, improvements demonstrated in the 55 kW wind turbine as a case study are now used to look at potential and improvement in a real wind turbine.

## 7.1 Introduction

The United Kingdom is one of the most windy countries in Europe; the estimated mean wind speed at a height of 45 metres is between 6 m/s and 7 m/s for England, and between 7 m/s and 8 m/s for Scotland [194-196]. Therefore, developing the wind technologies for the utilisation of renewable wind resources in UK is an important task.

Before any wind turbine is installed, extensive knowledge of the wind characteristics at a specific site has to be gained in the following areas [15]:

- System design – the selection of an appropriate size of wind turbine for a particular site. Hence, information about this site is required such as the wind speed profile and variation, and the status of extreme wind.
- Data analysis – initial wind speed data requires correction for turbine height and an estimation of mean wind speed, as well as the statistics for wind speed variation.
- Performance evaluation – prediction of annual energy production and cost effectiveness based on the wind speed profile at the specific location.
- Operation – a series of data analyse will be used for load and operation management and system maintenance.

In this chapter, the wind speed profile at a specific location – Albemarle site (Latitude = 55:02 N, Longitude = 01:88 W), is analysed once the wind speed correction for the height difference between the testing point and the wind turbine is completed. Also, the mean wind speed and available wind power are estimated. Furthermore, in order to precisely predict the annual energy production of a wind turbine at this specific site, one of the most important parts is that the measurement of the Weibull distribution must be carried out to analyse the probability of wind speed variation.

## 7.2 Estimation of Wind Resource

Actual annual wind speed data from a U.K. wind farm at Albemarle as shown in figure 7.1 was analysed using statistical methods. The height of the test point is 144 metres.

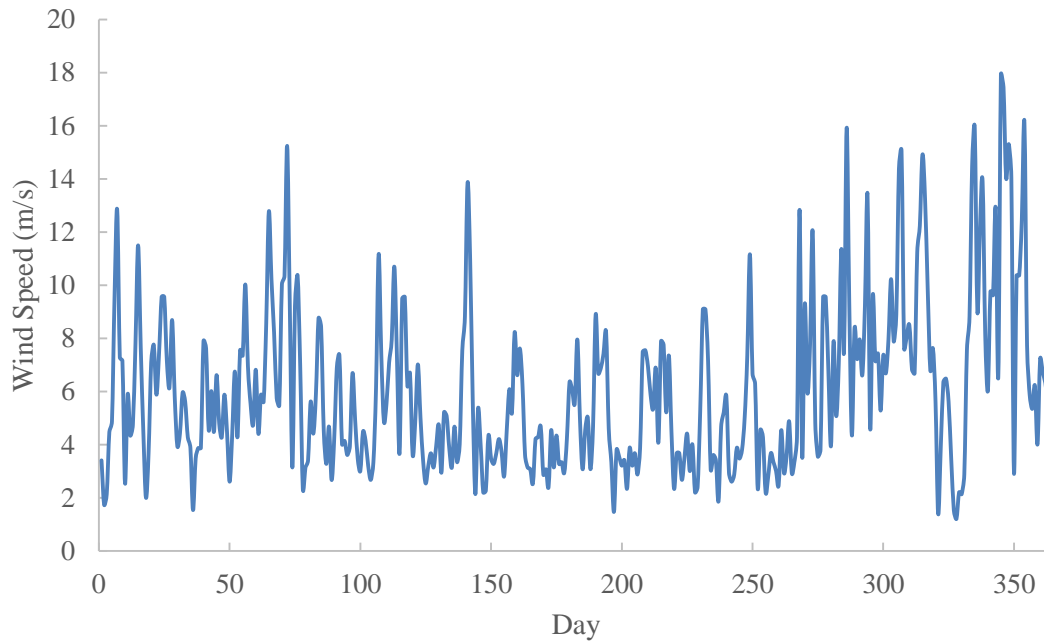


Figure 7.1 Annual wind speed data at Albemarle.

### 7.2.1 Available Wind Power

Assuming that the rotor diameter is 19m, which is one of the largest rotor diameters per rated kW in its class, when the wind is blowing to the turbine, the mass flow of air,  $\frac{dm}{dt}$ , through the swept area of turbine blade  $A_s$ , with air density  $\rho_a$ , and wind velocity  $V_w$ , is given by:

$$\frac{dm}{dt} = \rho_a A_s V_w \quad (7.1)$$

The air density is  $1.225 \text{ kg/m}^3$  in standard condition (sea-level,  $15^\circ\text{C}$ ). So the wind power is shown in equation 7.2, which is proportional to the swept area of the rotor blade and the wind velocity cubed.

$$P = \frac{1}{2} \rho_a A_s V_w^3 \quad (7.2)$$

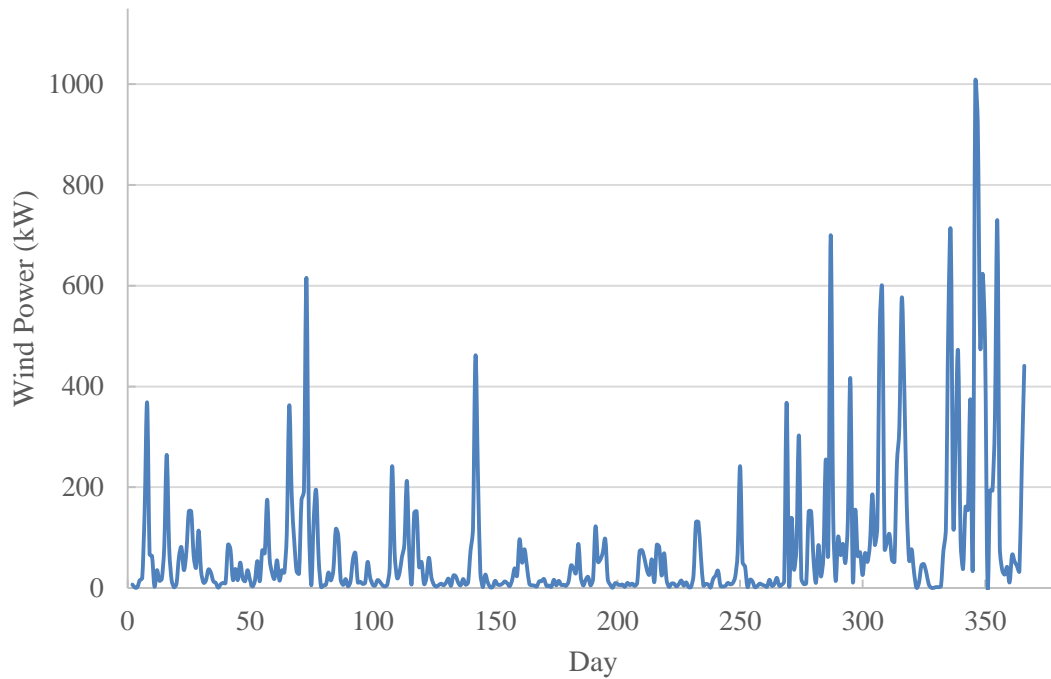


Figure 7.2 Available wind power at Albemarle site.

Figure 7.2 gives the estimation of wind power at the Albemarle site. However, this is an ideal situation. In reality the fluid mechanics of air flow through the turbine blades, their aerodynamics, and the efficiency of the rotor/generator combination have a huge effect on actual power production, which is approximately 45% at most values of available wind power in the best horizontal axis wind turbines [15].

### 7.2.2 Mean Wind Speed

Compared to the direct method of mean value measurement, a more useful calculation of annual mean wind speed  $\bar{V}_w$  over  $N_{ob}$  observations is given by equation 7.3:

$$\bar{V}_w = \left( \frac{\sum_{i=1}^{N_{ob}} V_w^3}{N_{ob}} \right)^{\frac{1}{3}} \quad (7.3)$$

Therefore, the mean wind speed at Albemarle site is about 6.32 m/s.

The estimation of power density is used to evaluate whether or not the wind resource is generally sufficient, but it needs more accurate estimation if hourly wind speed data is available, and so the observed points are for 8760 hours in a year. Then, the average wind power density is determined from hourly mean wind speed  $V_h$  and energy pattern factor  $K_e$  as in equations 7.4 and 7.5.

$$\frac{\bar{P}}{A_s} = \frac{1}{2} \rho_a K_e \bar{V}_w^3 \quad (7.4)$$

$$K_e = \frac{1}{N_{ob} \bar{V}_w^3} \sum_{i=1}^{N_{ob}} V_h^3 \quad (7.5)$$

A wind power density of less than 100 W/m<sup>2</sup> is defined here as a low wind source, which means that this place is not suitable to site a wind turbine; whereas at around 400 W/m<sup>2</sup> it is a good site; A very good wind resource has a power density of more than 700 W/m<sup>2</sup> [15].

### 7.2.3 Power Law Profile

The power law is used to describe velocity with height due to surface roughness and boundary effects, as in the equation shown below:

$$V_2 = V_1 \left( \frac{H_2}{H_1} \right)^\lambda \quad (7.6)$$

where  $V_1$  is the wind speed at a reference height  $H_1$ ,  $H_2$  is the projected height, and  $\lambda$  is the power law exponent.

The power-law component,  $\lambda$ , depends upon the roughness of the surface. For open land,  $\lambda$  is usually chosen as 1/7. From the previous studies [197, 198], the power law exponent is determined as follows:

$$\lambda = \frac{1}{\ln \left( \frac{Z}{Z_0} \right)} \quad (7.7)$$

where  $Z_0$  is the aerodynamic roughness length, which depends on wave characteristics. It can also be computed as shown in equation 7.8 [198, 199]:

$$\frac{Z_0}{H_s} = 1200 \left( \frac{H_s}{L_p} \right)^{4.5} \quad (7.8)$$

where  $H_s$  and  $L_p$  are the significant wave height and peak wave length respectively for the wave spectrum.

The height of the test point at the Albemarle site is 144 metres and the turbine's tower height is 36 metres, so figure 7.3 compares the available wind power captured with two different heights at Albemarle after using power law correction.

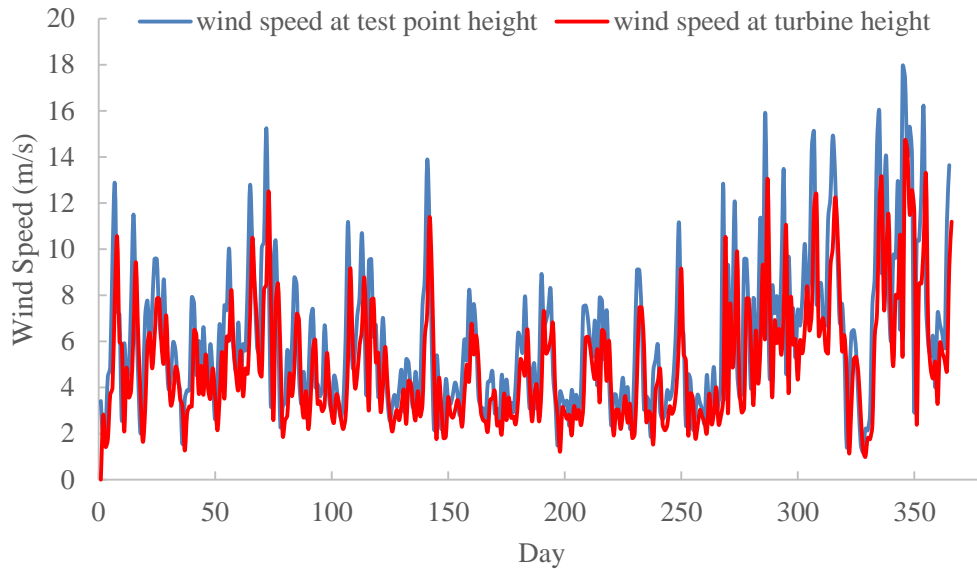


Figure 7.3 Actual wind speed at turbine height.

Therefore, the wind turbine with 19 metres rotor diameter and 36 metres tower height is able to harvest the available wind power at a height lower than the test point, as shown in figure 7.4.

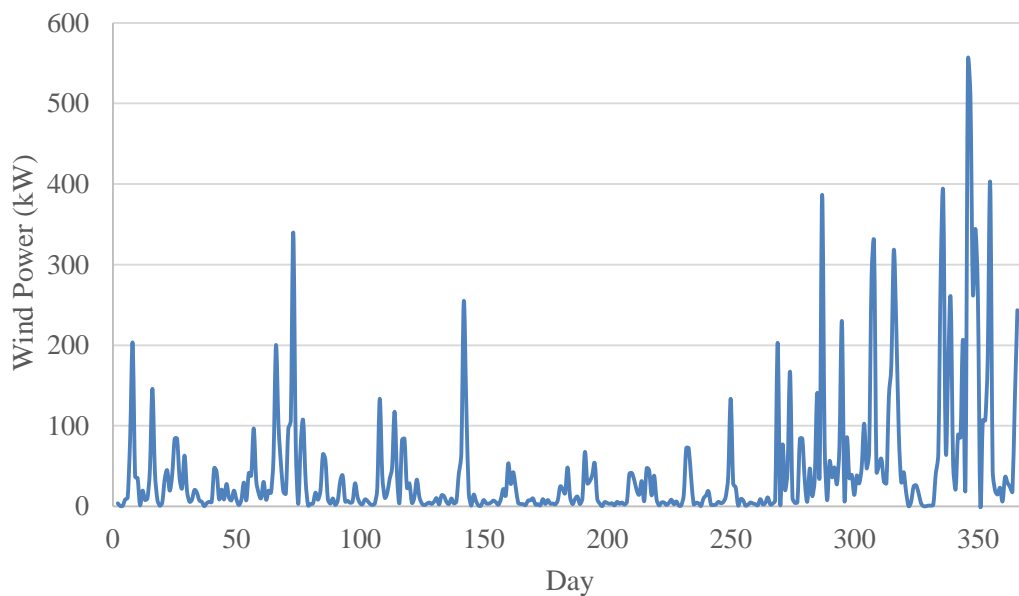


Figure 7.4 Available wind power for wind turbine.

### 7.3 Statistical Analysis of Wind Speed Data

It is very important to describe the variations in wind speed at a specific site and to estimate the annual energy production from a wind turbine located there. To compute a random variable such as wind speed, a probability density function is used to describe the likelihood of wind speeds occurring. Two main types of probability density function are used to fit the distribution of wind speed frequencies: the Rayleigh distribution and the Weibull distribution.

#### 7.3.1 Rayleigh Probability Distribution

The Rayleigh distribution is simpler than the Weibull distribution in representing wind resources, because only one parameter is used: mean wind speed. The Rayleigh probability density function and the cumulative distribution function are expressed as the following equations [15]:

$$f(V) = \frac{\pi}{2} \left( \frac{V_w}{\bar{V}_w^2} \right) \exp \left[ -\frac{\pi}{4} \left( \frac{V_w}{\bar{V}_w} \right)^2 \right] \quad (7.9)$$

$$F(v) = 1 - \exp \left[ -\frac{\pi}{4} \left( \frac{V_w}{\bar{V}_w} \right)^2 \right] \quad (7.10)$$

Therefore, mean wind speed has a direct effect on the pattern of the Rayleigh probability density function, as shown in figure 7.5. When the mean wind speed increases, a larger value of probability density function is given.

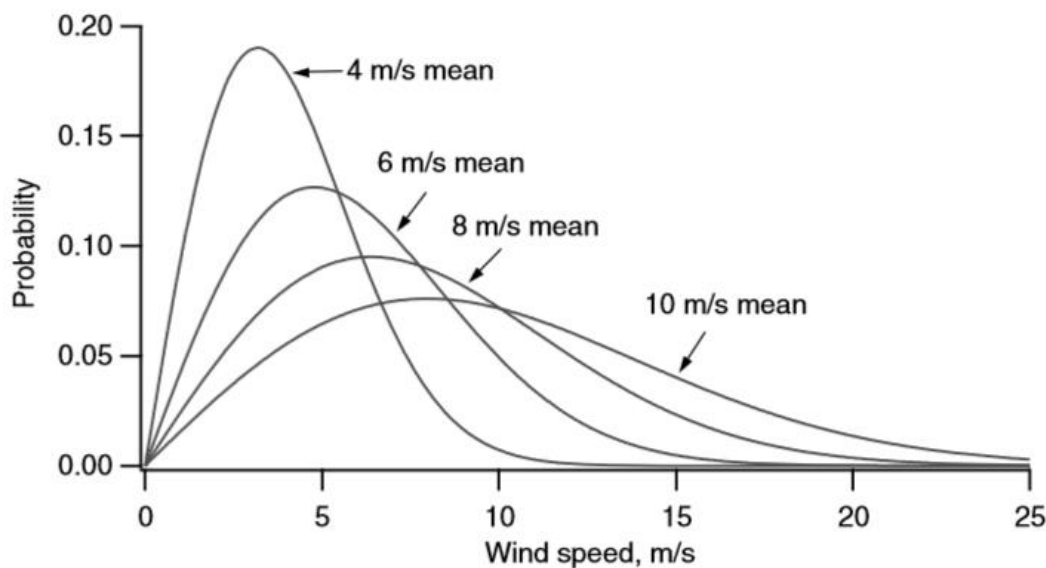


Figure 7.5 Rayleigh distribution with different mean wind speed [15].



### 7.3.2 Weibull Probability Distribution

Unlike the Rayleigh distribution, the Weibull probability distribution adopts two parameters, a shape factor  $k$  and a scale factor  $c$ , in wind speed analysis. This has been shown to give a better and more accurate fit to measured wind speed data [200], and hence it is most commonly recommended. However, situations of extreme wind speeds are not included in the analytic procedure.

The Weibull probability density function is expressed as in equation 7.11.

$$f(V_w) = \frac{k}{c} \left( \frac{V_w}{c} \right)^{k-1} e^{-\left( \frac{V_w}{c} \right)^k} \quad (7.11)$$

The probability function can also be interpreted as a relative fractional probability function, since wind speed exceeds zero in reality. The Weibull cumulative distribution function is given by:

$$F(v) = \int_0^{+\infty} f(V_w) dV_w = 1 - e^{-\left( \frac{V_w}{c} \right)^k} \quad (7.12)$$

Therefore, the most important parameters in the Weibull distribution are the shape and scale factors. The brief description in figure 7.6 shows that with an increasing shape factor increasing, the peak of the curve becomes sharper when the mean wind speed is at a constant value.

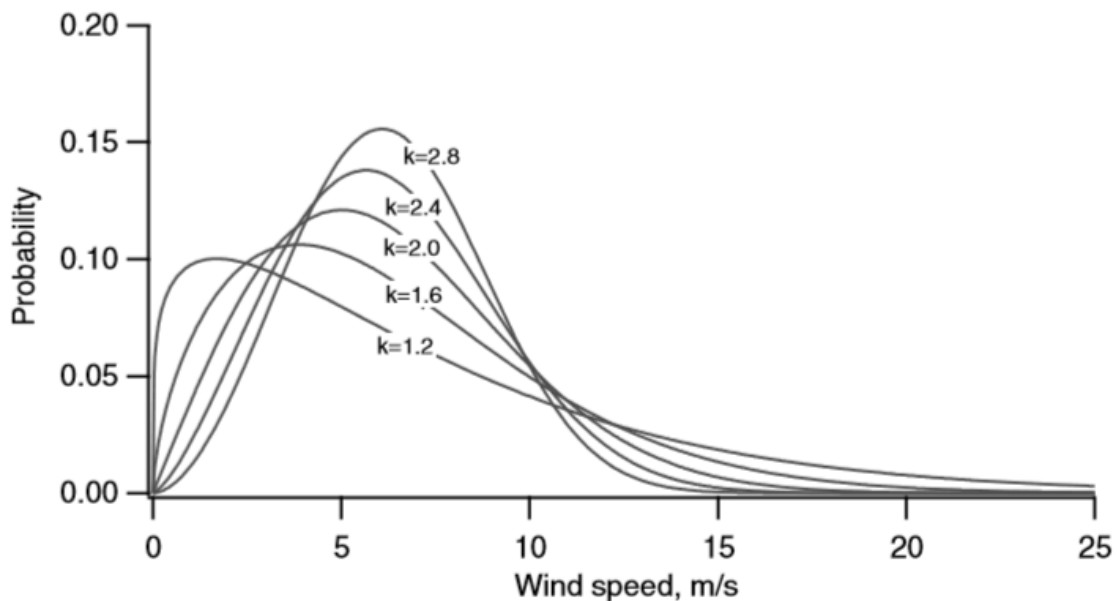


Figure 7.6 Example of the Weibull distribution when mean wind speed is 6 m/s [15].

Several methods have already been used for the estimation of the Weibull distribution parameters, such as statistical estimation, maximum likelihood and graphic methods. Among these, the statistical estimation method uses average wind velocity and standard deviation to estimate the Weibull probability density function based on statistical data of the wind speed. The biggest advantages of this method is simple, convenient, and high precise. Therefore, it was widely used and applied in wind data analysis.

It is worth noting that the shape and scale factors are related to mean wind speed  $\bar{V}$  and standard deviation  $\sigma$  in the Weibull distribution. The mean wind speed describes the main tendency change of in the data and the standard deviation of a sample represents the extent of deviation from the mean wind speed [201]. The standard deviation of wind speed and mean wind speed can be expressed as in equations 7.13 and 7.14.

$$\sigma^2 = \frac{1}{N_{ob}} \sum_{i=1}^{N_{ob}} (V_i - \bar{V}_w)^2 \quad (7.13)$$

$$\bar{V}_w = \left( \frac{\sum_{i=1}^{N_{ob}} V_i^3}{N_{ob}} \right)^{\frac{1}{3}} \quad (7.14)$$

Hence, the standard deviation of the wind speed at Albemarle is 2.94 when the mean wind speed is 6.32 m/s. Therefore, the shape factor can be determined by a good approximation as shown in equation 7.15, but there is a limitation in this approximation, which is that  $1 \leq k < 10$ .

$$k = \left( \frac{\sigma}{\bar{V}_w} \right)^{-1.086} \quad (7.15)$$

So, the shape factor is calculated as 2.29 for Albemarle. The scale factor can also be solved using the gamma function as in equation 7.16.

$$c = \frac{\bar{V}_w}{\Gamma\left(1 + \frac{1}{k}\right)} \quad (7.16)$$

An approximation for the determination of the scale factor, which is shown in equation 7.17:

$$\Gamma\left(1 + \frac{1}{k}\right) = \left(0.568 + \frac{0.434}{k}\right)^{\frac{1}{k}} \quad (7.17)$$

After calculating the gamma function, the scale factor is about 7.133 at Albemarle. Then, the Weibull probability density functions and cumulative distribution functions at different wind speeds can be obtained. It should be noted that in the Weibull distribution there is a special case that when the shape factor  $k=2$ , when it equals the Rayleigh distribution. The Weibull distribution at the Albemarle site is presented in figure 7.7. It can be seen that the highest frequencies of wind speeds occurring are concentrated in the range between 4 m/s to 8 m/s. The Weibull probability density function is hence expressed as in equation 7.18.

$$f(V_w) = 0.321 \times \left( \frac{V_w}{7.133} \right)^{1.29} e^{-\left( \frac{V_w}{7.133} \right)^{2.29}} \quad (7.18)$$

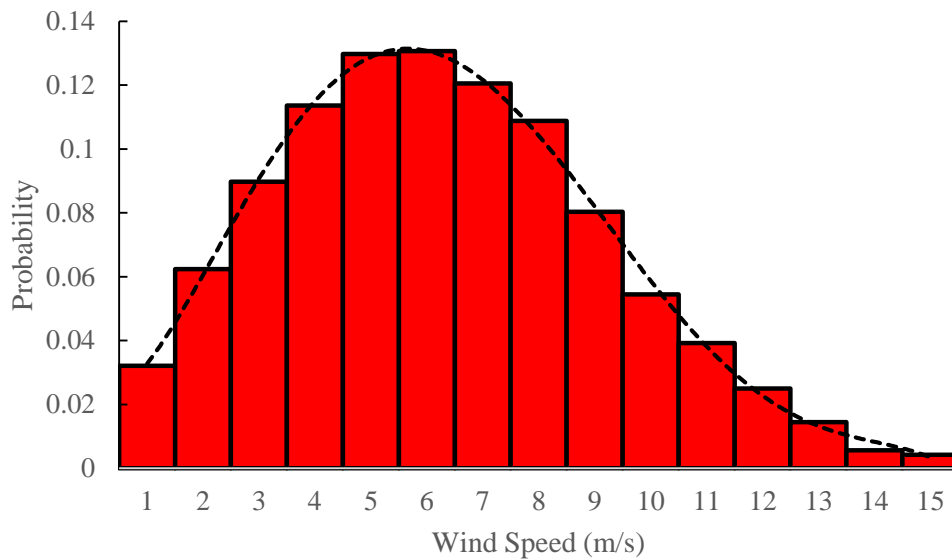


Figure 7.7 Weibull distribution at Albemarle site.

Tables 7.1 and 7.2 present the frequency and average days of various wind speeds in a year at the Albemarle site, which are calculated based on the Weibull distribution. This will then be used to estimate the annual wind turbine energy production.

Table 7.1 Probability of wind speed at Albemarle site

Wind Speed (m/s)	Frequency	Wind Speed (m/s)	Frequency
1	3.18 %	9	7.95 %
2	6.17 %	10	5.39 %
3	8.87 %	11	3.88 %
4	11.24 %	12	2.47 %
5	12.83 %	13	1.43 %
6	12.92 %	14	0.56 %
7	11.92 %	15	0.42 %
8	10.76 %		

Table 7.2 Wind speed of average days in a year

Wind Speed (m/s)	Days in a year	Wind Speed (m/s)	Days in a year
1	11.6	9	29.0
2	22.5	10	19.7
3	32.4	11	14.2
4	41.0	12	9.0
5	46.8	13	5.2
6	47.2	14	2.0
7	43.5	15	1.6
8	39.3	Total	365

## 7.4 Wind Turbine Energy Estimation

### 7.4.1 Power Curve

The power curve of a wind turbine is a graph that indicates how large the electrical power output will be for the turbine at different wind speeds. In this thesis, the pitch control is chosen as shown in figure 7.8, and there are three regions in the power curve of turbine power output with a steady wind speed.

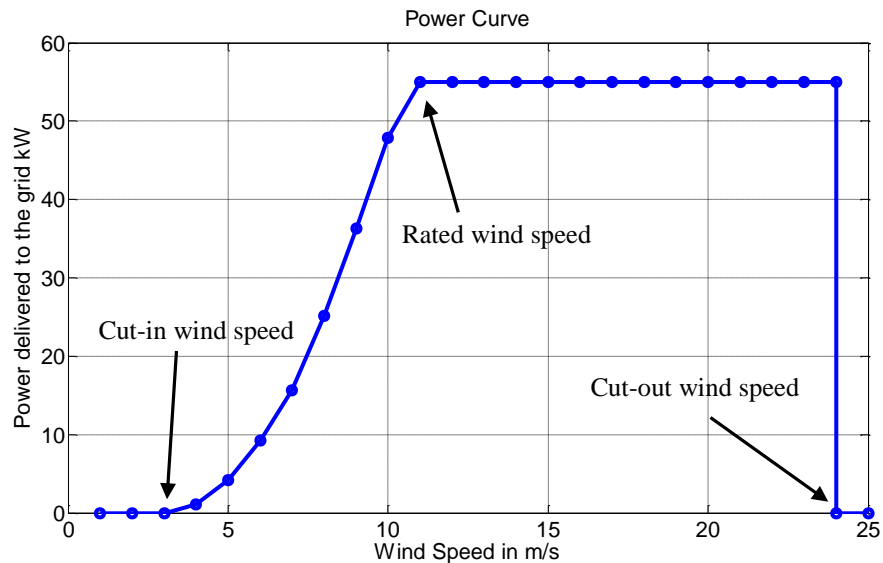


Figure 7.8 Wind turbine power curve.

When the wind speed is below 3 m/s, the wind is not able to provide sufficient torque to rotate the turbine blades. As the wind speed increases up to the cut-in speed of about 3 m/s, the wind turbine will start to rotate and generate power output; in the rated power output region, electrical power rises cubically with wind speed increasing to the rated speed of 11 m/s, and then the power output reaches a steady state, which is the rated power output. In this region, the turbine will generate rated power even if the wind speed is still increasing. Finally, there is a third region where the turbine rotor may be damaged when the wind speed exceeds the cut-out speed of 24 m/s. However, the power curve cannot be used to calculate the power generation of the wind turbine at any specific average wind speed. If the power curve was used to calculate energy production, the estimated results would not be close to real power production. This is because wind power varies significantly with wind speed. The average wind speed is more relevant, and also the wind power is proportional to the cube of wind speed at the site.

### 7.4.2 Betz Law

A German physicist, Albert Betz, concluded that a wind turbine is not able to convert more than 16/27 of the kinetic energy of wind into mechanical energy [202]. This is known as the Betz Law. The power coefficient of wind turbine can be expressed in equation 7.19.

$$C_p = \frac{P_{rotor}}{\frac{1}{2} \rho_a A_s V_w^3} = \frac{Rotor\ Power}{Wind\ Power} \quad (7.19)$$

In theory, the maximum power coefficient  $C_{pmax}$  for any wind turbine design is 16/27, which is defined as in equation 7.20:

$$C_{pmax} = \frac{16}{27} = 0.5926 \quad (7.20)$$

However, only an ideal wind turbine can operate with the maximum power coefficient. In reality, the real power coefficient is between 0.35 to 0.45 after taking into account various inevitable losses, such as bearing, gearbox, and generator losses [203], so that only approximately 10-30% of the wind power can be converted into usable electricity. In this work, the conventional efficiency of 30% is assumed. Figure 7.9 gives a clear comparison of the wind power wastage at the Albemarle site.

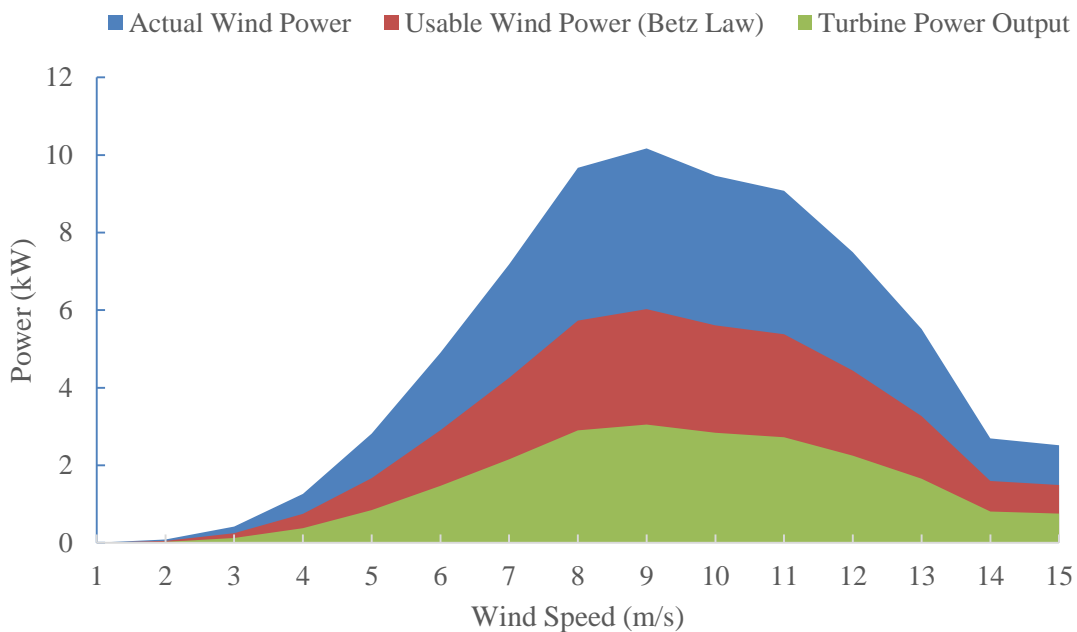


Figure 7.9 Wind power wastage.

### 7.4.3 Wind Turbine Annual Energy Production

The basic information about the wind turbine can be used to determine its annual power output. Combined with the Weibull probability density function  $p(V_w)$ , the average wind turbine energy production can be expressed as in equation 7.21.

$$\bar{P}_w = \int_0^{\infty} P_w(V_w) p(V_w) dV_w \quad (7.21)$$

Therefore, taking into consideration the drive train efficiency (generator power/rotor power)  $\eta_1$  and generator efficiency  $\eta_2$ , another equation for the average power output of a turbine generator is given by equation 7.22:

$$\bar{P}_w = \frac{1}{2} \rho_a A_s \eta_1 \eta_2 C_p \int_0^{\infty} V_w^3 p(V_w) dV_w \quad (7.22)$$

In figure 7.10, the energy production with different wind speed and the Weibull distribution are presented, and hence can be used to estimate actual annual energy production.

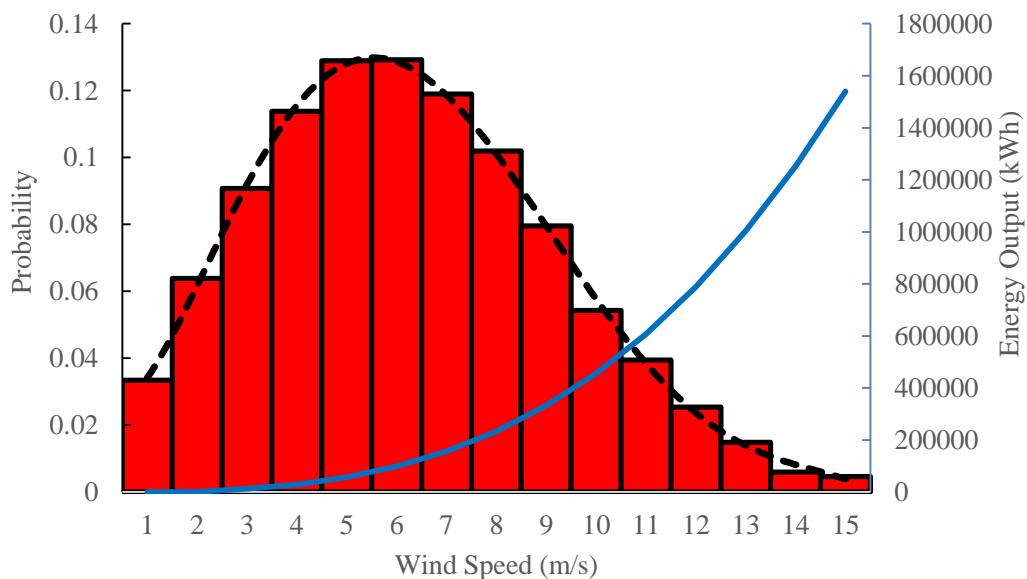


Figure 7.10 Estimation of annual energy production.

Assuming that drive train efficiency has a constant value, the annual energy production based on the wind speed profile at the given site can be found to be approximately 192.3 MWh. Detailed information about annual energy production is shown in Table 7.3 and Figure 7.11.

Table 7.3 Annual Energy Production

Wind Speed (m/s)	Energy Production (kWh)	Wind Speed (m/s)	Energy Production (kWh)
1	0	9	26724.83
2	0	10	24868.69
3	1105.608	11	23852.63
4	3318.09	12	19692.09
5	7401.433	13	14492.85
6	12879.1	14	7078.476
7	18870.98	15	6613.235
8	25411.29	Total	192309.3

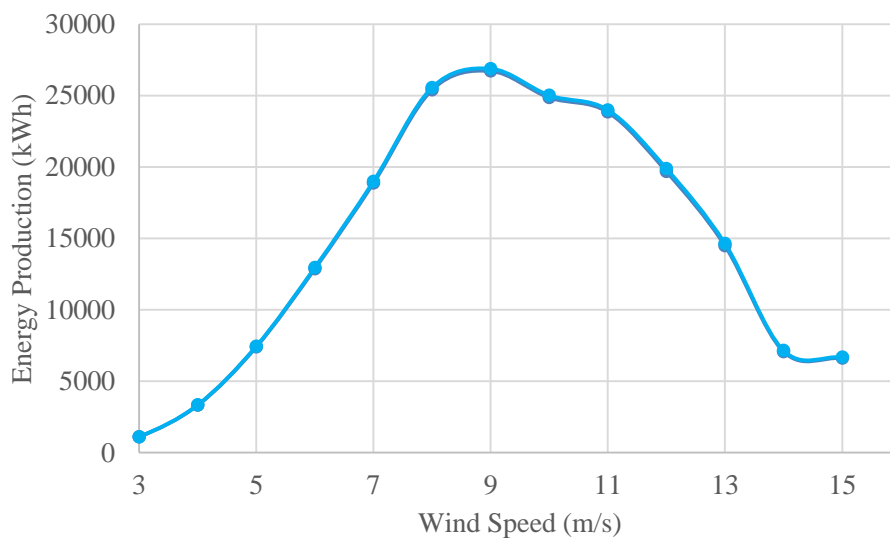


Figure 7.11 Annual energy production at Albemarle site.

#### 7.4.4 Improved Annual Energy Production

As referred to in section 7.3, no power is generated from the wind turbine in the first region, and so the wind speed data in this area is not relevant to the performance of a turbine generator. Then, with increasing wind speed, the turbine power output increases rapidly until the rated wind speed is reached. This is the power increase area. The turbine generator then begins to produce electrical power in sub-synchronous operational mode since the wind speed is between 3 to 11 m/s, and the rotational speed range of the turbine generator is from 1200 rpm to a value less than 1500 rpm. From figure 7.12, it can be found that the higher probabilities of wind speed



always appear between 3 to 9 m/s, and so efficiency improvement is focused on sub-synchronous operational mode. The final region is the constant power output area when the wind speed exceeds the rated wind speed of 11 m/s. The DFIG is then running in the super-synchronous operational mode since the generator speed is above 1500 to 1800 rpm.

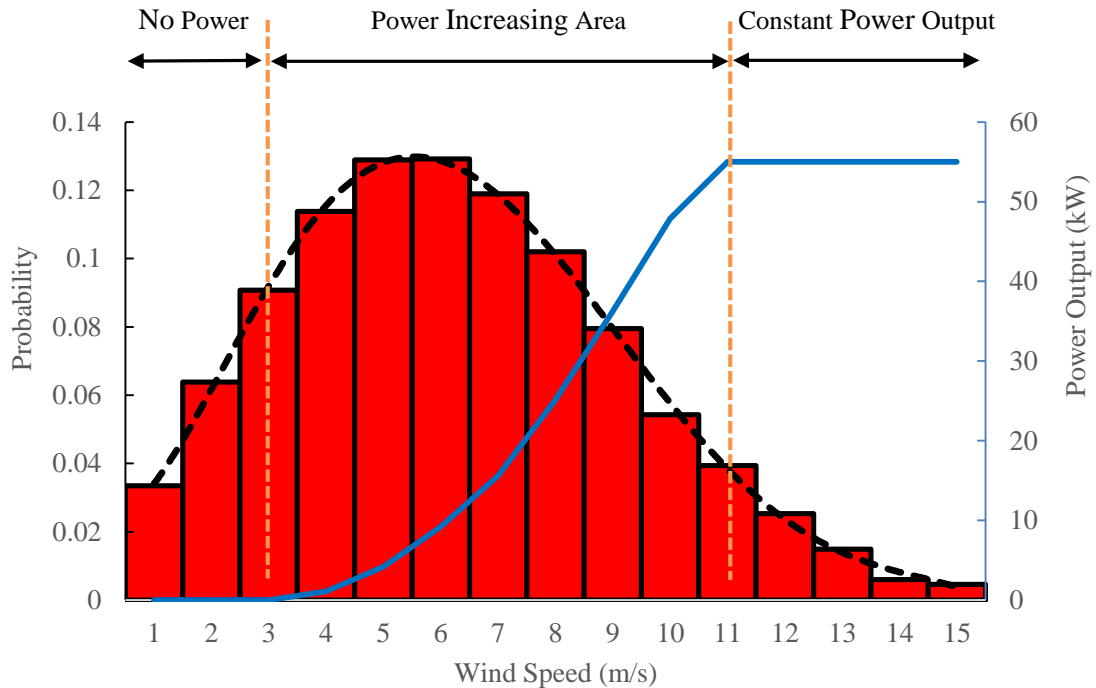


Figure 7.12 High probability area with turbine power curve.

Because the wind turbine adopts the pitch control, the power generation is kept constant of 55 kW once the rated power level is achieved. Therefore, the improved efficiency of the optimised rewind machine is only affect power increase area. In the power increase area, as referred to in Chapter 6, the efficiency of the optimised rewind DFIG is improved by about 0.9%, 0.4%, and 0.6% at 1200, 1300, 1457 rpm respectively, as shown in figure 7.13. So, based on equation 7.22, the improvement of the annual energy production is about 106.43, 228.65, and 452.68 kWh at these three generator rotational speed levels. Hence, the total improvement in annual energy production is 787.76 kWh.

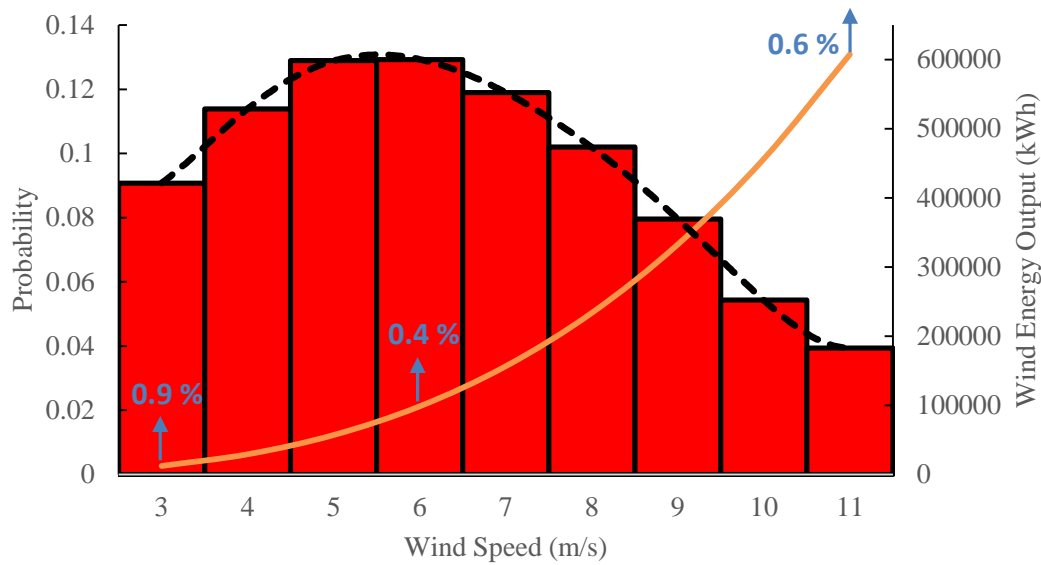


Figure 7.13 Improvement in annual energy production.

As a result, in this case study of a 55 kW wind turbine, if the price for 1 kWh of electricity is £0.145, then after winding repair and re-design, the extra saving per year is about £114.225. It can be imagined that the repair and re-design of a mega-watts wind turbine generator could save much more, so £114.225 on a 55 kW wind turbine could be scaled up to £4153.636 on a 2 MW wind turbine per year, if applied to 50 2-MW DFIG wind turbines over 5 year lifetime, the total of 1 million pounds are saved.

The greatest interest of this work is to improve the machine efficiency to obtain the maximum power generation; in the meanwhile, an alternative way of illustrating wind turbine performance is to check the capacity factor,  $CF$ , for the turbine in a specific location. The capacity factor is the energy actually produced by the turbine divided by the theoretical rated power output  $P_R$ , which is expressed as in equation 7.23.

$$CF = \frac{\bar{P}_w}{P_R} \quad (7.23)$$

Therefore, the capacity factors of the original wind turbine and optimised wind turbine are 39.91% and 40.19% respectively. Due to the efficiency of the optimised rewind DFIG is higher than the original DFIG, so the average power output of a wind turbine is improved accordingly, which means that the optimised wind turbine gives better performance than the original.

## 7.5 Summary

The status of the wind resource and its characteristics has been introduced in this chapter, presenting the different types of wind speed variation and the effects of wind speed at different locations. The available wind power and mean wind speed have been estimated from the wind speed profile of a specific location at Albemarle site. The power law is used to correct the actual wind speed for turbine height, since the wind speed data is obtained from a specific test point higher than the turbine height. The Weibull distribution has been chosen to analyse the probability density of wind speed variations at the Albemarle site in this thesis, since research into the most important factors in the Weibull distribution, the shape and scale factors, was carried out using the statistical estimation method. Betz Law states that only part of available wind power can be harvested by a wind turbine, and a series of mechanical losses also reduces the utilization of wind power. The process of determining the annual energy production of a wind turbine at the given site has been demonstrated, which is combined with the Weibull probability density function, turbine power curve, and wind speed data. In this work, according to the winding re-design and optimisation, the stator copper loss of the DFIG machine is reduced to improve efficiency. So a comparison has been conducted of annual energy production in the original and the optimised rewound DFIG wind turbines and the capacity factors for both wind turbines have been determined.

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## Chapter 8 Conclusions

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The key points and important outcomes of the thesis are summarised in this chapter. The winding repair and re-design of a doubly fed induction generator to obtain the maximum wind energy production has been studied. This chapter also includes suggestions for future work.

### 8.1 Conclusions

The work of this thesis has been carried out in a number of steps.

First of all, the relevant literature has been reviewed in Chapter 2, and this has shown that the doubly fed induction generator (DFIG) has huge potentials to be developed for wind energy applications due to the overall considerations of cost, eco-friendliness, and machine performance. The estimation of wind energy production is significantly related to the turbine topology used, and much work has been undertaken on the design and topologies of modern wind turbine generators. Nowadays, the specific sized DFIGs from different wind turbine manufacturers are mass-produced, which have their fixed generator structure and winding configurations. They are designed and operated for a large range of wind speed, so the problem of modern DFIGs is that they are not running at the best operation point generally. When the failure occurs in the turbine generator, it needs to be repaired and re-designed for safety reasons. A study of turbine failures has highlighted winding faults in either the stator or the rotor. Current opinions on repairing or replacing the generator with faulty winding were described, whilst winding repair generally are attempted to return to the original design. However, in this thesis a new viewpoint on winding repair is proposed, because it is a good opportunity to re-design and optimise the winding configuration while the machine is being repaired in order to achieve better performance than before.

The mechanical aspects of an existing doubly fed induction generator such as winding configuration and laminations of the stator and rotor, have been studied in Chapter 3. In order to improve machine efficiency, a study of the major power losses in DFIGs is presented and analysed. This shows the characteristics and determination of conventional losses and additional loss. An off-the-shelf 55kW, 4-pole, three-phase DFIG was modelled with an electromagnetic finite element tool in order to validate the optimisation process, and the model was solved by a 2-D transient with a motion optimiser. Its inclusion is important to validate the

model's accuracy via electromagnetic field and loss analysis in different components in the machine. However, some limitations in the finite element analysis were also identified; these are that the stray load loss cannot be estimated and nor can windage and friction losses be included. A novel method of combining finite element analysis with an evolutionary optimisation algorithm had been chosen to optimise the DFIG's windings.

The novel approach to the winding re-design and optimisation of the DFIG was then focused in Chapter 4. Based on the original design (stator: 16 turns with  $4.29 \text{ mm}^2$  cross-sectional area, rotor: 12 turns with  $6.95 \text{ mm}^2$  cross-sectional area), a process of finite element-based surrogate optimisation algorithm has been deployed to explore which combination of winding turn and cross-sectional area of the stator and rotor has the highest efficiency. In this procedure, the design of experiment is used to allocate the sampling points in the design space, in order to minimise the time consumed and maximise the information acquired from a trade-off between the number of selected points and the amount of information. The Latin Hypercube sampling technique is the DoE technique selected to generate the random and uniform sampling distributions. This has led to the maximising the amount of information acquired with the minimum bias error, since a totally 34 and 36 sampling points were selected to build the surrogate model of the stator winding and rotor winding. These sampling points have been used in the finite element programme to obtain the numerical results of the electromagnetic analysis. The results have then been further used to build the surrogate model of the DFIG and the Kriging model takes the finite element outputs to estimate the value or response of a function in the unknown area. The errors in the estimation fluctuate around the real function. With more sampling points selected, the estimated function will become closer to the real function. The optimisation algorithm is then developed to find the optimal location, once the surrogate model is created. In addition, the particle swarm optimisation algorithm has already been proven to be an efficient method, and has been adopted to find the best solution of the DFIG windings. The optimised winding parameters for the stator and rotor windings are 14 turns with  $5.21 \text{ mm}^2$  cross-sectional area and 10 turns with  $5.94 \text{ mm}^2$  cross-sectional area, respectively. The optimisation results have been successfully validated using the finite element analysis.

The optimised plan of the DFIG has been implemented, with the design of the machine winding parameters learned along the way. The American IEEE standard 112-B for polyphase induction machine testing has then been selected after comparison with other international testing standards, due to its relatively higher precision. The IEEE standard 112-B is used for conventional induction machine testing, but is found to be difficult to satisfy the requirements of this work. An improved testing method based on IEEE standard 112-B has been developed

to measure generator efficiency using an input-output method with loss segregation as described in Chapter 5. In this method, the determination of the machine efficiency at sub-synchronous and super-synchronous operational modes should be conducted separately. Meanwhile, the converter efficiency of 95% has already been considered with grid-side rotor power. The original and optimised rewind DFIGs have been tested based on this improved testing method and presented in Chapter 6. The two machines are compared using the same method and conditions. The no-load tests on the machines were used to determine the core loss and windage and friction loss, the core loss of 521.47W and windage and friction loss of 1280.61W in the optimised rewind DFIG has a slight increasing than that of 501.95W and 1136.44W in the original DFIG. The load tests were used to determine conductor losses, stray load loss, and machine efficiency. The tests show that the stator conductor loss in the optimised rewind machine reduces significantly than the original machine, but the rotor conductor loss only increases slightly. Overall, the optimised rewind DFIG has 0.9%, 0.4%, and 0.6% efficiency improvement than the original machine at 1200, 1300, and 1457 rpm during the sub-synchronous mode, respectively. In the super-synchronous operational mode, the machine efficiency of the optimised rewind DFIG has improved by 1%, 1%, and 1.3% than the original DFIG at 1600, 1700, and 1800 rpm, respectively.

Finally Chapter 7 has focused on the estimation of the annual wind energy production at a specific site in the UK. The wind speed and direction vary randomly, and are also dramatically affected by the surrounding environment. The wind speed profile of the Albemarle site was analysed by combing the processed wind speed results with the turbine topology and tower height following the Power Law and Betz Law. In addition, the Weibull distribution had been employed to calculate the probability of the annual wind speed for annual power production. Two 55 kW DFIGs were used on the wind turbine as a case study, and the annual wind energy production had been further calculated by considering all of the factors involved. The efficiency improvement of turbine generator lead to the increased annual energy production of 787.76 kWh, and the economic saving is £114.225 per year for one 55 kW wind turbine after winding re-design. If it is then scaled up to 50 2 MW DFIG wind turbines for 5-year operation, the total amount of 1 million pounds could be saved.

From this work, it is evident that the machine efficiency of turbine generators can be improved during machine repair and rewinding procedures by incorporating the site-specific wind profile and machine operational characteristics. This is more significant for the wind turbines operating towards the end of their service life. A key message from this work is that the industrial mind-set needs to be changed. That is, the machine rewinding holds a unique opportunity to resign

the machine, instead of faithfully following the original design, which is presently the common practice in industry. By doing so, the wind power industry will benefit from this work by the increased productivity. The society will benefit from the growing penetration of renewable energy in the power network. In the long run, everyone on the planet will benefit by the significant reduction of greenhouse gas emissions to the atmosphere.

## 8.2 Future work

With the work presented in this thesis, a few key areas are open for further investigation and exploration:

- Further investigation might apply the surrogate optimisation algorithm to the structural optimisation of different parts of electrical machines, such as slot shape and the size of internal components, since it has been proven to give good performance for the electromagnetic design.
- For specific industrial applications, the optimisation objectives and constraints can be defined more flexible, such as high torque density and low torque ripple. Therefore, the surrogate optimisation can be used in a wide range of applications.
- Further investigation of multi-objective and multi-variable optimisation can be explored to solve more complex problems, such as the efficiency improvement and cost reduction.
- The environment surrounding a wind turbine in a specific location is not always flat, and it has been shown that the terrain with obstacles has a significant effect on wind speed and characteristics. Considering all the factors influencing wind turbine operation, more accurate short-termed wind speed data are needed for statistical analysis.

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## Appendix

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### A. Thermocouple

The winding temperature is very important to accurately measure the conductor losses in the DFIG machine. According to the PT 100 thermocouple, to determine the winding temperature by measuring its resistance, Figure A.1 and Table A.1 show the detailed resistance of PT 100 with temperature varying.

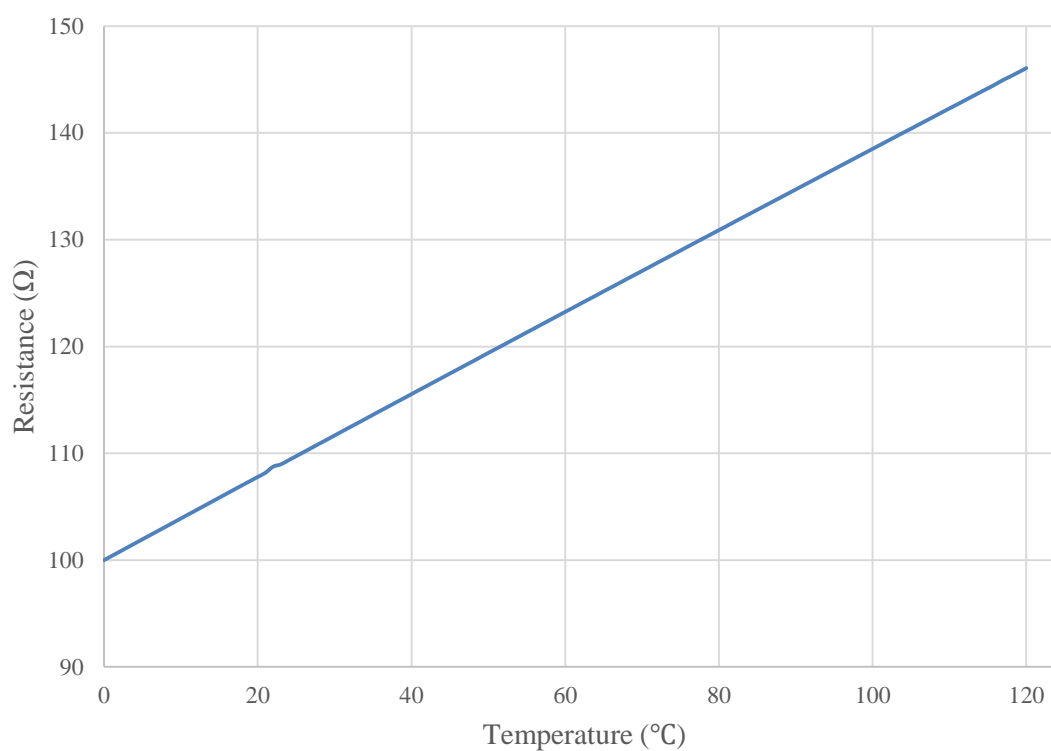


Figure A.1 Determination of winding temperature using PT 100 thermocouple.

Table A.1 Characteristic of PT 100 thermocouple.

Temperature	0	1	2	3	4	5	6	7	8	9	10
-100	60.25	59.85	59.44	59.04	58.63	58.22	57.82	57.41	57	56.6	56.19
-90	64.3	63.9	63.49	63.09	62.68	62.28	61.87	61.47	61.06	60.66	60.25
-80	68.33	67.92	67.52	67.12	66.72	66.31	65.91	65.51	65.11	64.7	64.3
-70	72.33	71.93	71.53	71.13	70.73	70.33	69.93	69.53	69.13	68.73	68.33
-60	76.33	75.93	75.53	75.13	74.73	74.33	73.93	73.53	73.13	72.73	72.33
-50	80.31	79.91	79.51	79.11	78.72	78.32	77.92	77.52	77.13	76.73	76.33
-40	84.27	83.88	83.48	83.08	82.69	82.29	81.89	81.5	81.1	80.7	80.31
-30	88.22	87.83	87.43	87.04	86.64	86.25	85.85	85.46	85.06	84.67	84.27
-20	92.16	91.77	91.37	90.93	90.59	90.19	89.8	89.4	89.01	88.62	88.22
-10	96.09	95.69	95.3	94.91	94.52	94.12	93.73	93.34	92.95	92.55	92.16
0	100	100.39	100.78	101.17	101.56	101.95	102.34	102.73	103.12	103.51	103.9
10	103.9	104.29	104.68	105.07	105.46	105.85	106.24	106.63	107.02	107.4	107.79
20	107.79	108.18	108.57	108.96	109.35	109.73	110.12	110.51	110.9	111.28	111.67
30	111.67	112.06	112.45	112.83	113.22	113.61	114	114.38	114.77	115.15	115.54
40	115.54	115.93	116.31	116.7	117.08	117.47	117.85	118.24	118.62	119.01	119.4
50	119.4	119.78	120.16	120.55	120.93	121.32	121.7	122.09	122.47	122.86	123.24
60	123.24	123.62	124.01	124.39	124.77	125.16	125.54	125.92	126.31	126.69	127.07
70	127.07	127.45	127.84	128.22	128.6	128.98	129.37	129.75	130.13	130.51	130.89
80	130.89	131.27	131.66	132.04	132.42	132.8	133.18	133.56	133.94	134.32	134.7
90	134.7	135.08	135.46	135.84	136.22	136.6	136.98	137.36	137.74	138.12	138.5
100	138.5	138.88	139.26	139.64	140.02	140.39	140.77	141.15	141.53	141.91	142.29
110	142.29	142.66	143.04	143.42	143.8	144.17	144.55	144.96	145.31	145.68	146.06

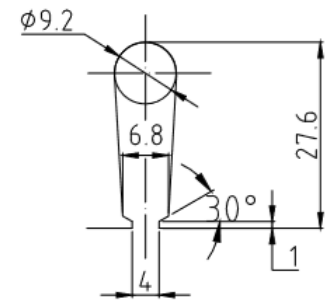
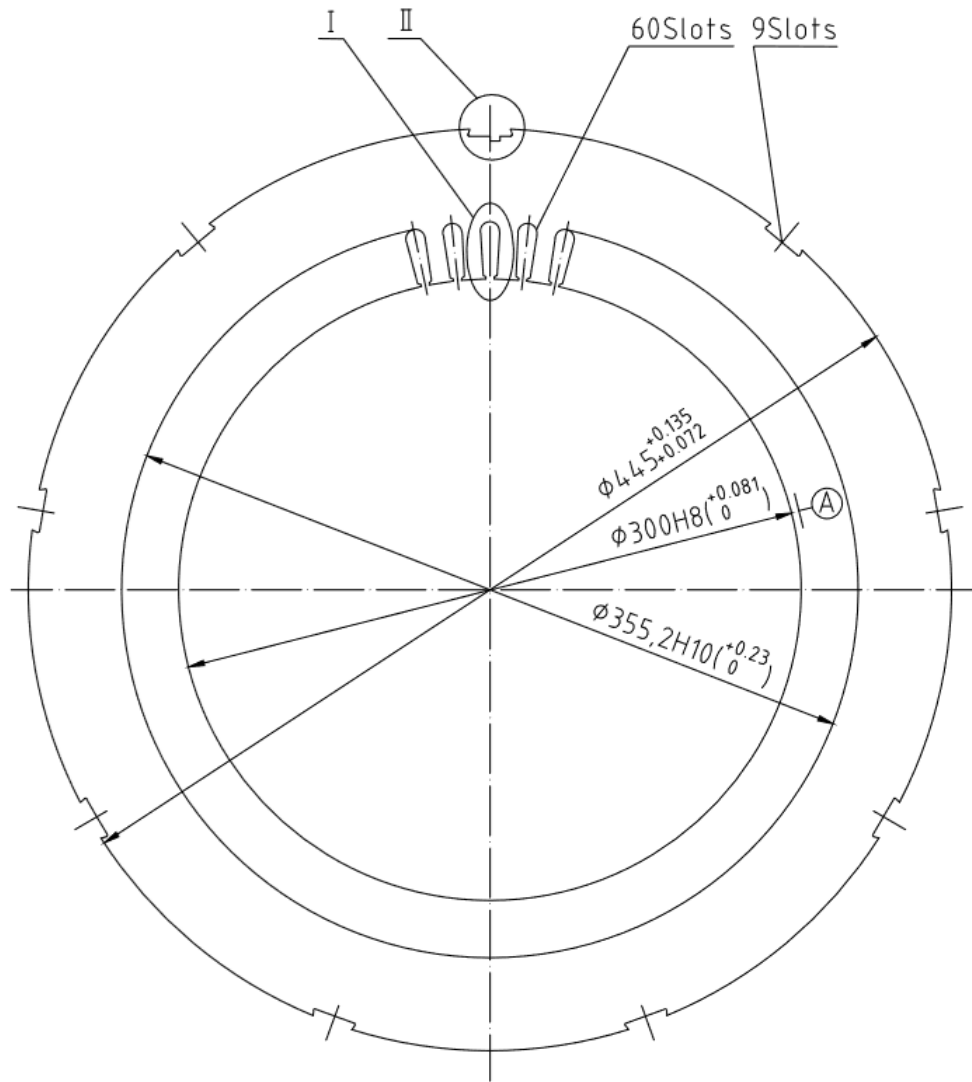
## B. Mechanical Structure of the DFIG

Table B.1 Stator parameter for the DFIG

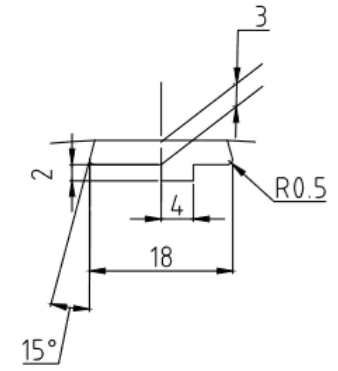
Stator outer diameter	445 mm
Stator inner diameter	300 mm
Stator slot depth	27.6 mm
Pole	4
Stator slot area	193.24 mm <sup>2</sup>
Number of stator slots	60
Stator winding layer	Double layer
Stator coil pitch	1-14
Stator winding material	Copper 100% IACS
Stator winding connection	2 delta

Table B.2 Rotor parameter for the DFIG

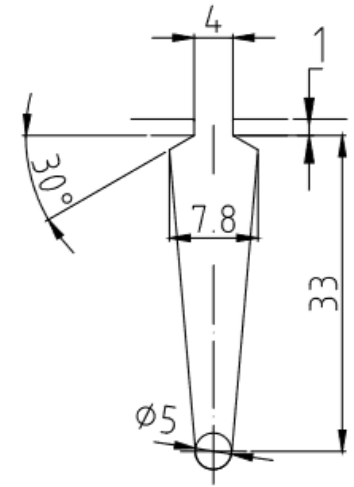
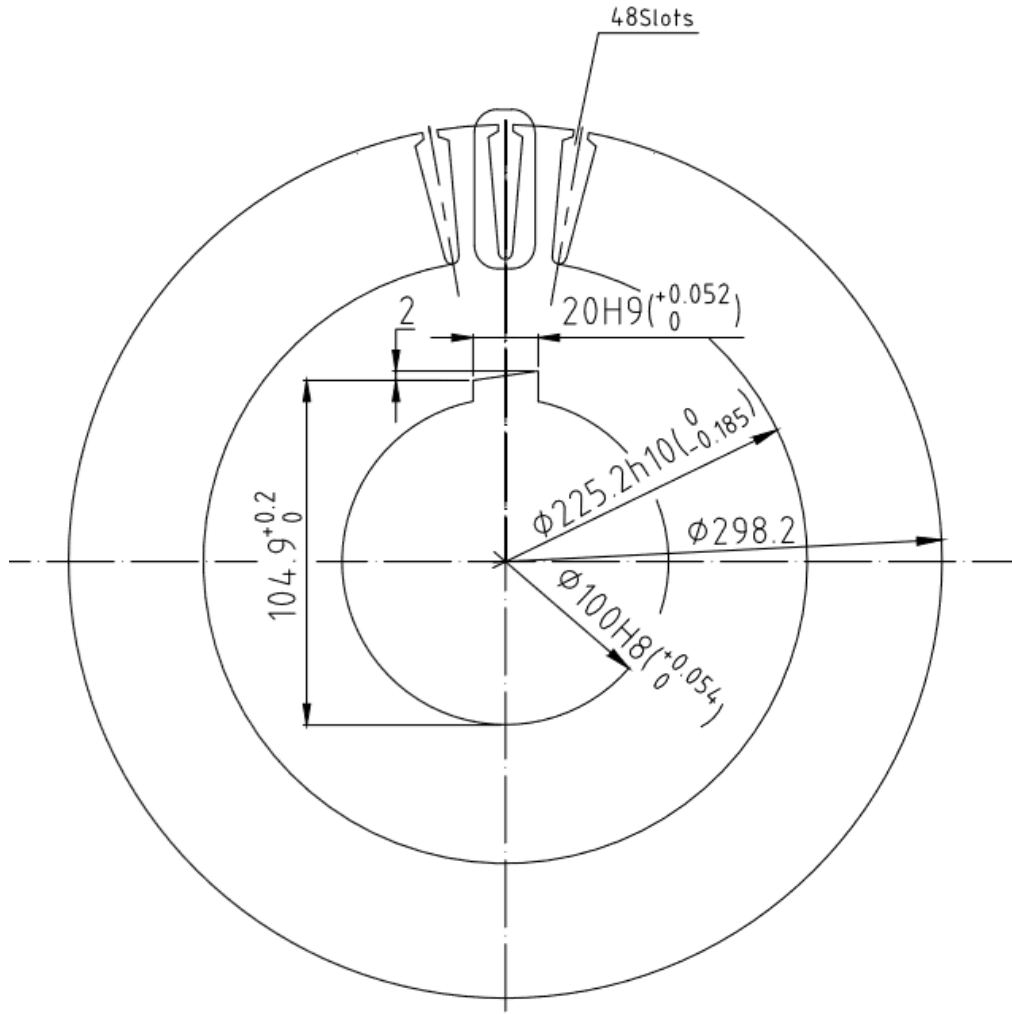
Rotor outer diameter	298.2 mm
Rotor inner diameter	100 mm
Rotor slot depth	36.5 mm
Pole	4
Rotor slot area	223.29 mm <sup>2</sup>
Number of rotor slots	48
Rotor winding layer	Double layer
Rotor coil pitch	1-12
Rotor winding material	Copper 100% IACS
Rotor winding connection	2 star



I



II



### C. Measurement of Winding Resistance



Figure C.1 Stator winding resistance measurement.

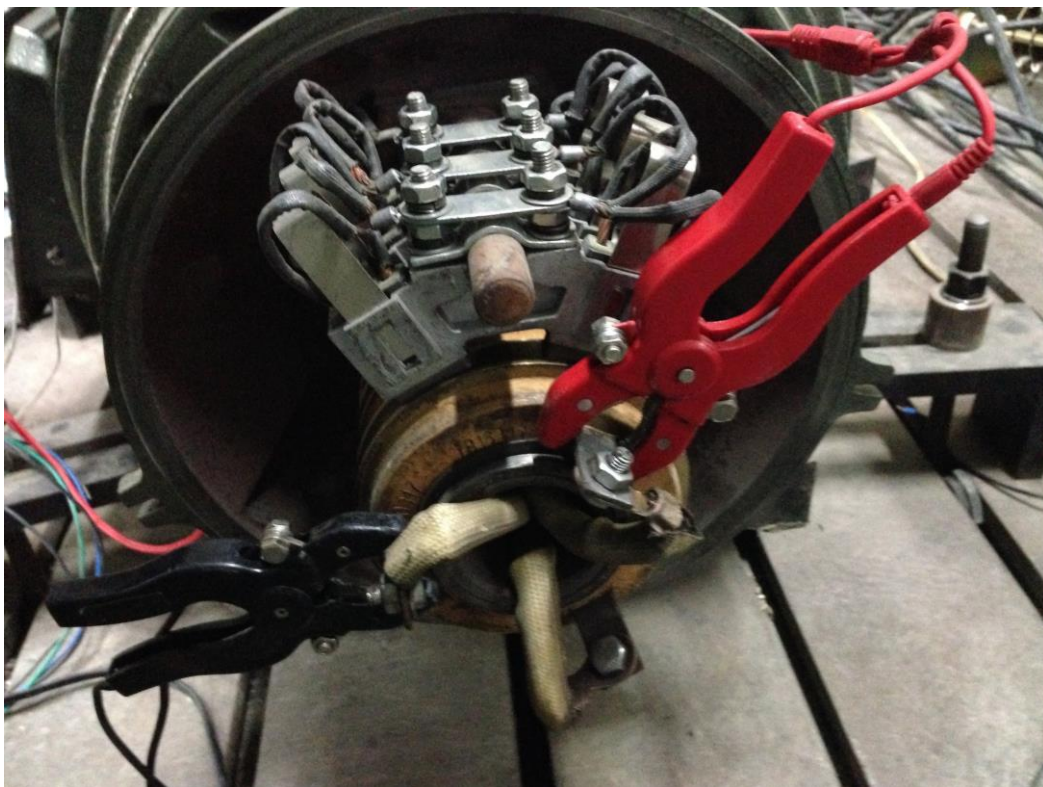


Figure C.2 Rotor winding resistance measurement.



D. No-Load Test

